

Evidence for line nodes in superconducting gap (*d*-wave superconductivity ?) of $(\text{K},\text{Na})\text{Fe}_2\text{As}_2$

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HTS-2013
Zvenigorod

Single crystals of $K_{1-x}Na_xFe_2As_2$:
S. Aswartham, I. Morozov, M. Roslova, S.
Wurmehl

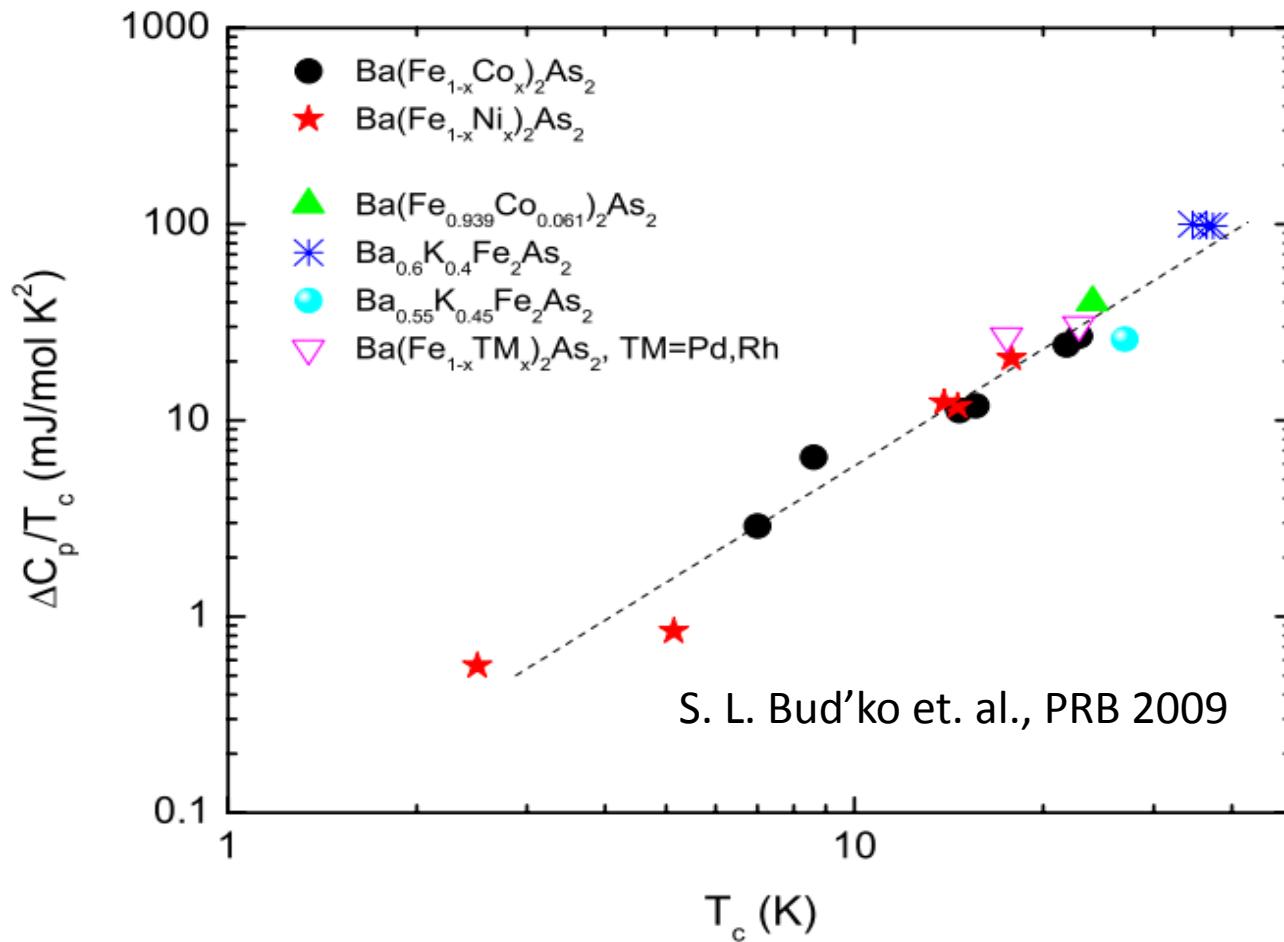
Experiment:

**M. Abdel-Hafiez, O. Vakaliuk, D. Gruner, E. L. Green, M.
Kumar, J. P. Vogt, A. Reifenberger, C. Enss, M. Hempel, R.
Klingeler, A.U.B. Wolter, B. C. Hess, B. Holzapfel, J. Wosnitza, B.
Büchner**

Theory:

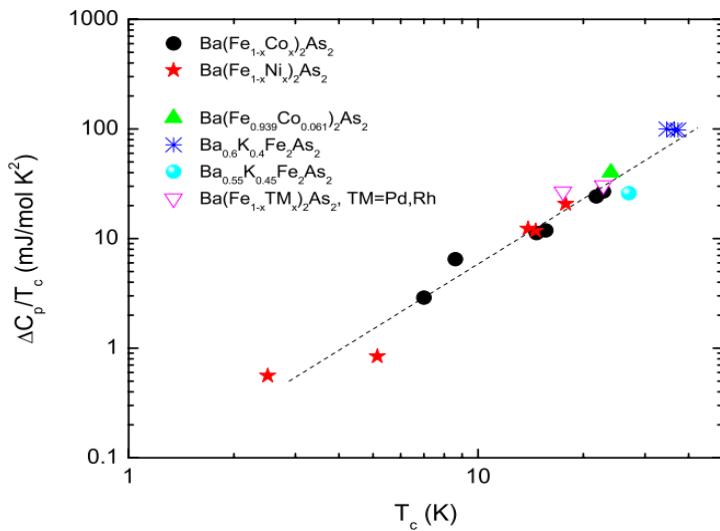
**D. Efremov, S. Johnston, H. Rosner, S.-L. Drechsler,
J. van den Brink**

BNC scaling $\Delta C \propto T_c^3$



Empirical scaling holds for 122 iron-pnictides

BNC scaling is expected in the limit of strong pair-breaking within BCS theory for d -wave or $s\pm$ SC gap

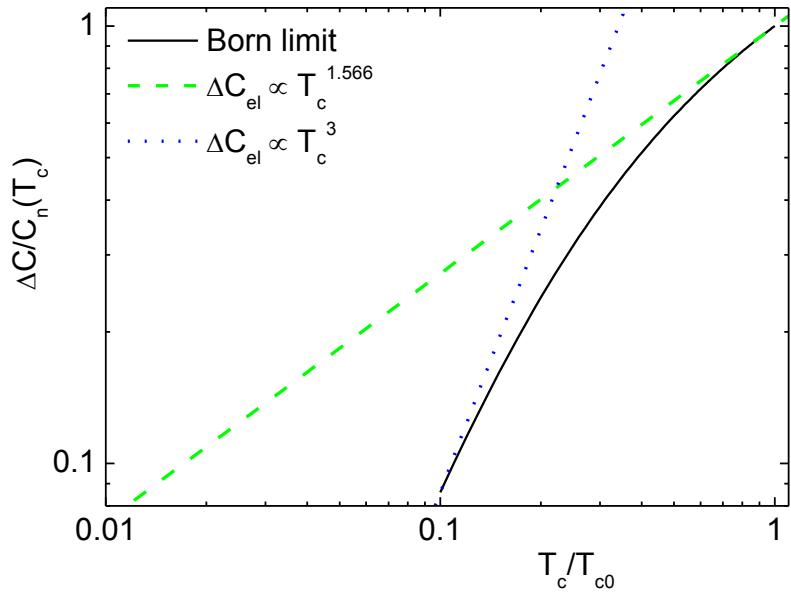


E. Pushkarov and K. Maki, Eur. Phys. J. B 4, 191 (1998)
L.A. Openov, Phys. Rev. B 69 224516 (2004)
V.G. Kogan Phys. Rev. B 80, 214532 (2009)

$$\Delta C = C_s - C_n = \frac{16\pi^4 k_B^4 N(0) \tau_+^2}{3\hbar^2(3\langle\Omega^4\rangle - 2)} T_c^3$$

strong pair-breaking at $T_c \ll T_{c0}$ for $\langle\Omega\rangle=0$
 T_{c0} – critical temperature in the clean limit

BNC scaling is expected in the limit of strong pair-breaking within BCS theory for d -wave or $s\pm$ SC gap



E. Pushkarov and K. Maki, Eur. Phys. J. B 4, 191 (1998)
L.A. Openov, Phys. Rev. B 69 224516 (2004)
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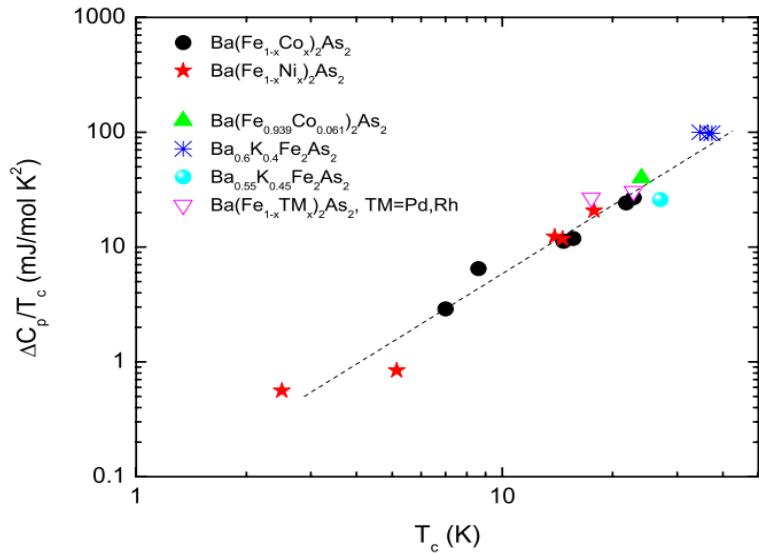
$$\Delta C = C_s - C_n = \frac{16\pi^4 k_B^4 N(0) \tau_+^2}{3\hbar^2(3\langle\Omega^4\rangle - 2)} T_c^3$$

strong pair-breaking when $T_c < 0.1T_{c0}$

$T_{c0} > 400$ K – critical temperature in the clean limit !

BNC scaling is expected for a quantum critical metal undergoing a pairing instability

J. Zaanen, Phys. Rev. B 80, 212502 (2009)



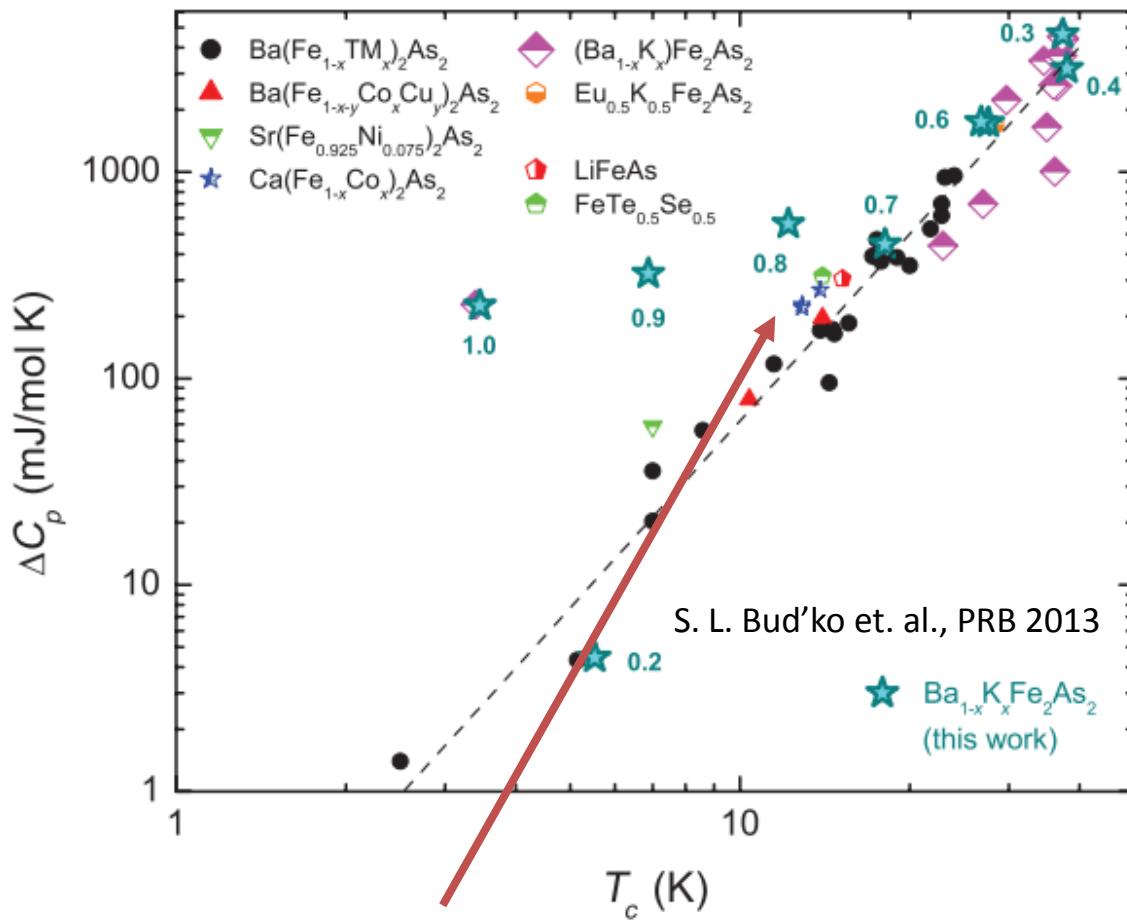
$$C_p = A_{cr} \left(\frac{T}{T_0} \right)^{d/z}$$

$$\Delta C \propto T_c^3 \quad \text{for three dimensional SC}$$

$$\Delta C \propto T_c^2 \quad \text{for two dimensional SC}$$

$z \sim 1$ and d is dimensionality of the space

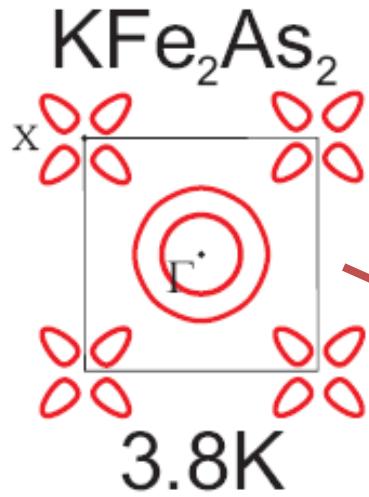
BNC scaling $\Delta C \propto T_c^3$



-deviation from the universal BNC curve for $\text{K}_x\text{Ba}_{1-x}\text{Fe}_2\text{As}_2$ at $x > 0.7$;
-essential changes in superconducting state was expected

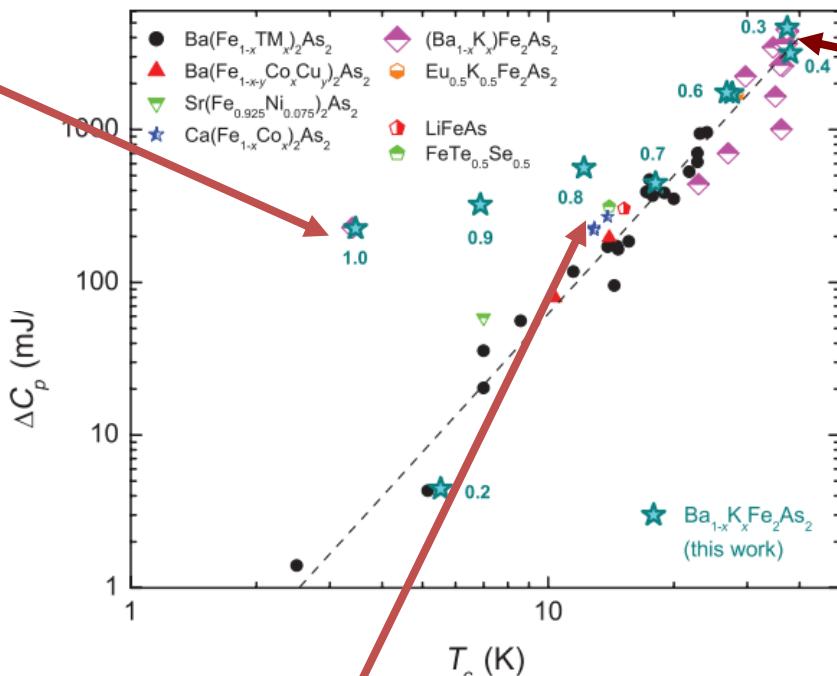
BNC scaling $\Delta C \propto T_c^3$

D. Evtushinsky et al., ARPES

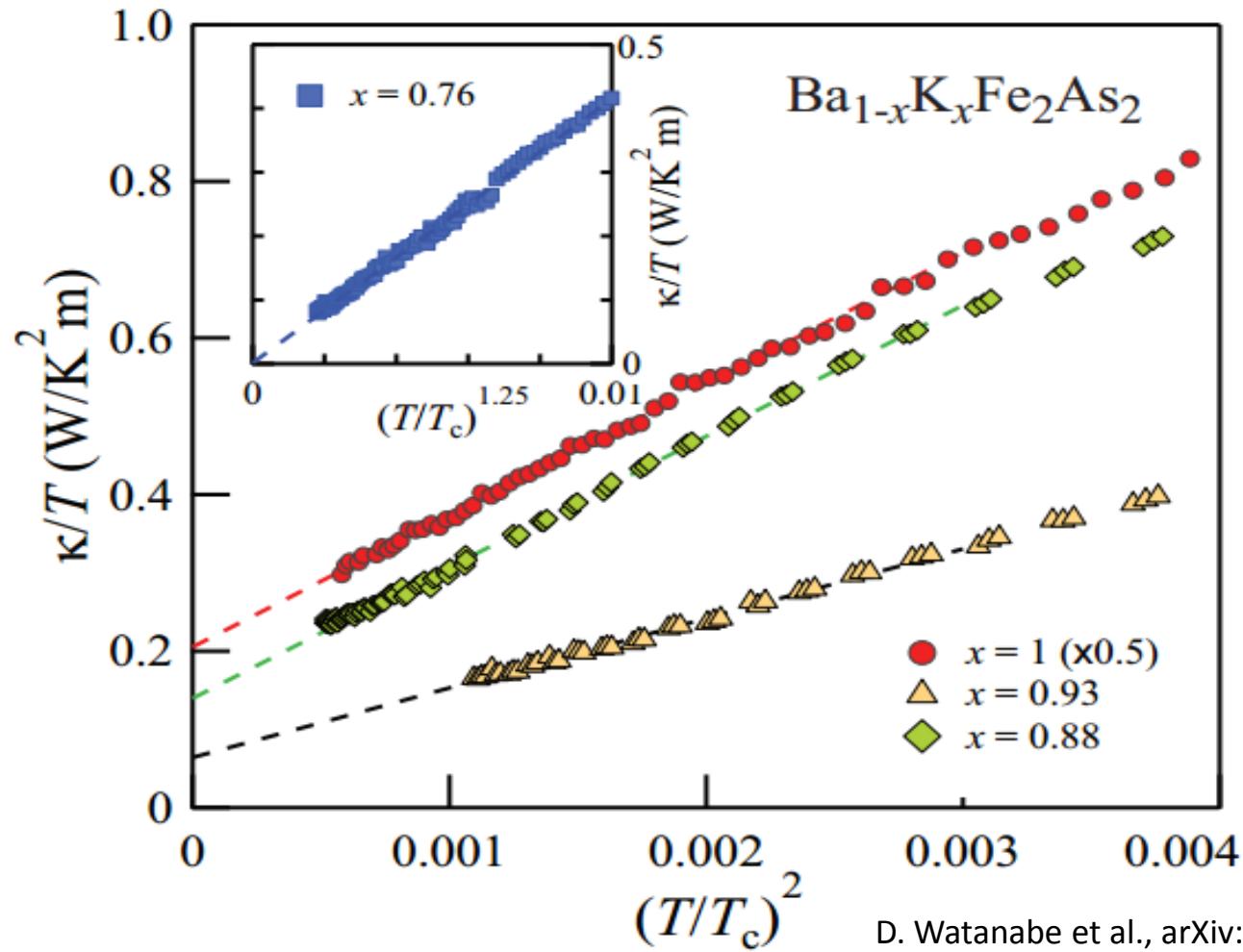


no el pockets
only h pockets
no nesting at $Q=[\pi;\pi]$
the gap symmetry?

S. L. Bud'ko et. al., PRB 2013

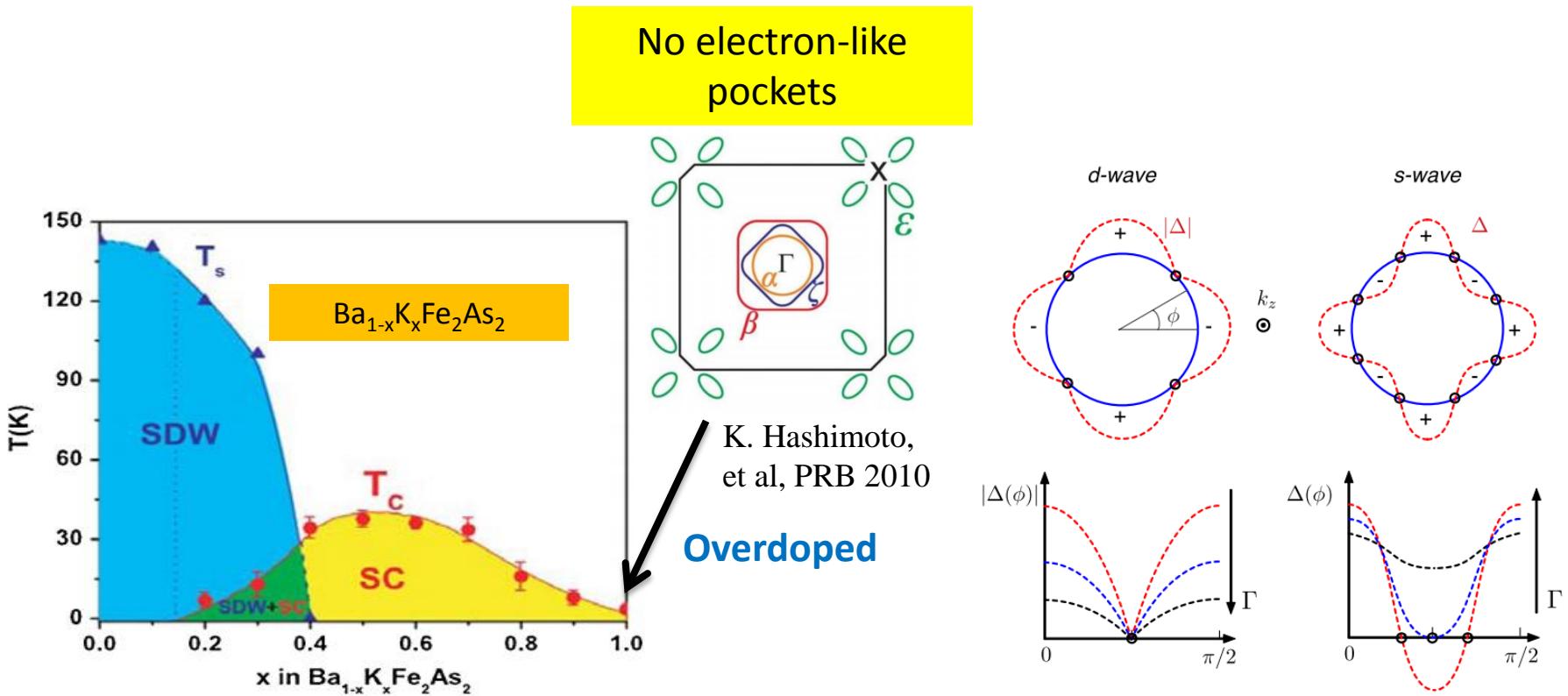


Thermal conductivity



- Residual contribution to thermal conductivity
- nodes in the SC gap of $\text{K}_x\text{Ba}_{1-x}\text{Fe}_2\text{As}_2$ at $x > 0.7$
- Non universal behavior -> s± gap with accidental nodes ?

Possible gap symmetry of KFe₂As₂

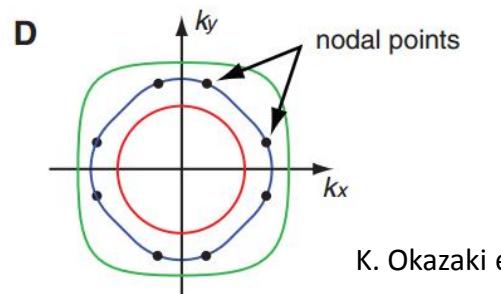
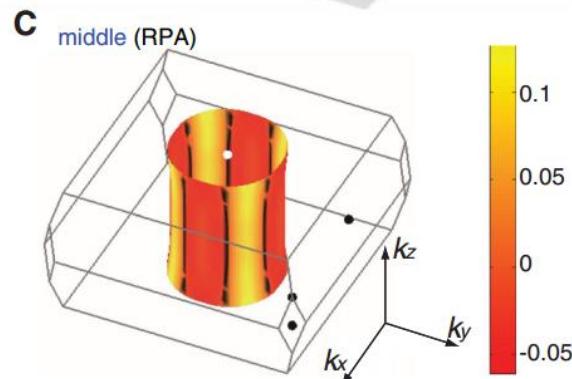
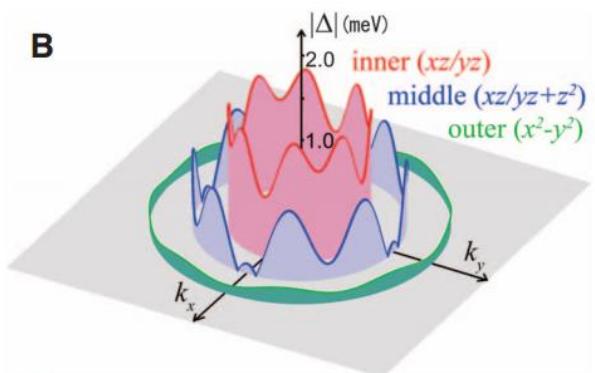


Johrendt *et al.*, (2009), H. Chen *et al.*, 2009

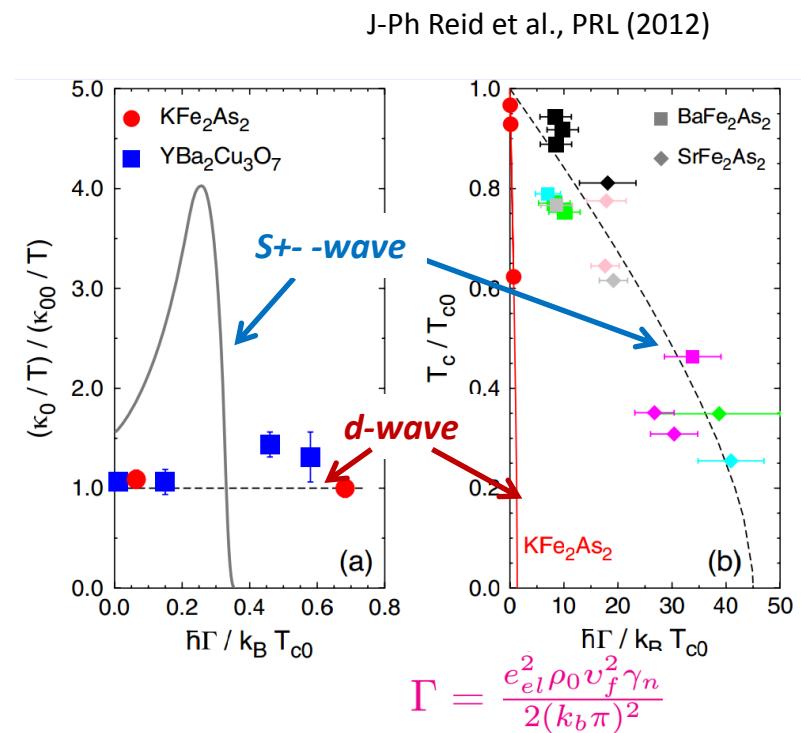
J-Ph Reid et al., Supercond. Sci. Technol. (2012)

$s\pm$ with accidental nodes or d – wave ?

Superconductivity of KFe₂As₂: s₊ accidental nodes or d – wave ?

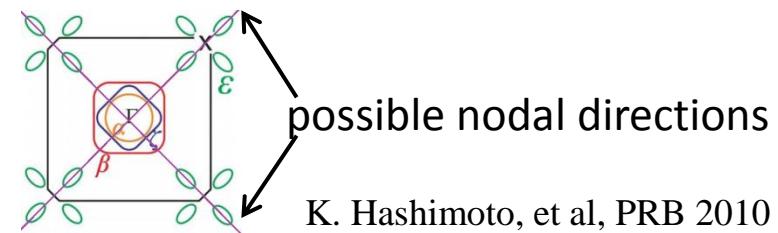


K. Okazaki et al., Science (2012)

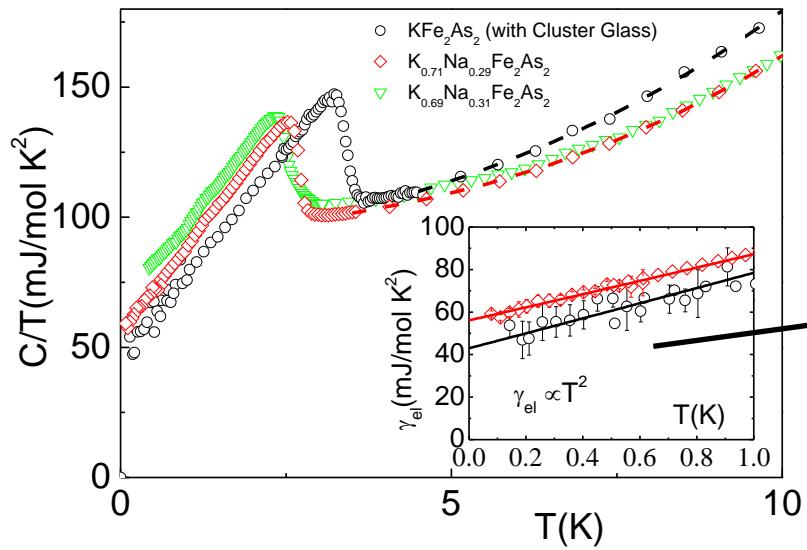


Disorder independent Thermal conductivity
 T_c unusually sensitivity to disorder

$$\Gamma_{cr}/T_{c0} \approx 0.9$$



Disorder independent *line nodes* in the gap of $K_{1-x}Na_xFe_2As_2$

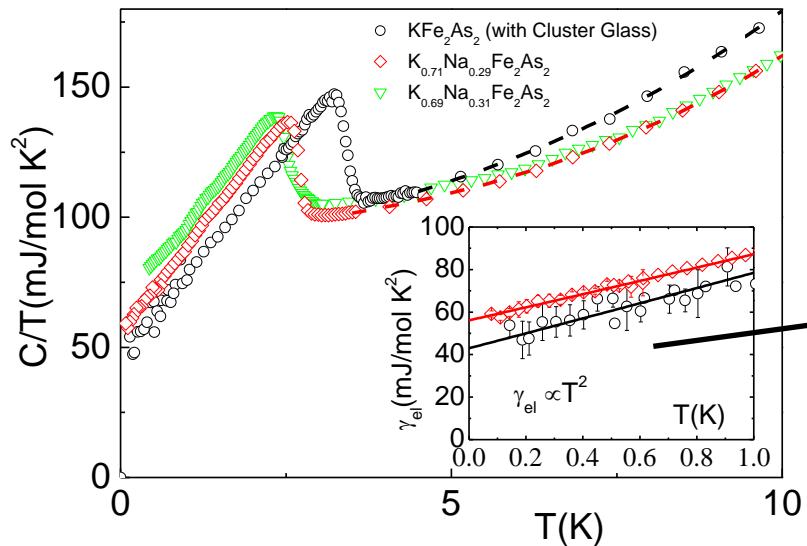


$$\gamma_{el} \propto \alpha_{sc} T^2$$

$$\alpha_{sc}(\text{mJ/mol K}^3) \approx 0.283 \frac{\kappa \gamma_{el}(\text{mJ/mol K}^2)}{\Delta_0(\text{meV})}$$

line nodes in SC gap

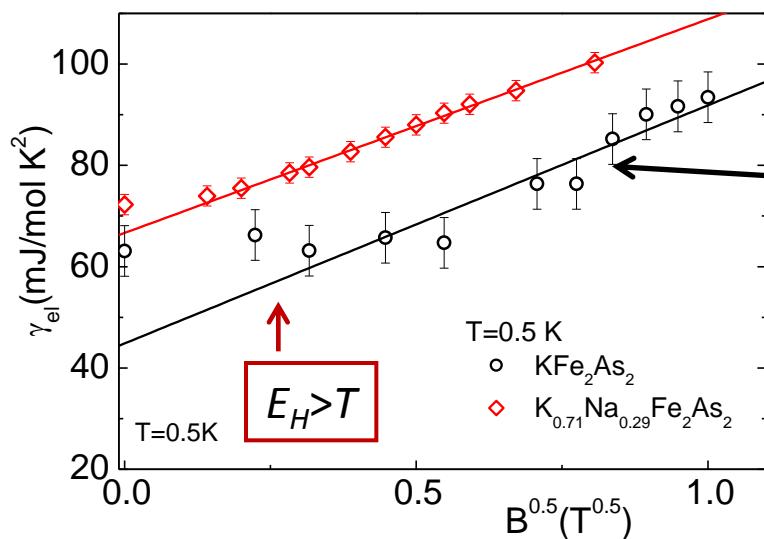
Disorder independent *line nodes* in the gap of $K_{1-x}Na_xFe_2As_2$



$$\gamma_{\text{el}} \propto \alpha_{\text{sc}} T^2$$

$$\alpha_{\text{sc}}(\text{mJ/mol K}^3) \approx 0.283 \frac{\kappa \gamma_{\text{el}}(\text{mJ/mol K}^2)}{\Delta_0(\text{meV})}$$

$B^{0.5}$ dependence of specific heat due to Doppler shift of electrons in magnetic field



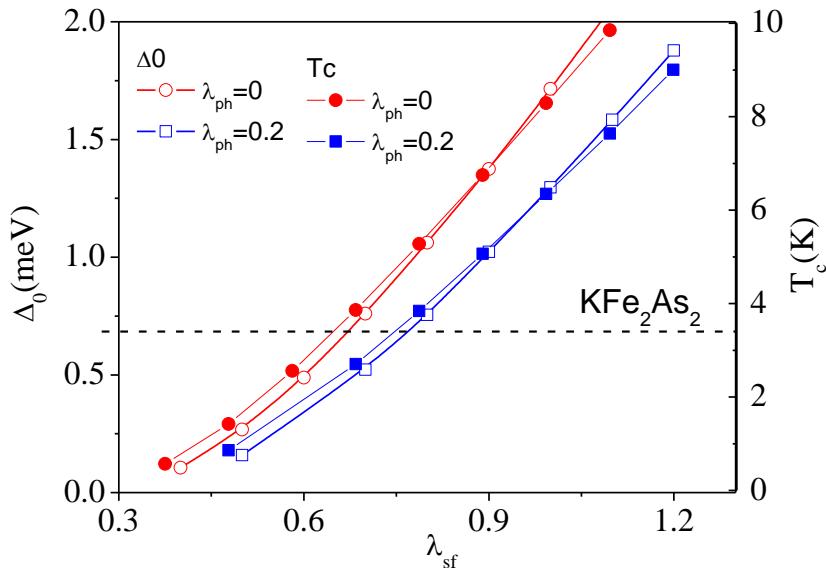
$$C(T,H) \approx \frac{2TE_H}{\pi v_f v_\Delta} \left(\frac{\pi^2}{3} M_1 + \frac{7\pi^4}{15} P(0) \frac{T^2}{E_H^2} \right)$$

$$E_H = \hbar v_F (\pi B / \Phi_0)^{0.5}$$

$$\Delta_0^{\text{exp}} \sim 0.4 - 0.7 \text{ meV}$$

consistent with single-band d-wave

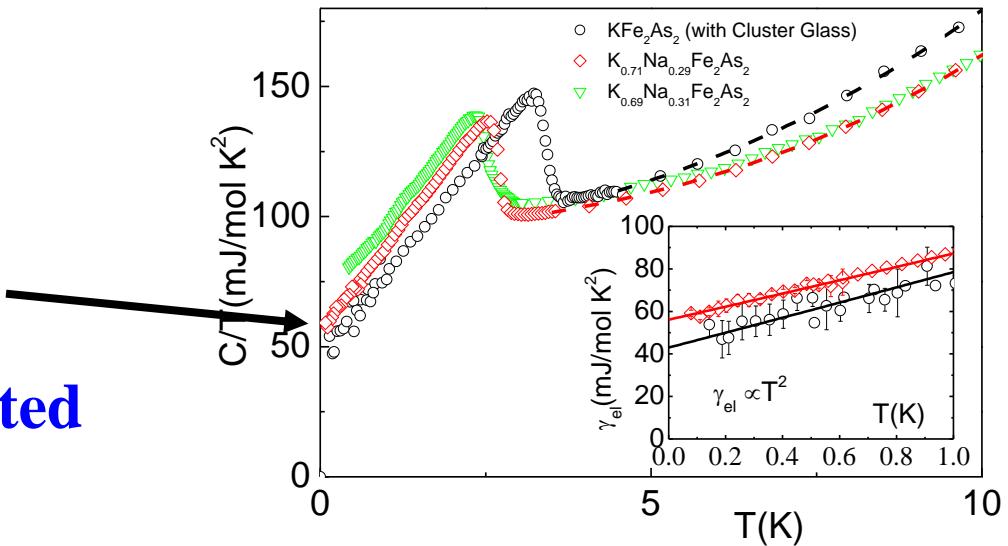
KFe₂As₂ : a two-dimensional effective single-band d-wave superconductor?



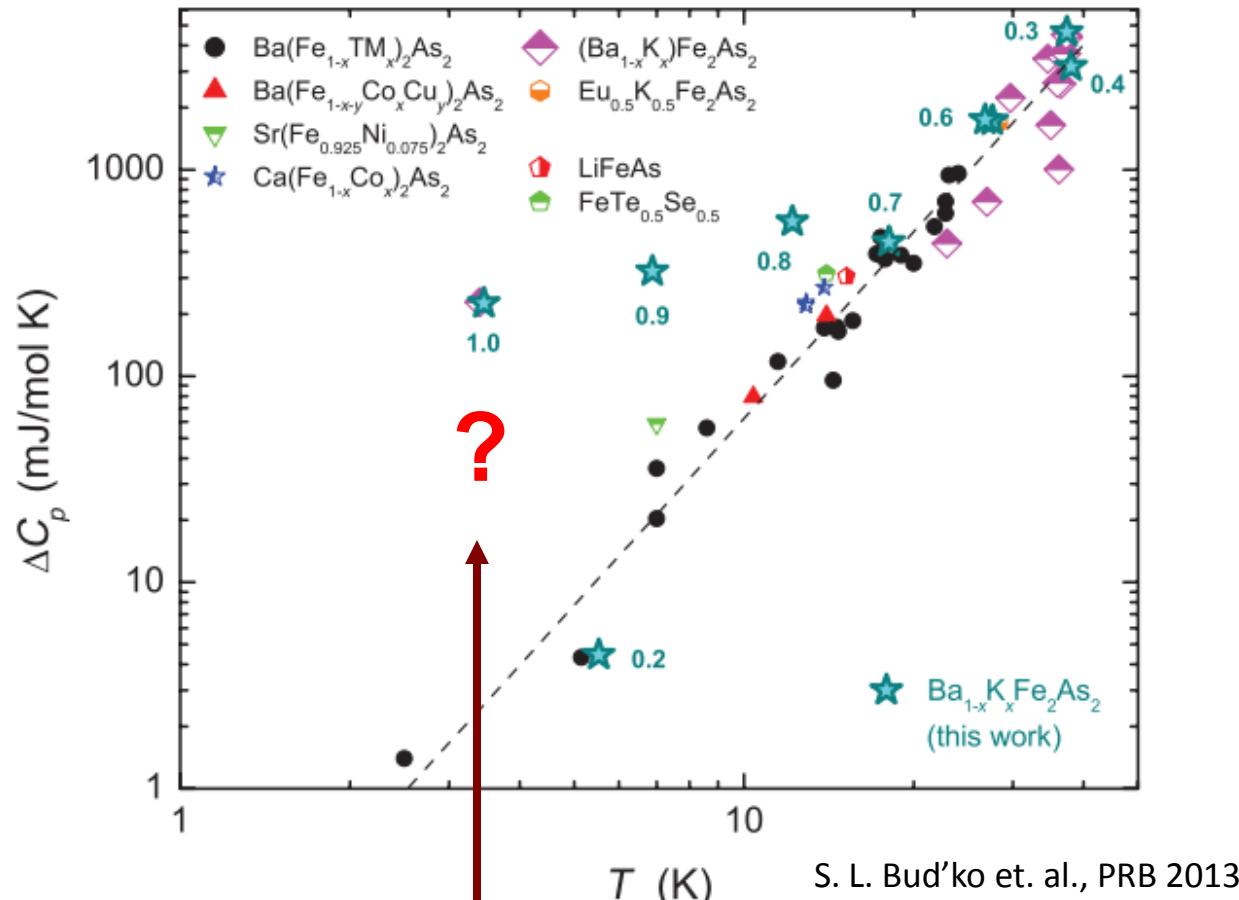
Eliashberg theory for *d*-wave consistent with evaluated gap value:

$$\Delta_0^{exp} \sim 0.4 - 0.7 \text{ meV}$$

Unusually larger residual electronic specific heat
Unpaired electrons are related to the pair-breaking due to disorder?

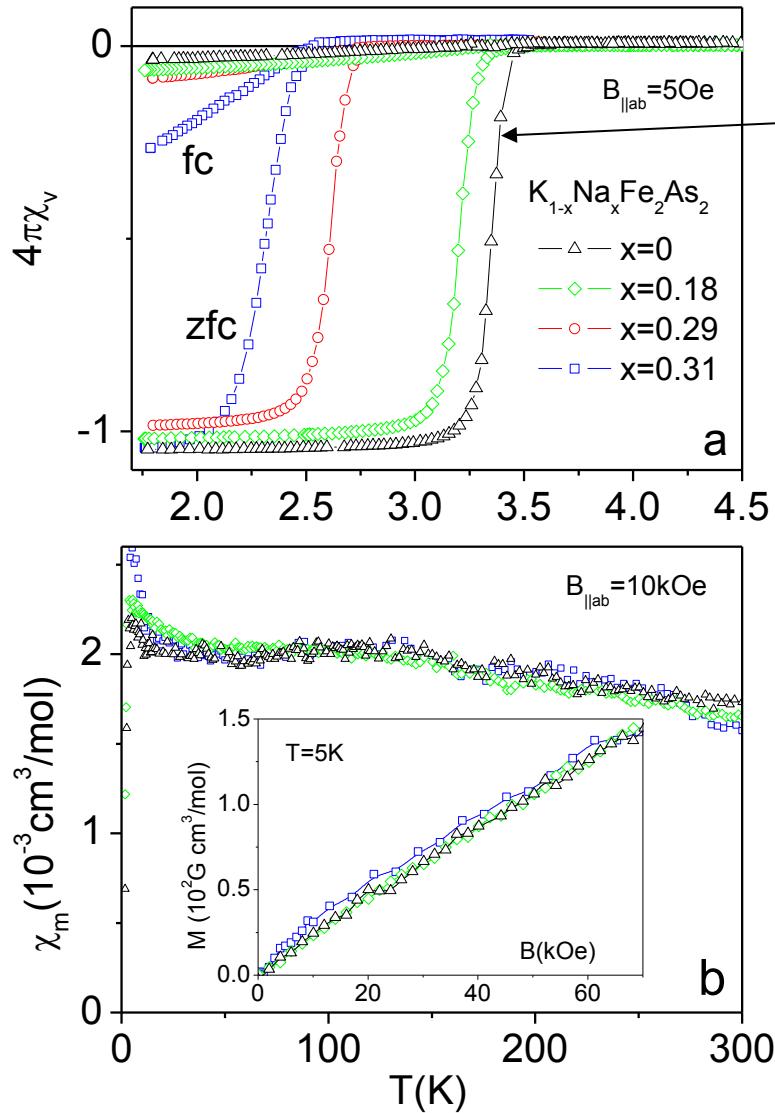


Superconducting specific heat jump ΔC for $K_{1-x}Na_xFe_2As_2$



We fix the hole doping and vary amount of disorder induced by Na doping

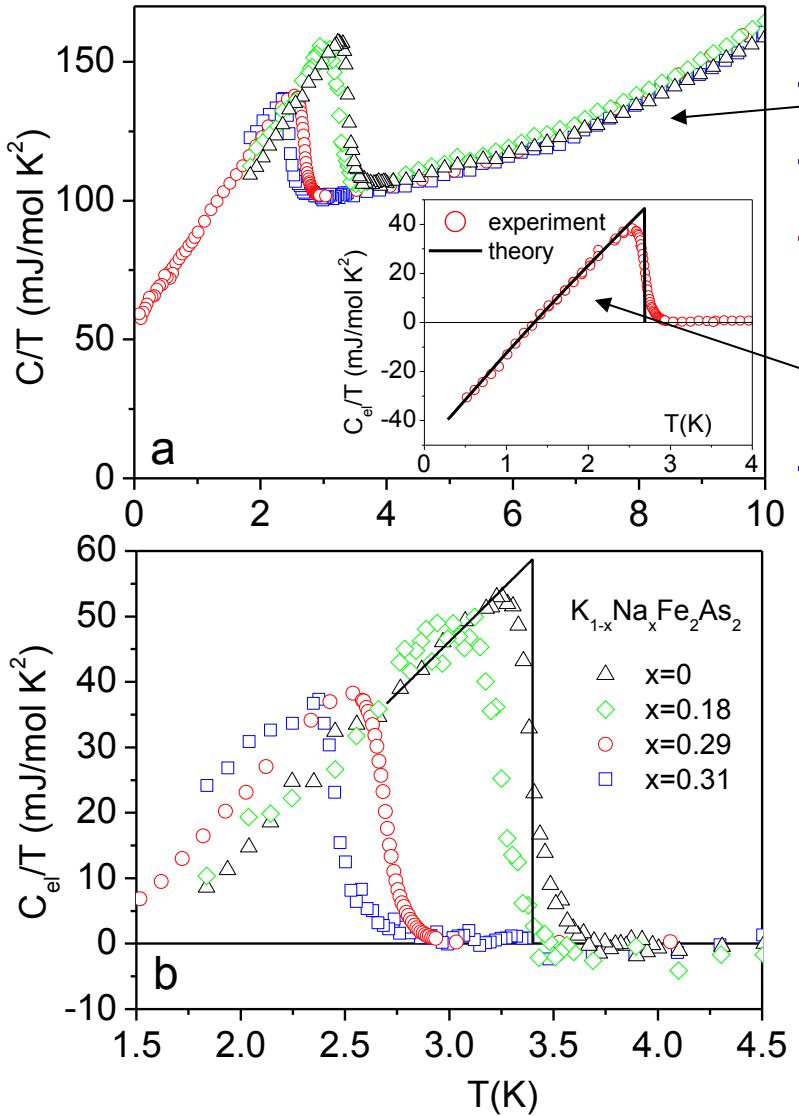
Magnetic susceptibility $K_{1-x}Na_xFe_2As$



nearly parallel shift of the zfc
curve with Na doping ->
homogenous Na distribution

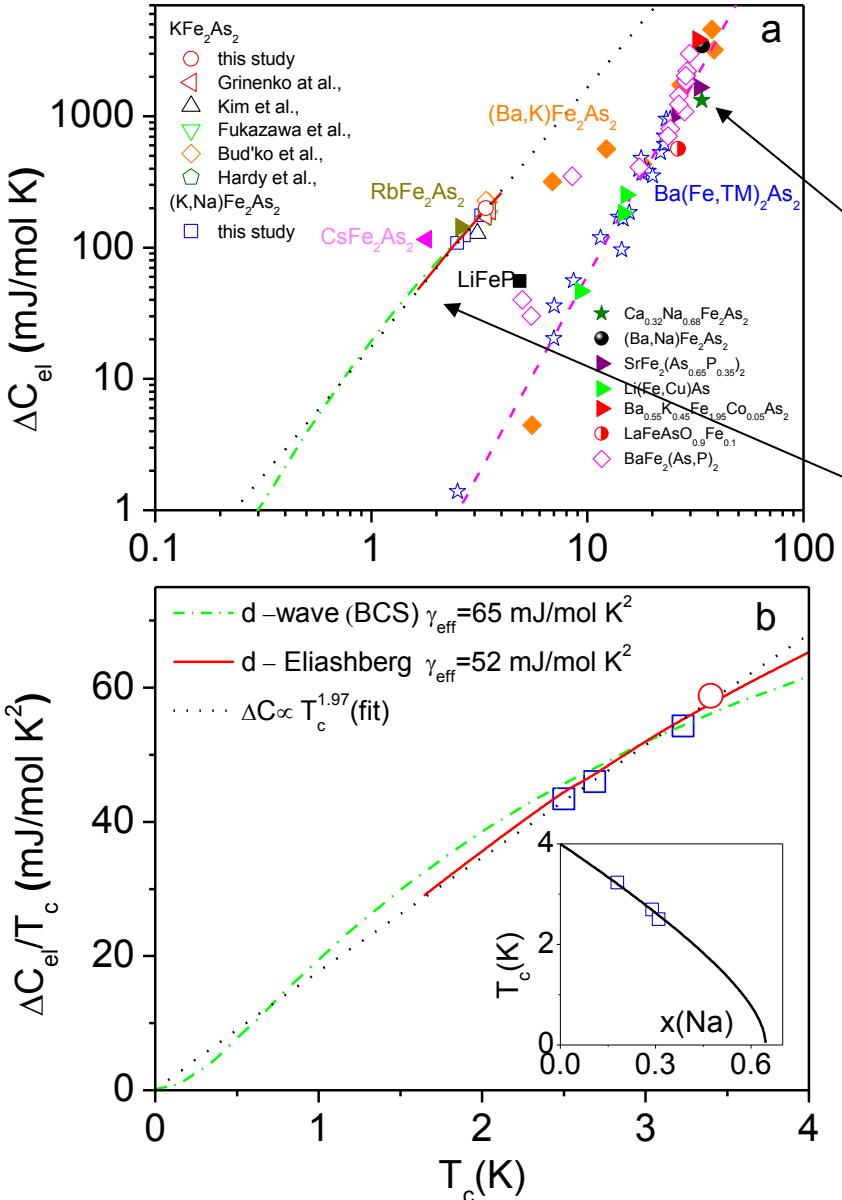
nearly T -independent below 100K
-> Pauli susceptibility;
independent on Na doping
-> Na doping does not change
density of state;
Na is nonmagnetic impurity

Specific heat of $K_{1-x}Na_xFe_2As$



- independent on Na doping;
 - does not change the correlation effect
 - good agreement between experiment and Eliashberg theory for single-band *d*-wave with nonmagnetic disorder;
 - unusual T^2 dependence cannot be explained by nodless s-wave gap
-
- Monotonic reduction of SH jump height \rightarrow pair breaking effect

Specific heat jump at T_c



- two regions can be identified:

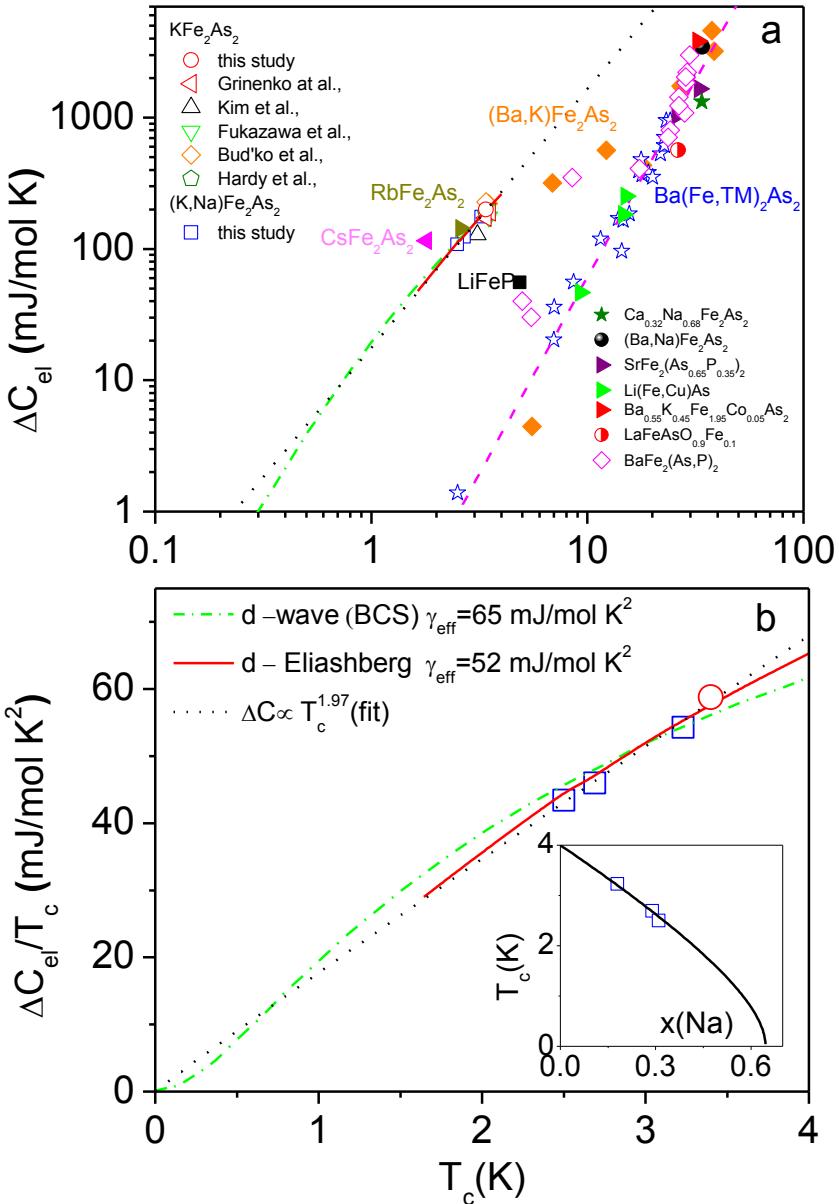
- i) BNC scaling $\Delta C \propto T_c^3$ for the most of iron-pnictides

- ii) new scaling for $K_{1-x}Na_xFe_2As_2$

$$\Delta C \propto T_c^2$$

**Consistent with d-wave SC gap
but with reduced γ_{el} ;
Residual specific heat cannot be
explained by pair-breaking due to
disorder**

Open questions

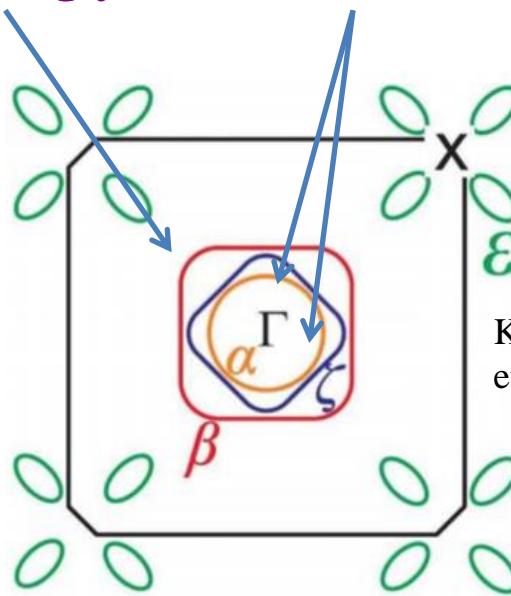


- Part of quasiparticles does not contribute to SH jump at T_c

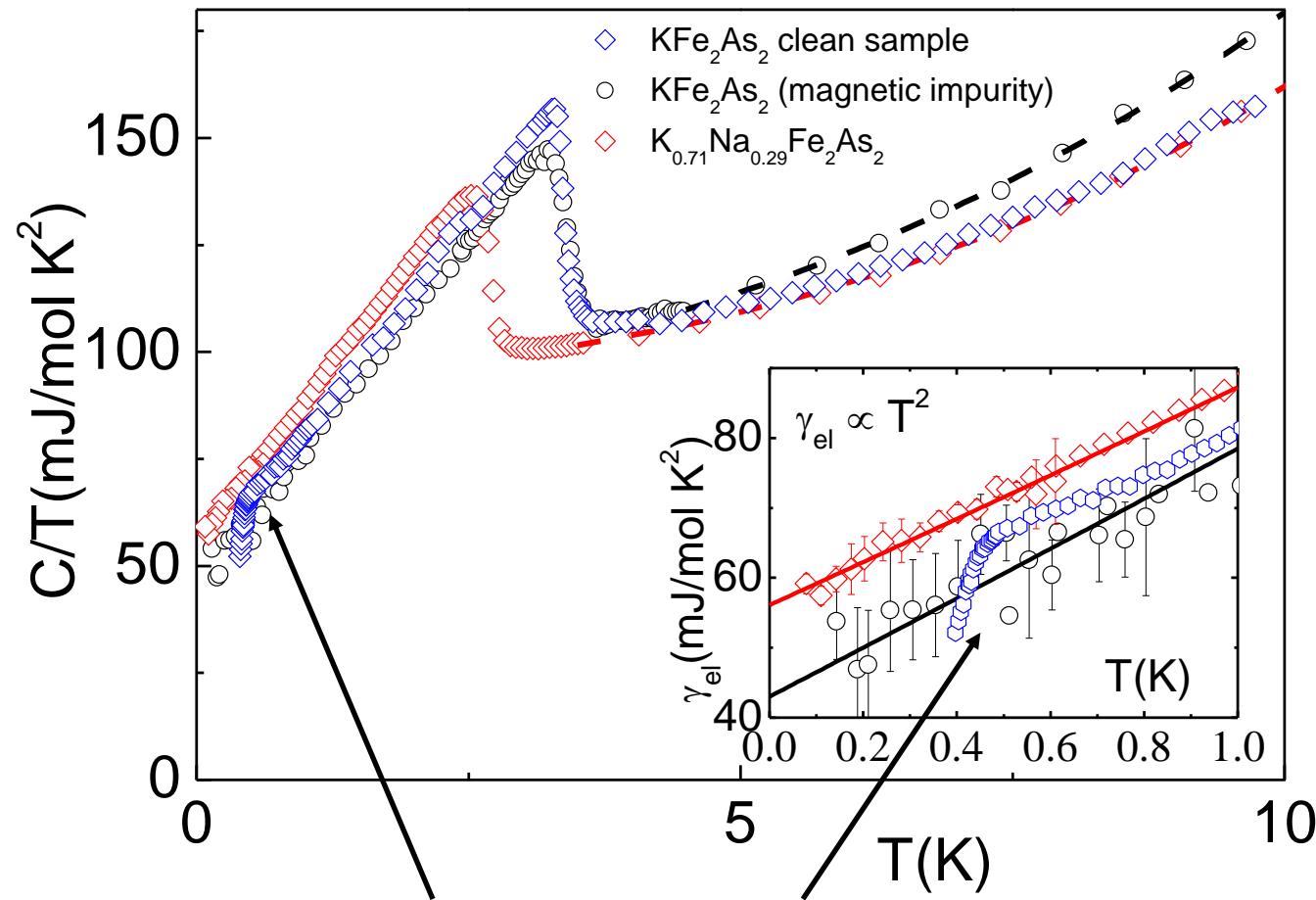
$$\gamma_n \sim 100 \text{ mJ/mol K}^2$$

$$\gamma_{\text{eff}} \sim 60 \text{ mJ/mol K}^2$$

- What bands are superconducting strongly or less correlated?



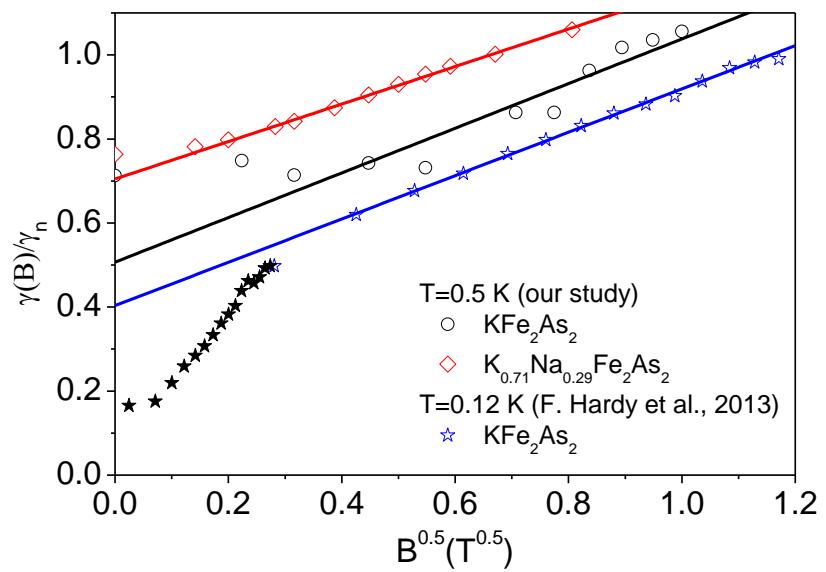
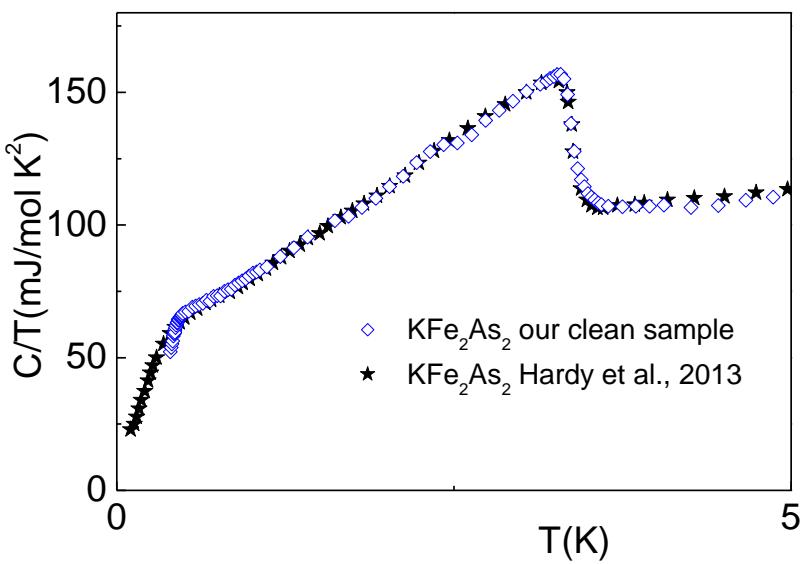
Possible nodal *multi-band* superconductivity of KFe_2As_2



anomaly at $T \sim 0.5$ K in clean sample

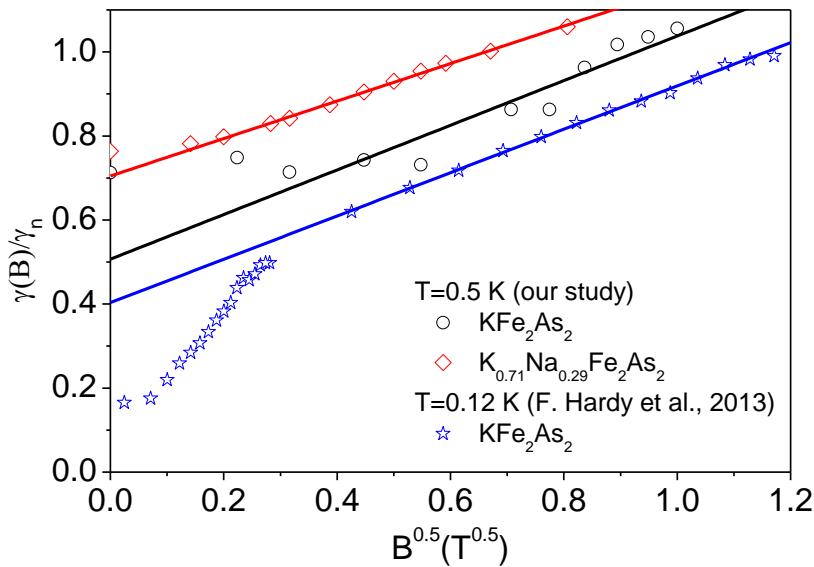
small gaps suppressed by weak disorder;
 T_c is nearly unaffected by magnetic impurity

Possible nodal *multi-band* superconductivity of KFe_2As_2



Consistent with data from F. Hardy et al., arXiv:1309.5654v1;
Low-T anomaly interpreted as small gaps

Possible nodal *multi-band* superconductivity of KFe₂As₂



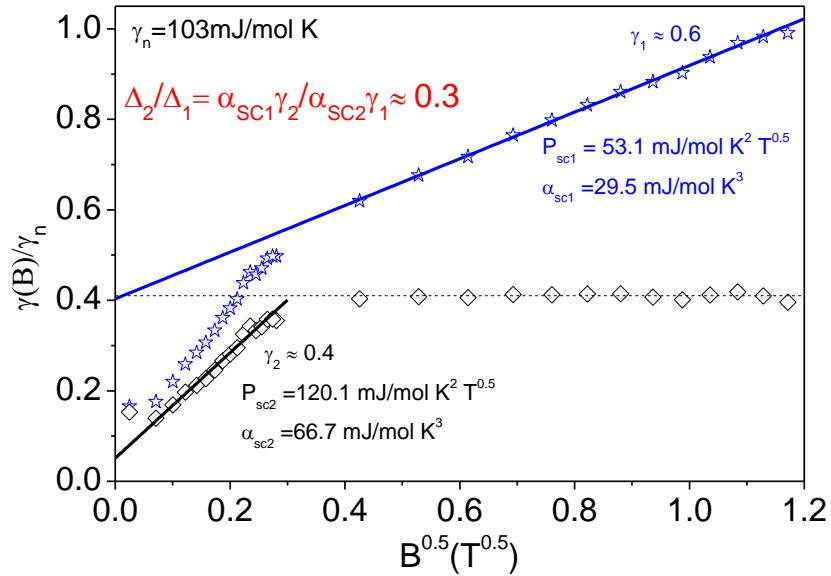
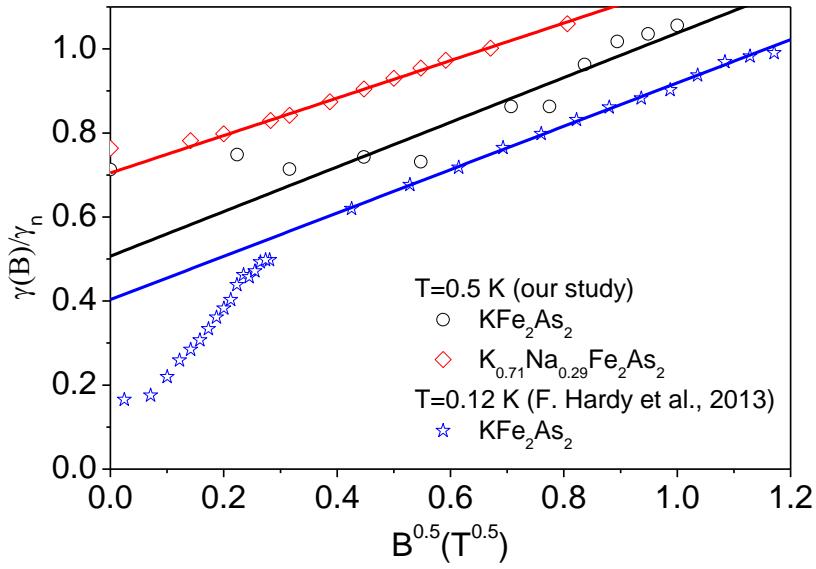
$B^{0.5}$ dependence of specific heat due to Doppler shift of electrons
in magnetic field

$$C(T,H) \approx \frac{2TE_H}{\pi v_f v_\Delta} \left(\frac{\pi^2}{3} M_1 + \frac{7\pi^4}{15} P(0) \frac{T^2}{E_H^2} \right)$$

$$E_H = \hbar v_F (\pi B / \Phi_0)^{0.5}$$

Possible nodal *multi-band* superconductivity of KFe₂As₂

F. Hardy et al., arXiv:1309.5654v1



$B^{0.5}$ dependence of specific heat due to Doppler shift of electrons
in magnetic field

$$\frac{\Delta_1}{\Delta_2} = \frac{\alpha_1 \gamma_2}{\alpha_2 \gamma_1} \approx 0.3$$

$$C(T,H) \approx \frac{2TE_H}{\pi v_f v_\Delta} \left(\frac{\pi^2}{3} M_1 + \frac{7\pi^4}{15} P(0) \frac{T^2}{E_H^2} \right)$$

$$E_H = \hbar v_F (\pi B / \Phi_0)^{0.5}$$

$$\alpha_{sc}(\text{mJ/mol K}^3) \approx 0.283 \frac{\kappa \gamma_{el}(\text{mJ/mol K}^2)}{\Delta_0(\text{meV})}$$

consistent with multi-band nodal superconductivity (*d*-wave ?)

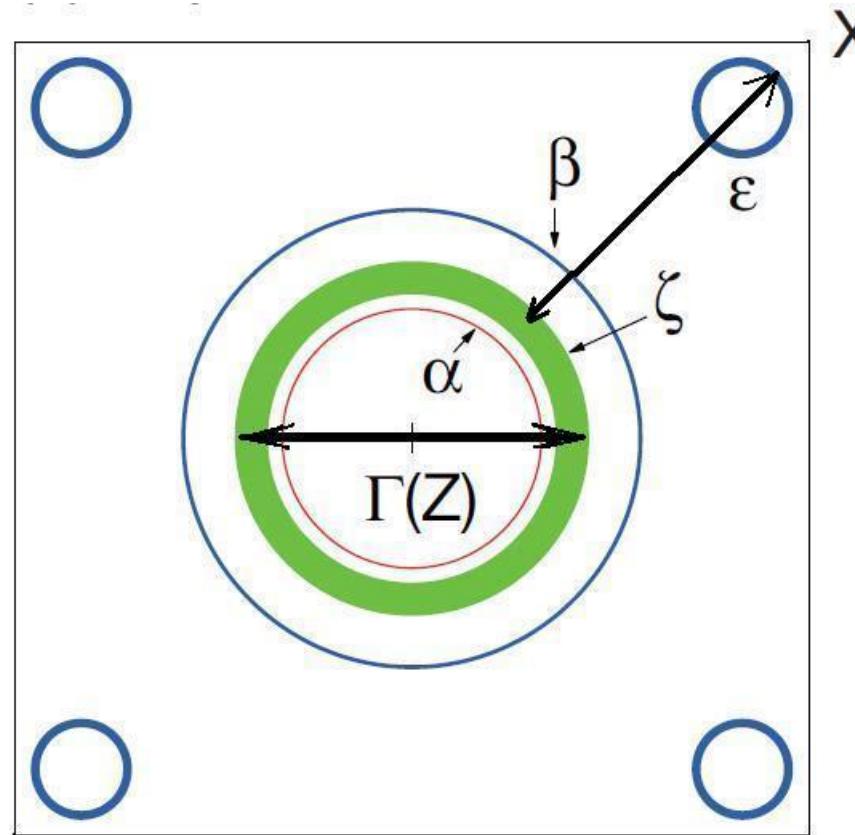
Conclusion

Disorder under control:

the powerful tool to investigate physical properties of iron-pnictides

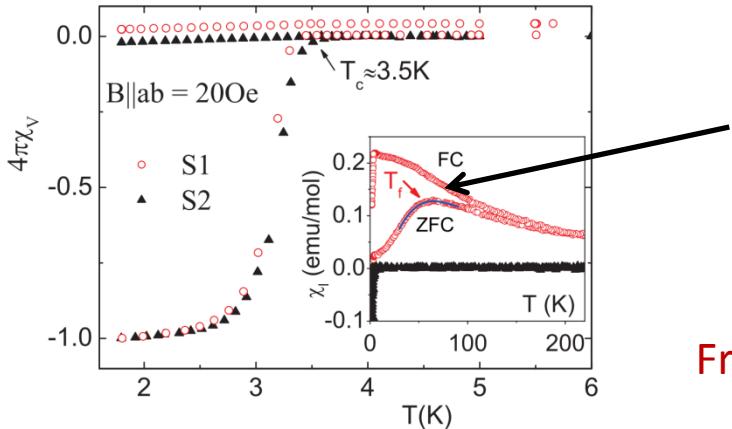
- Disorder suppresses small gaps and results in the large residual electronic specific heat;
- Nodes in the large superconducting gap stable against disorder: evidence for *d*-wave;
- Conventional behavior of $\Delta C_{\text{el}} \propto T_c^2$ for unconventional Fe-pnictides, also consistent with *d*-wave superconductivity;
- Nodal multi-band superconductivity, in clean samples;

Thank you for attention!



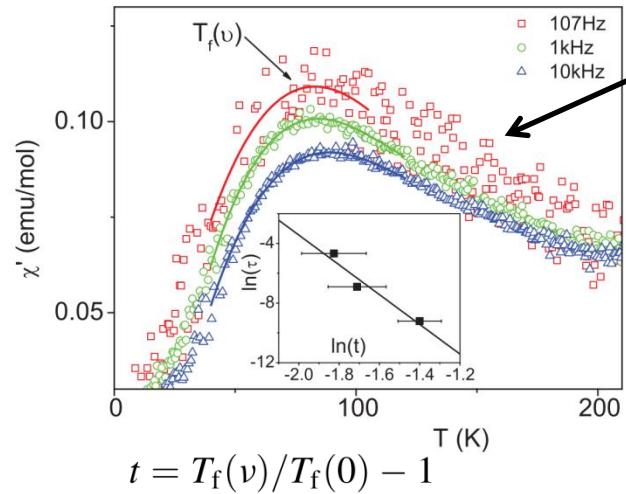
Critical behavior I: susceptibility

DC susceptibility



Hysteresis in the normal state
between zero field cooled
and field cooled curves
 T_f - freezing temperature

AC susceptibility



Frequency shift of the maximum in AC susceptibility
shows conventional power-law divergence
of critical slowing down

$$\tau = \tau_0 \left[\frac{T_f(v)}{T_f(0)} - 1 \right]^{-z\nu'}$$

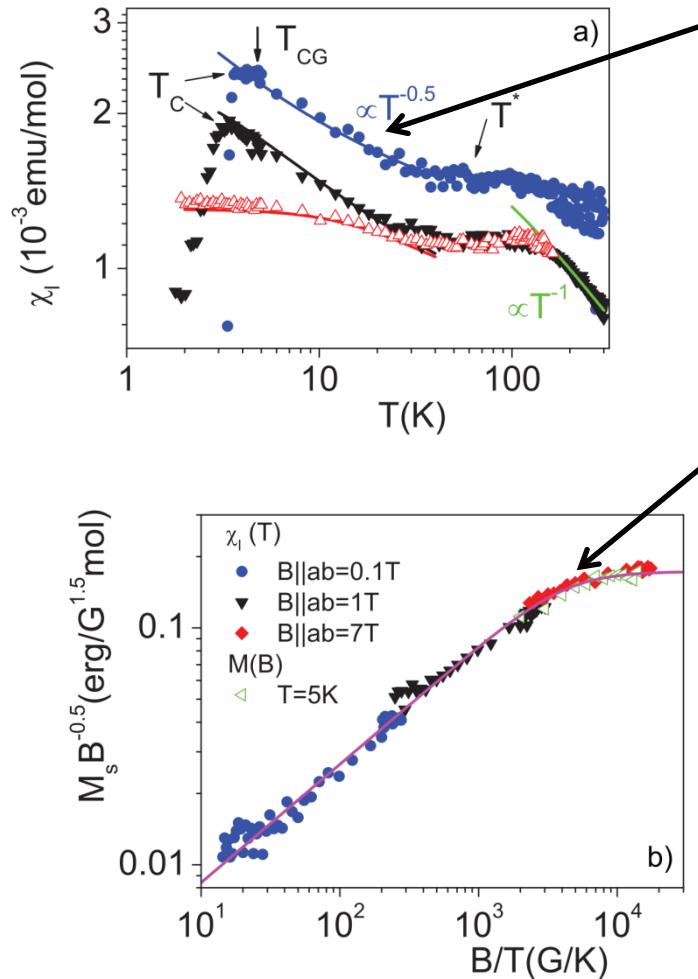
$z\nu' = 10$ the dynamic critical exponent
 $\tau_0 = 6.9 \times 10^{-11} \text{ s}$ relaxation time of a single spin flip



Cluster Glass phase

Non – universal critical behavior

DC susceptibility



Power law behavior at low temperatures

Scaling with a non-universal exponent $\lambda_G = 0.5$
and effective magnetic moment $\mu \sim 3.5 \mu_B$

$$M_s(T, B) = B^{1-\lambda_G} Y\left(\frac{\mu B}{k_b T}\right)$$

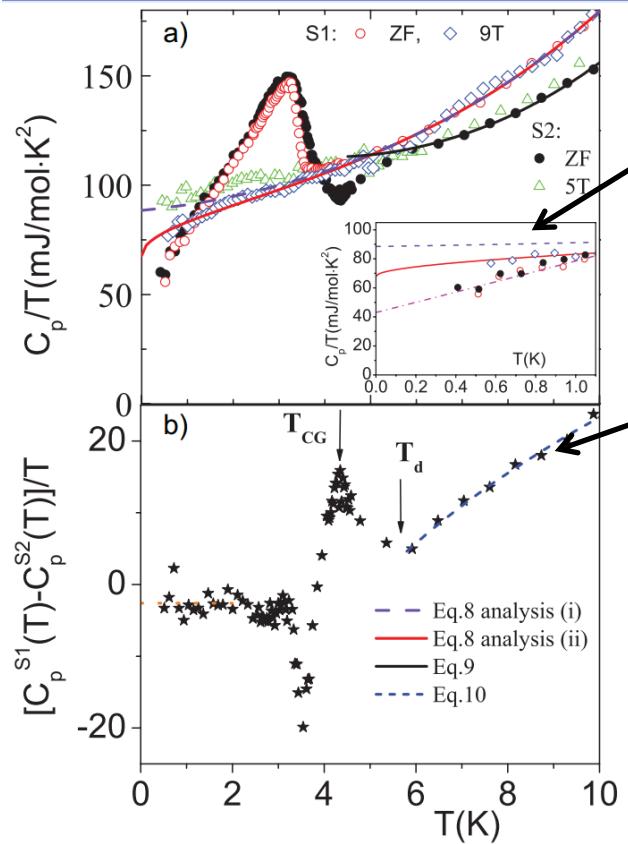
$$Y(z) = A' / (1 + z^{-2})^{\lambda_G/2}$$



Griffiths phase - like behavior

Critical behavior II: specific heat

V. Grinenko et al., Phys. Status Solidi B (2013)



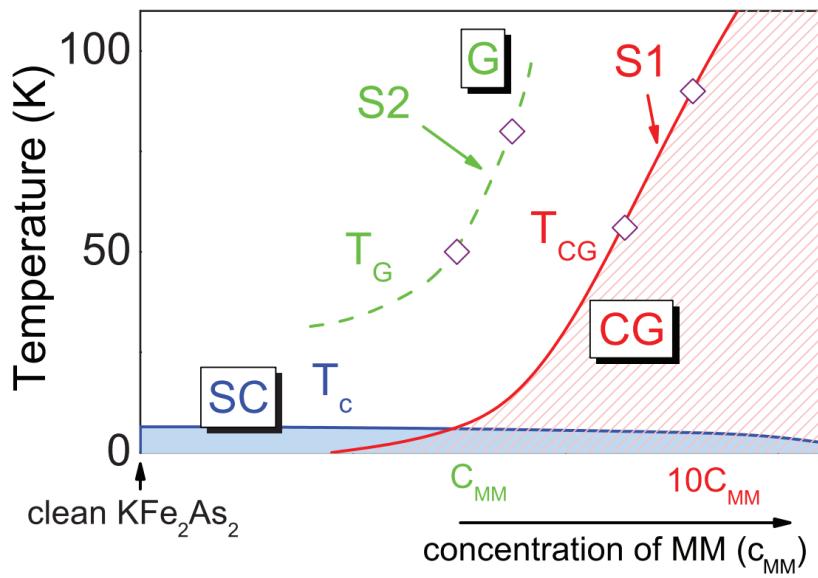
SC – superconductivity
G – Griffiths phase
CG – Cluster glass phase

At low-T: $C_{CG} \approx \gamma_{CG} T + \varepsilon_{CG2} T^2$

The same the non-universal exponent $\lambda_G = 0.5$ in specific heat

$$[C_p^{S1}(T) - C_p^{S2}(T)]/T = C_{CG}/T - \gamma_G T^{\lambda_G - 1}$$

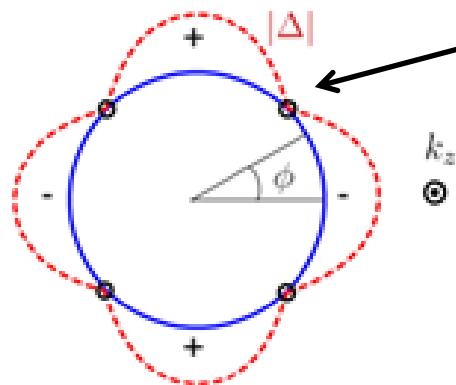
Schematic phase diagram



Specific heat of d - wave SC

The quasiparticle excitation spectrum at low-T

$$\Delta_{\mathbf{k}} = \Delta_0 \cos 2\theta_{\mathbf{k}}$$



$$E_k = \sqrt{v_F^2 k_{\perp}^2 + v_{\Delta}^2 k_{\parallel}^2}$$

contribution from the parts of the Fermi surface
in the vicinity of the nodes

$$v_{\Delta} \approx \partial \Delta / \hbar \partial k$$

$$\partial \Delta / \partial k = \partial \Delta / \partial \theta \frac{1}{k_f}$$

(DOS) linear in-energy

$$N_{SC}(E) = \sum_i \frac{E}{\pi \hbar v_f^i \partial \Delta^i / \partial k} \approx \frac{E}{\partial \Delta / \partial \theta} \sum_i \varkappa^i N^i(\varepsilon_f)$$

At T-> 0 electronic specific heat:

$$C_{SC} \propto \alpha_{sc} T^2$$