

# *Thermodynamic properties of Fe-based superconductors*

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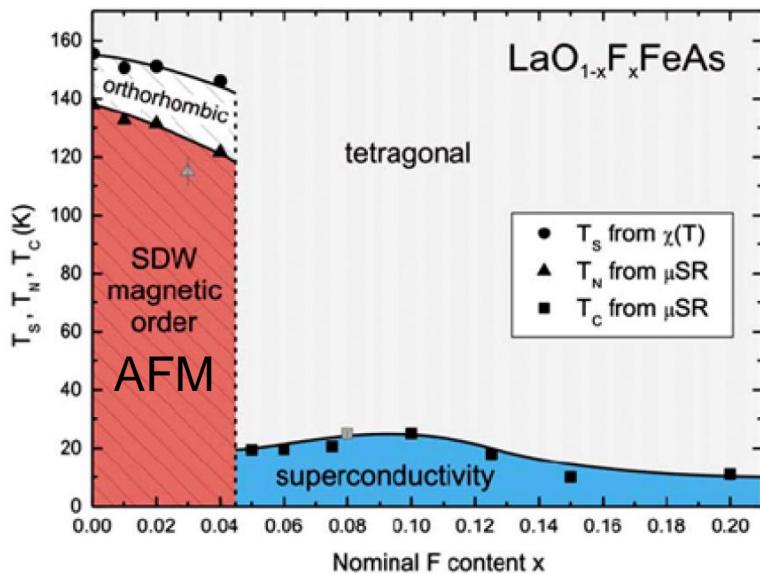
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G. Kotliar

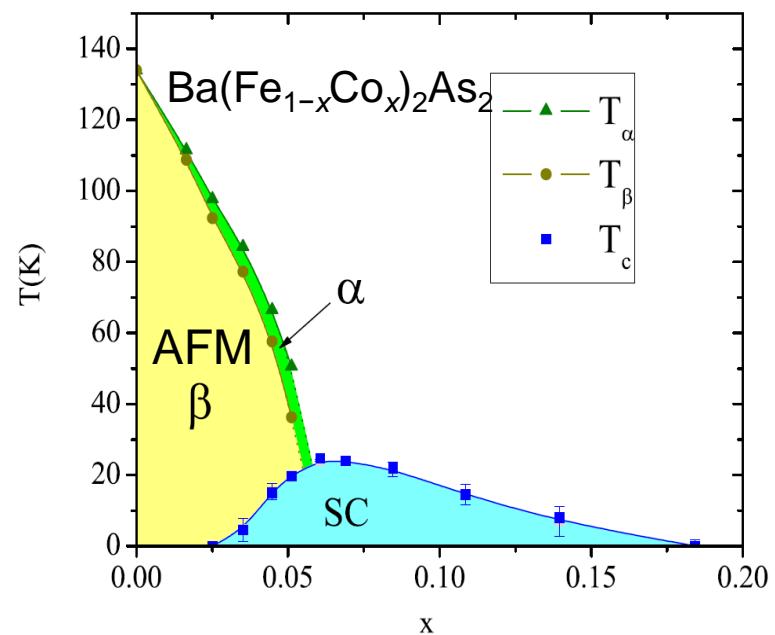
*Rutgers University*

# Phase diagrams

H. Luetkens et al., arXiv:0806.3533



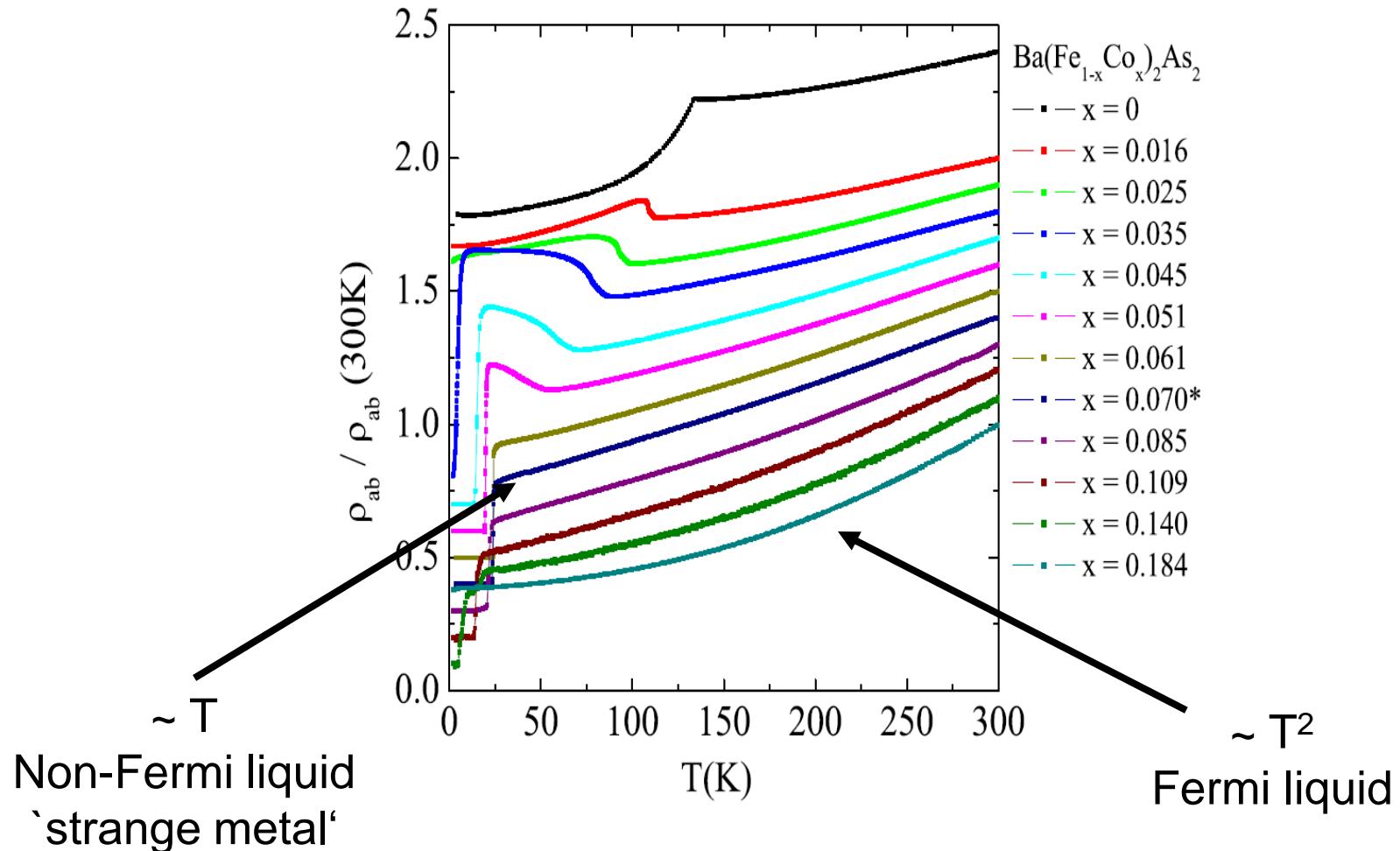
Chu et al. PRB79, 014506 (2009)



- superconductivity arises near a magnetic instability
- similar phase diagrams for other unconventional superconductors  
e.g. cuprates, heavy fermions, organics, ....
- **questions:**
  - Is there a magnetic quantum critical point (QCP)?
  - Is the pairing due to the magnetic fluctuations around the QCP?

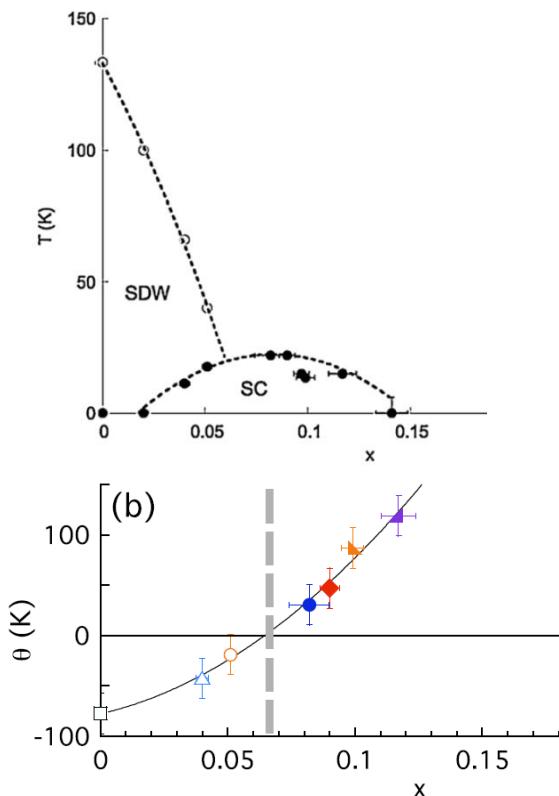
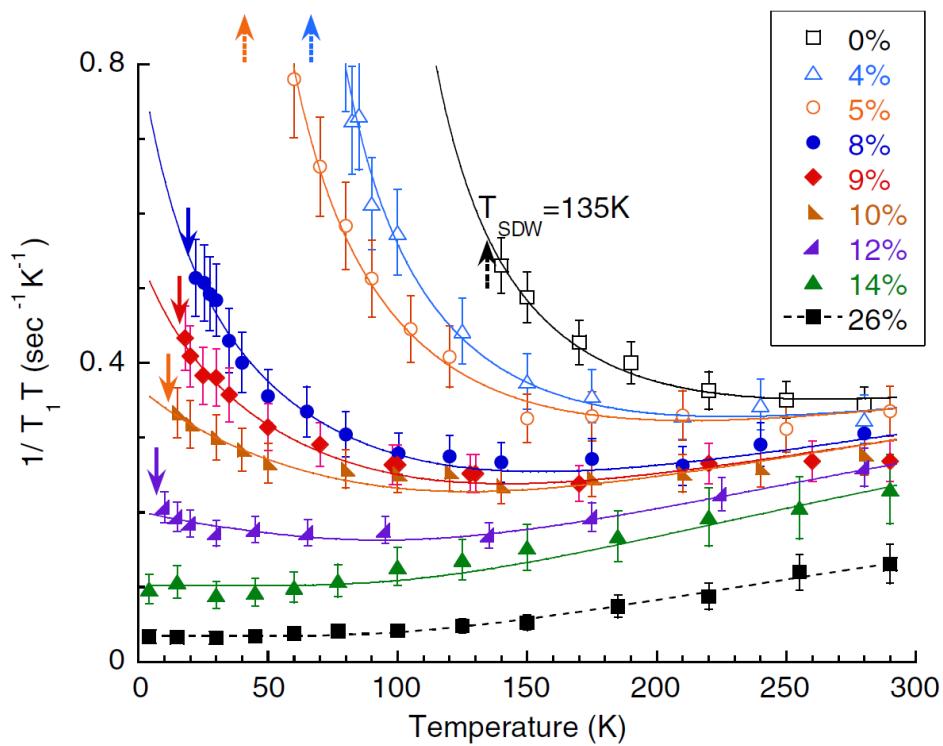
# Resistivity of $\text{Ba}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$

Chu et al. PRB79, 014506 (2009)



# NMR: AFM QCP from spin fluctuations in Co-Ba122

Ning et al. PRL 2010



- Spin-lattice relaxation rate diverges at  $-\theta$  (Curie-Weiss law):  $\frac{1}{T_1T} = \frac{C}{T + \theta}$
- $\theta$  crosses zero smoothly at the critical concentration

# Thermodynamics

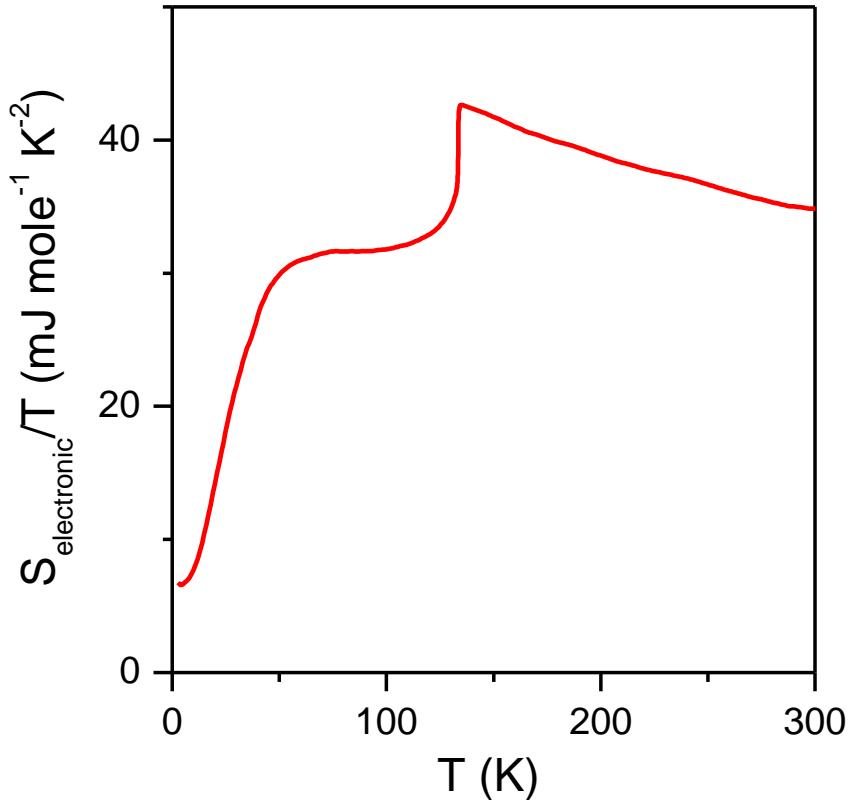
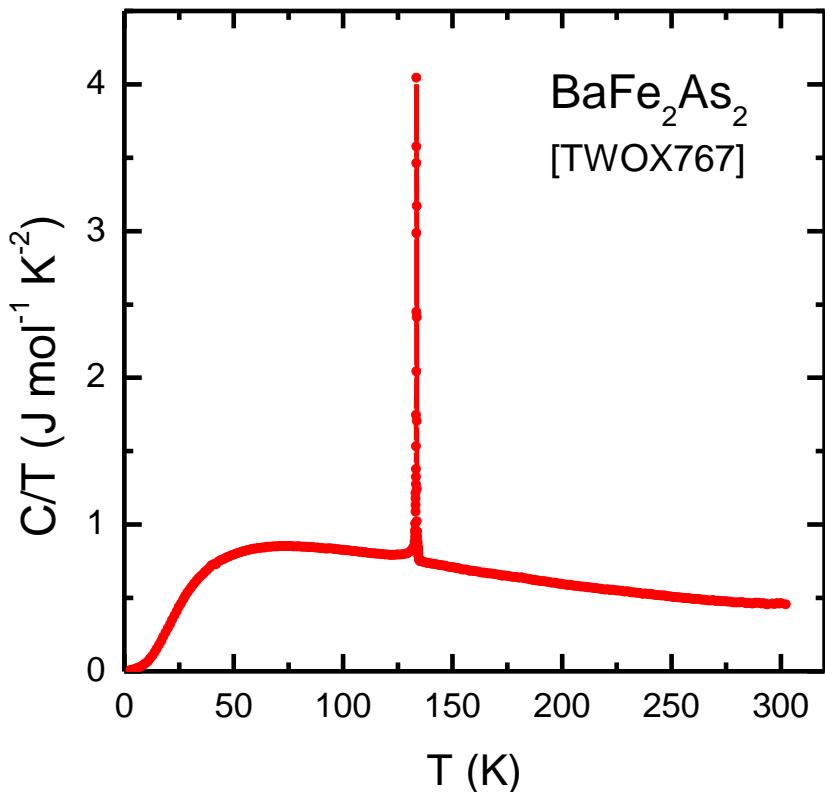
- **electronic heat capacity**
  - entropy, phase transitions, superconducting gaps, fluctuations,...
  - **QCP** - diverging effective mass?
- **electronic thermal expansion**
  - pressure dependence of entropy
  - **QCP** - diverging Grüneisen parameter?  
sign change of Grüneisen parameter?
- **This talk:**
  - Co-Ba122 - quantum critical behavior?
  - shear modulus (nematicity) - compare Co- and K-doping
  - $KFe_2As_2$  - most strongly correlated Fe-based material?

# Co-doped Ba122

specific heat  
and  
thermal expansion

- CM et al. Phys. Rev. Lett. 108, 177004 (2012)
- F. Hardy, et al. Phys. Rev. B 81, 060501 (2010)
- Frédéric Hardy, et al., Phys. Rev. Lett. 102, 187004 (2009)

# Specific heat of Ba122



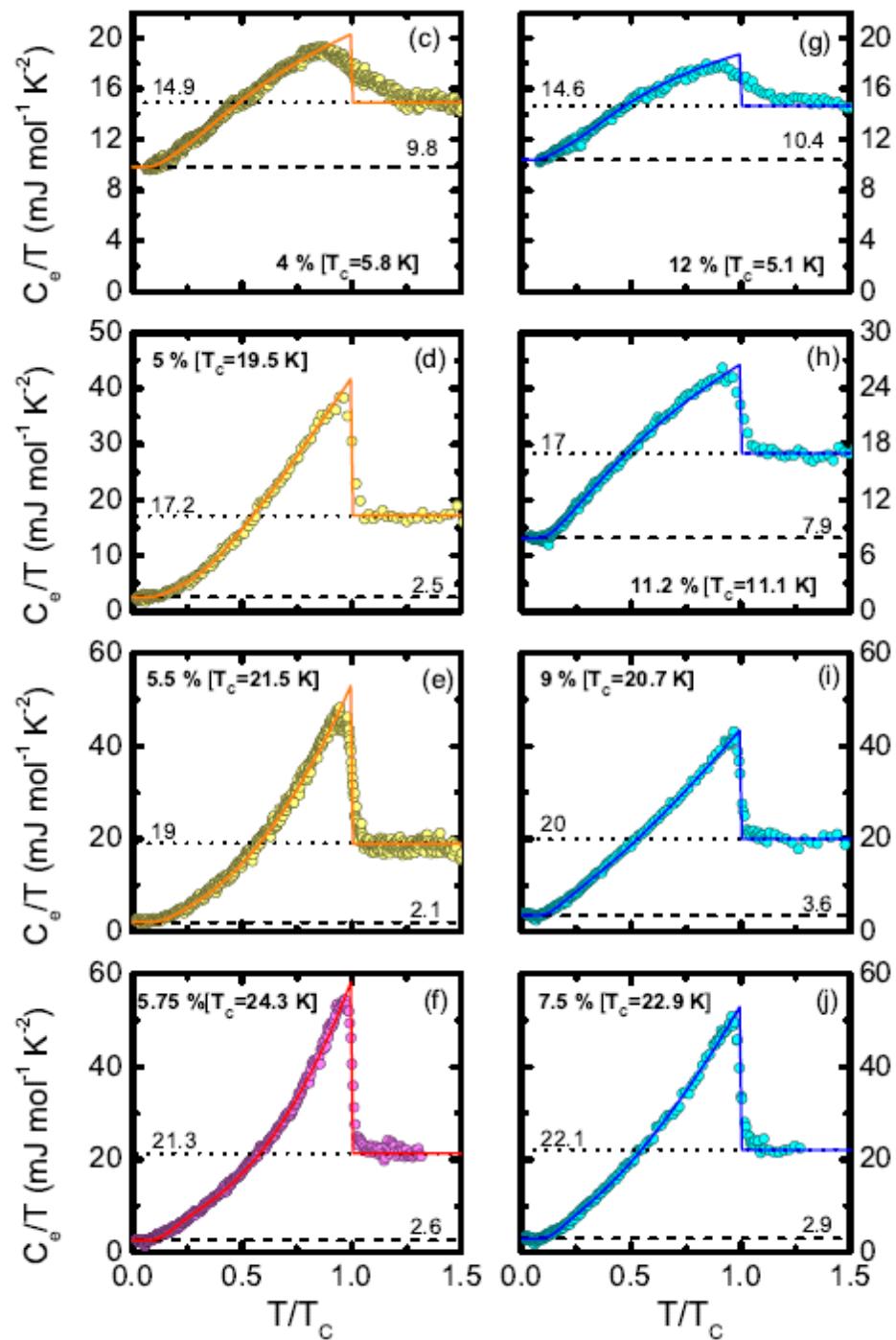
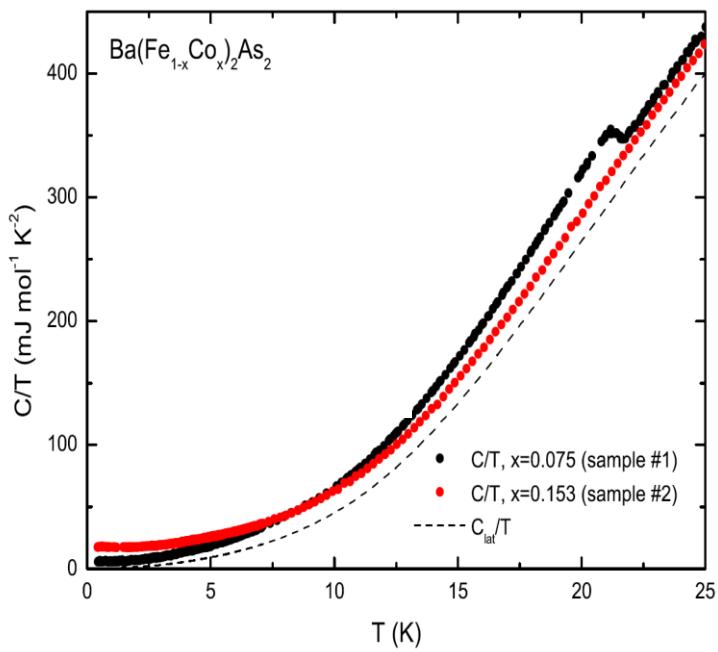
- sharp first-order SDW transition
- no visible precursors (fluctuations) above  $T_{\text{SDW}}$   
how does this fit into NMRpicture?
- clear reduction in electronic density of states below  $T_{\text{SDW}}$

# electronic heat capacity Co-Ba122

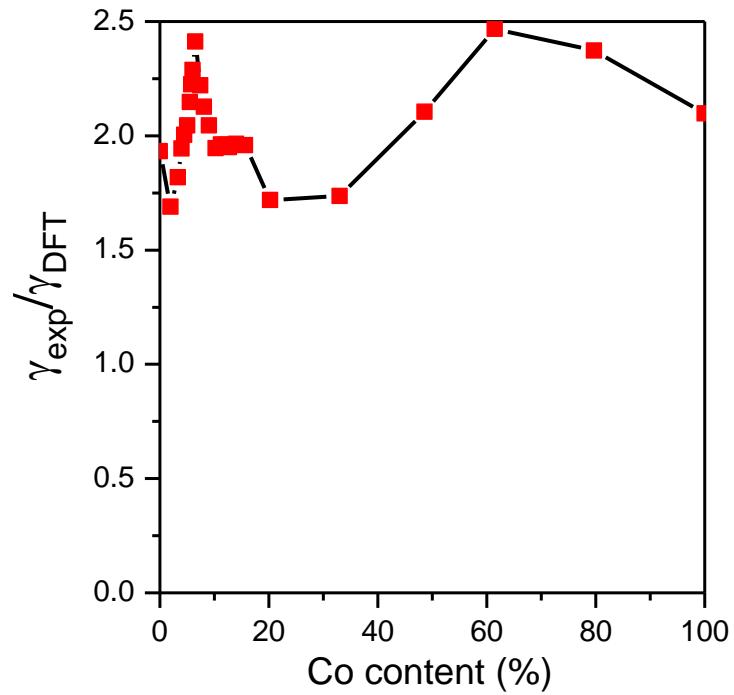
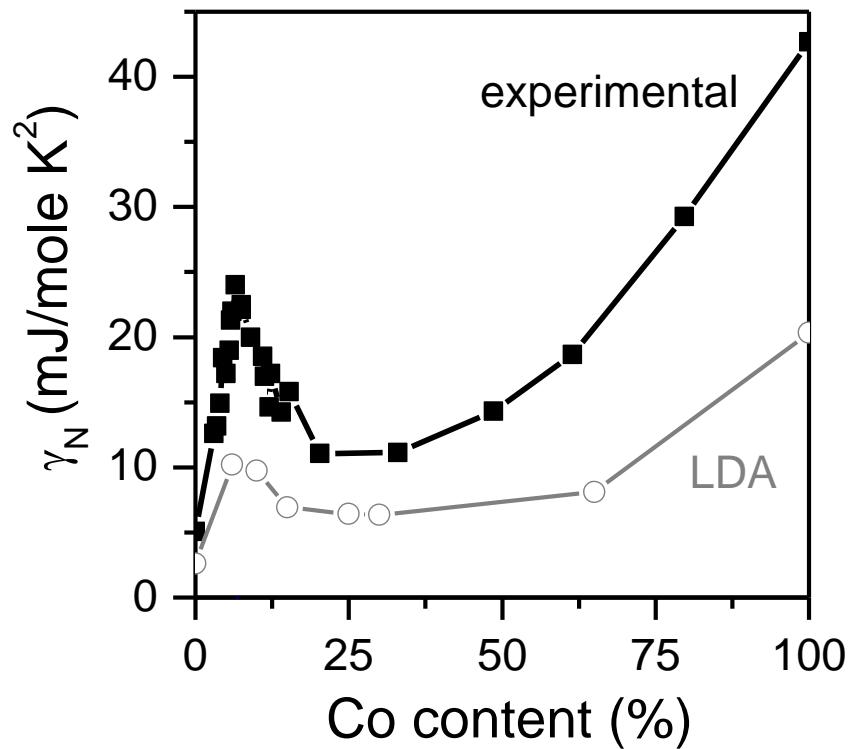
Frederic Hardy et al.

PRB 2009

EPL 2010



# electronic density of states - Sommerfeld coefficient

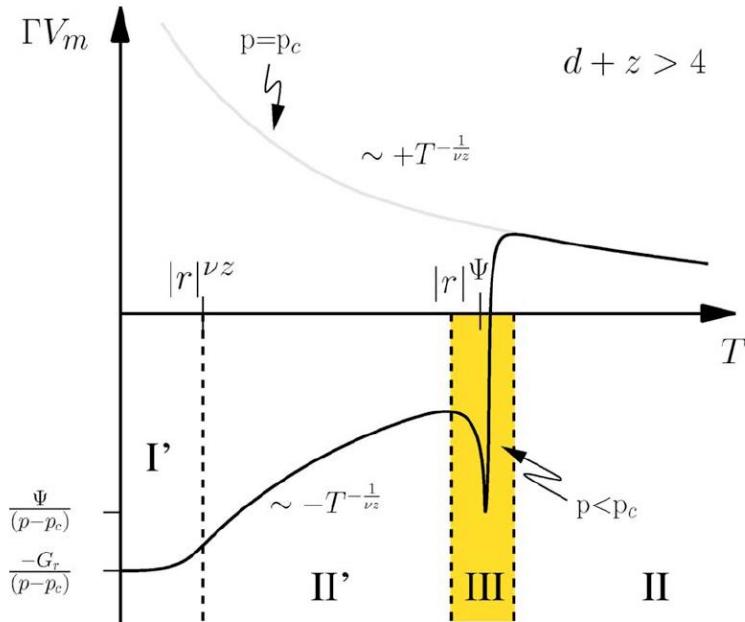
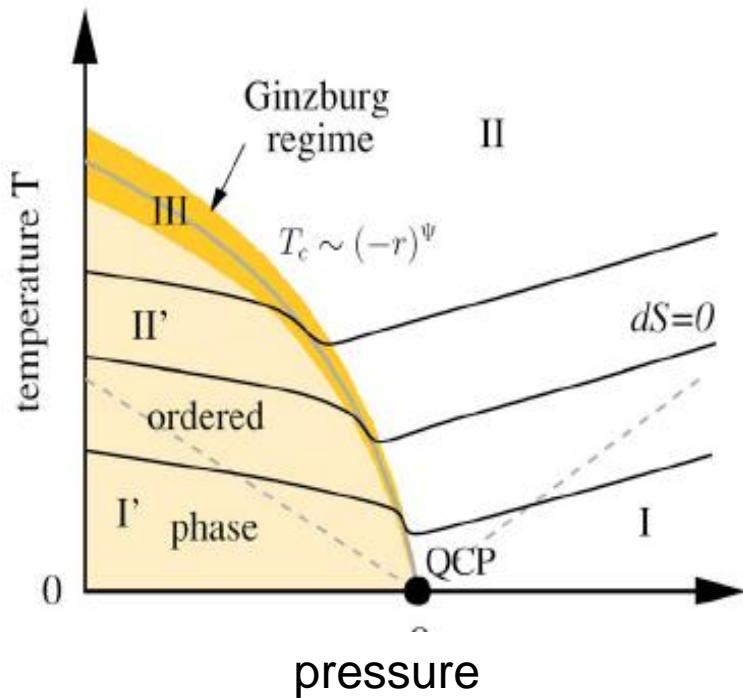


- sharp peak of  $\gamma_N$  at optimal doping
- DFT calculations predict similar peak (factor of 2)  
(SDW gaps FS - gap closes with doping)
- possible small mass enhancement at optimal doping

# *Grüneisen parameter near a QCP- pressure tuning*

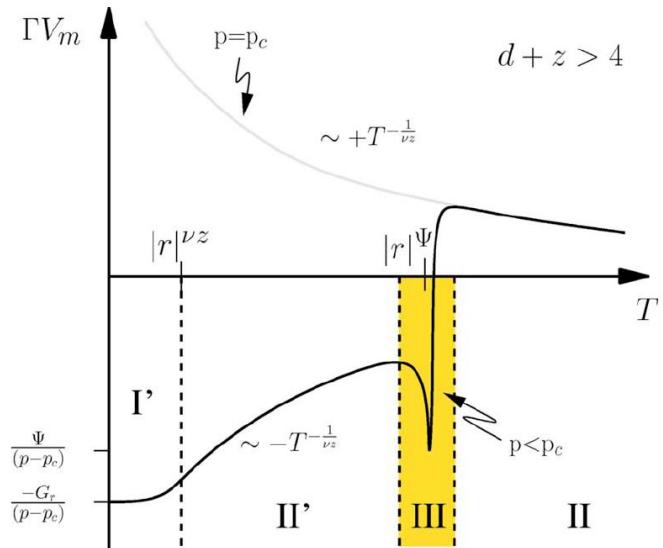
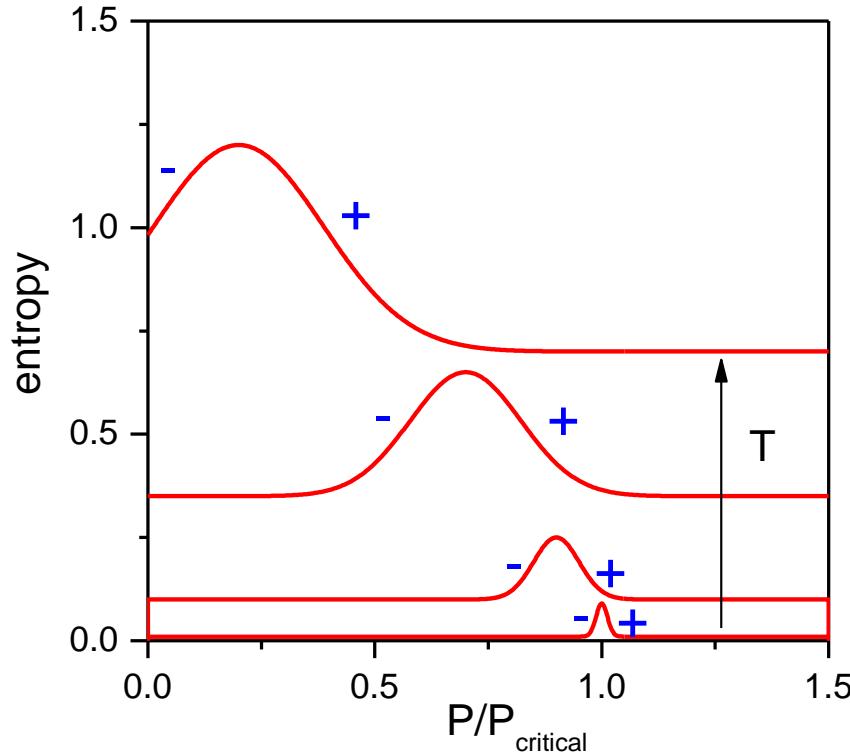
$$\Gamma^{Grüneisen} = \frac{\alpha(T)}{C_p(T)}$$

L. Zhu et al. PRL 2003  
 M. Garst et al. PRB 2005



- divergence of Grüneisen parameter at QCP
- sign change at finite-T transition
- 'smoking gun' of QCP

$$\alpha = \frac{1}{L_i} \frac{dL_i}{dT} = -\left. \frac{dS}{dp_i} \right|_T$$



- accumulation of entropy along critical line ending at the QCP competing phases  
new emergent phases - e.g. superconductivity

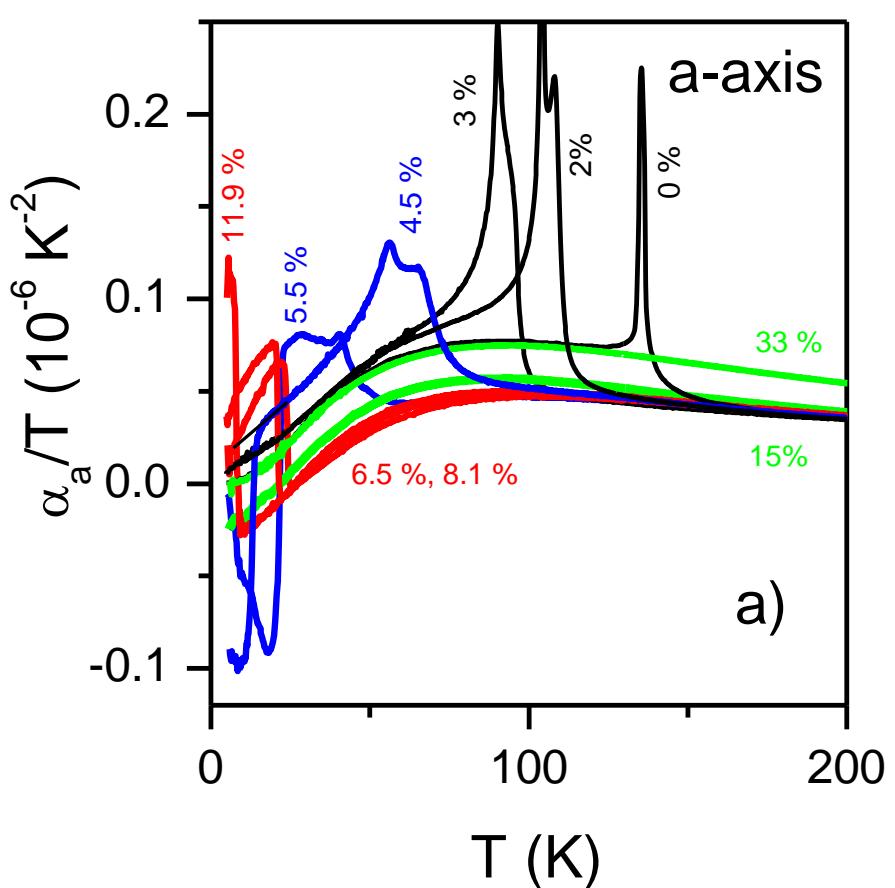
# thermal expansion - capacitance dilatometer



- absolute resolution:  $D L \sim 0.01 \text{ \AA}$
- relative resolution:  $D L/L \sim 10^{-8} - 10^{-10}$   
(diffraction  $\sim 10^{-6}$ )

# thermal expansion of Ba(Fe,Co)<sub>2</sub>As<sub>2</sub>

CM et al. PRL 2012



Fermi liquid

$$\alpha_i(T) = a \cdot T + b \cdot T^3 + \dots$$

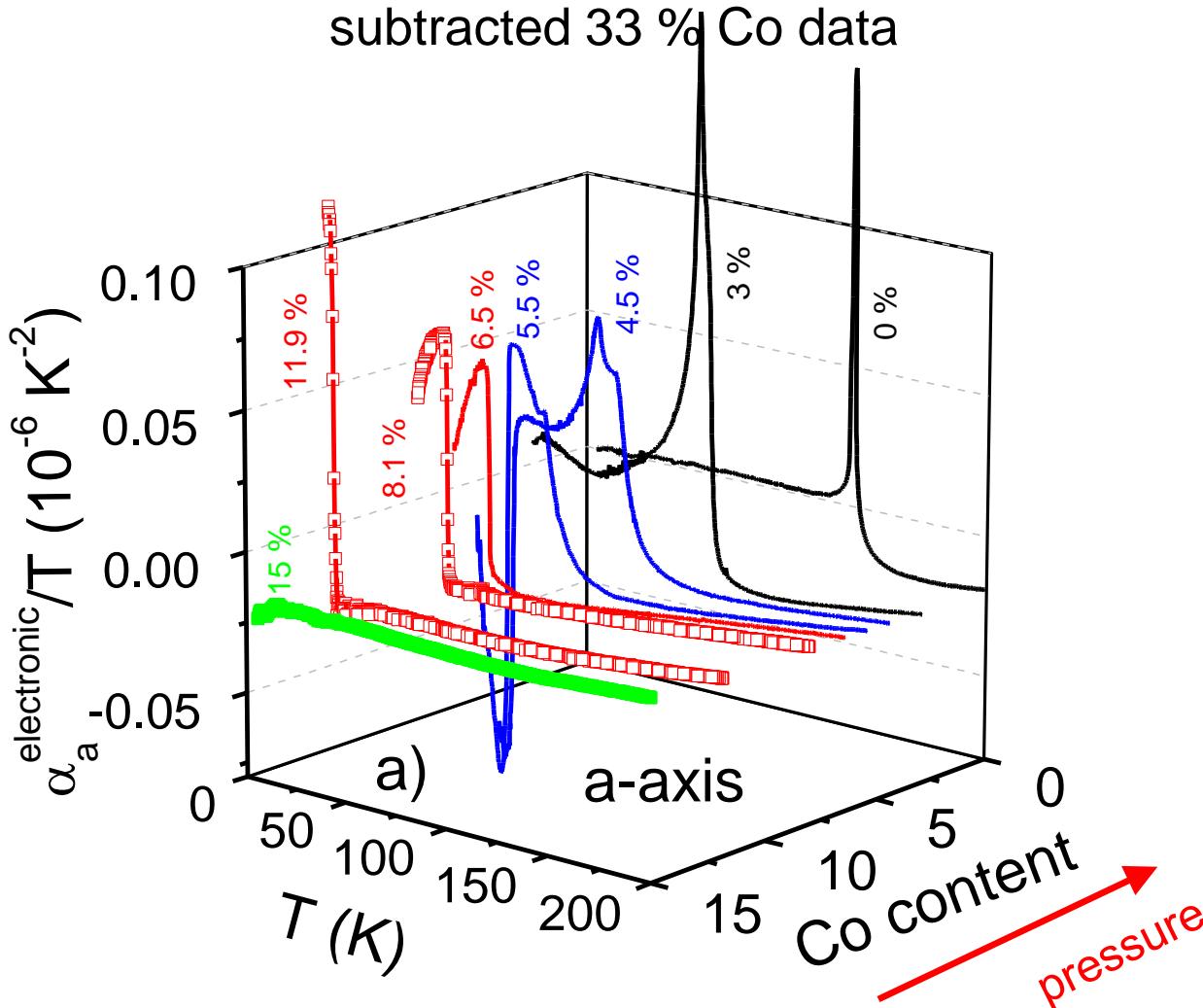
↑  
electronic      phonons

$$\frac{\alpha_i}{T} \Big|_{T=0} = -\frac{d\gamma_N}{dp_i}$$

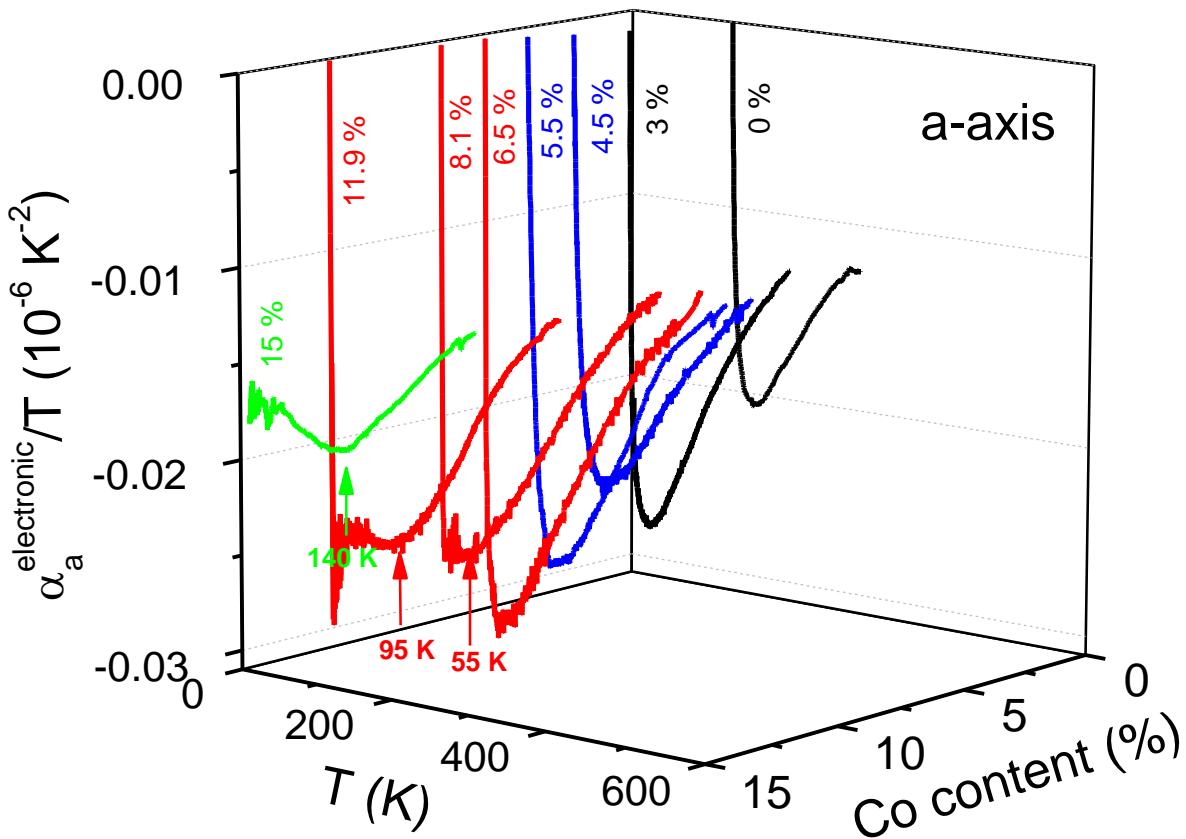
- clear signatures of SDW and superconducting transitions
- use 33 % data as phonon background: nearly zero electronic signal!!

# electronic/magnetic thermal expansion

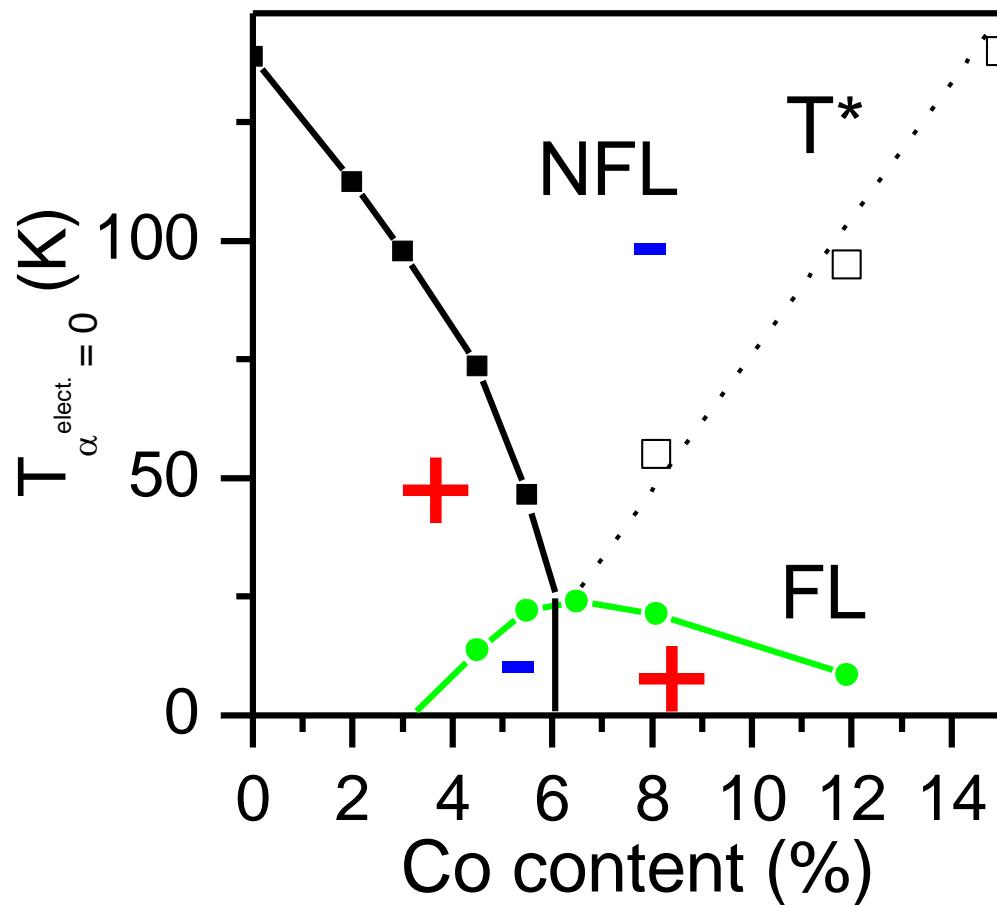
subtracted 33 % Co data



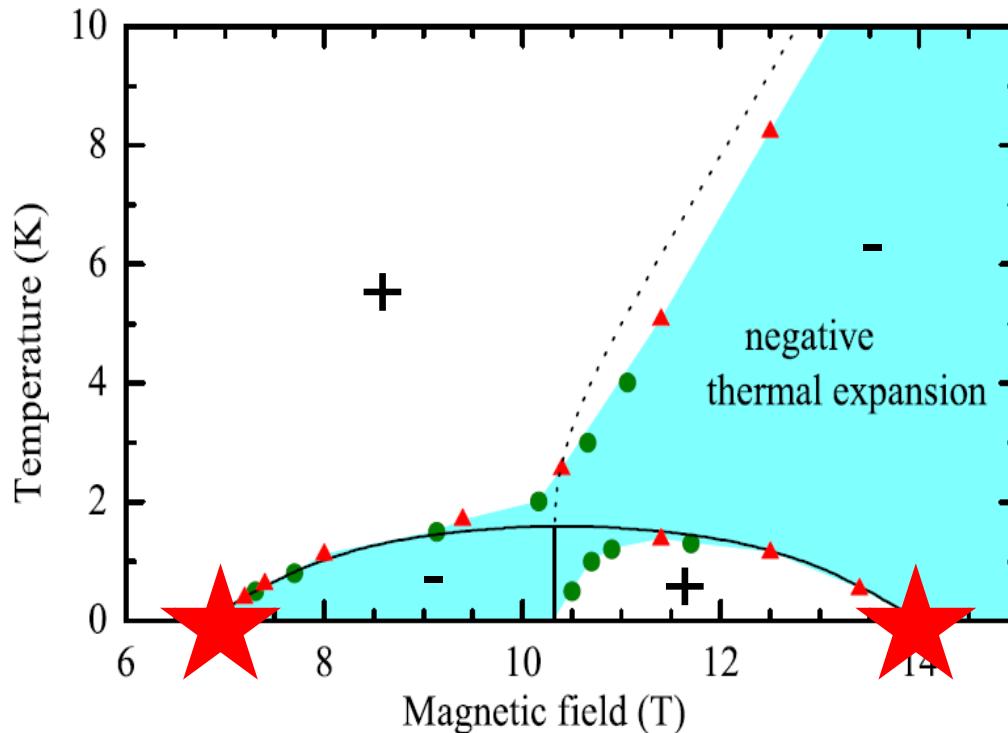
- negative contribution above  $T_{\text{SDW}}, T_c$
- sign changes at  $T_{\text{SDW}}$  and  $T_c$



- clear evidence for non-Fermi liquid state above  $T_{\text{SDW}}, T_c$
- possible crossover to Fermi-liquid behavior below  $T^*$

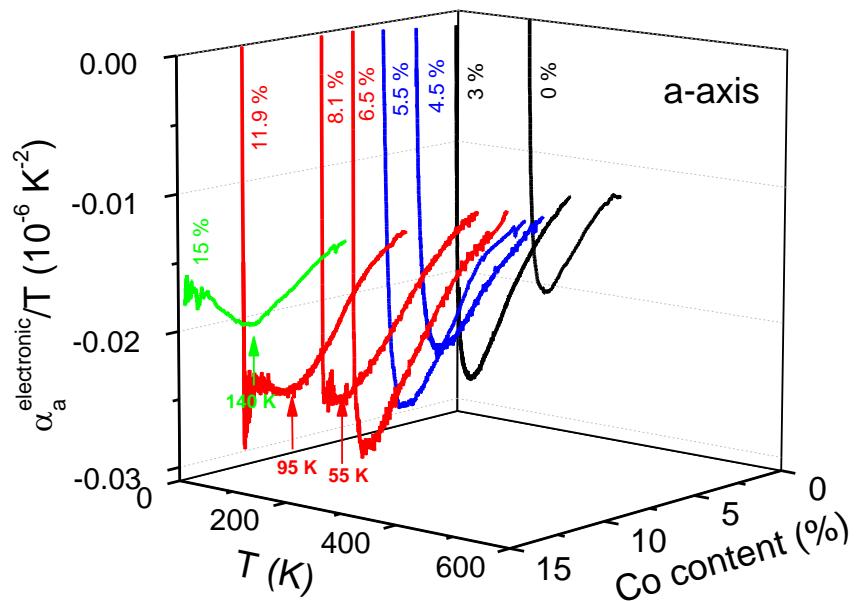
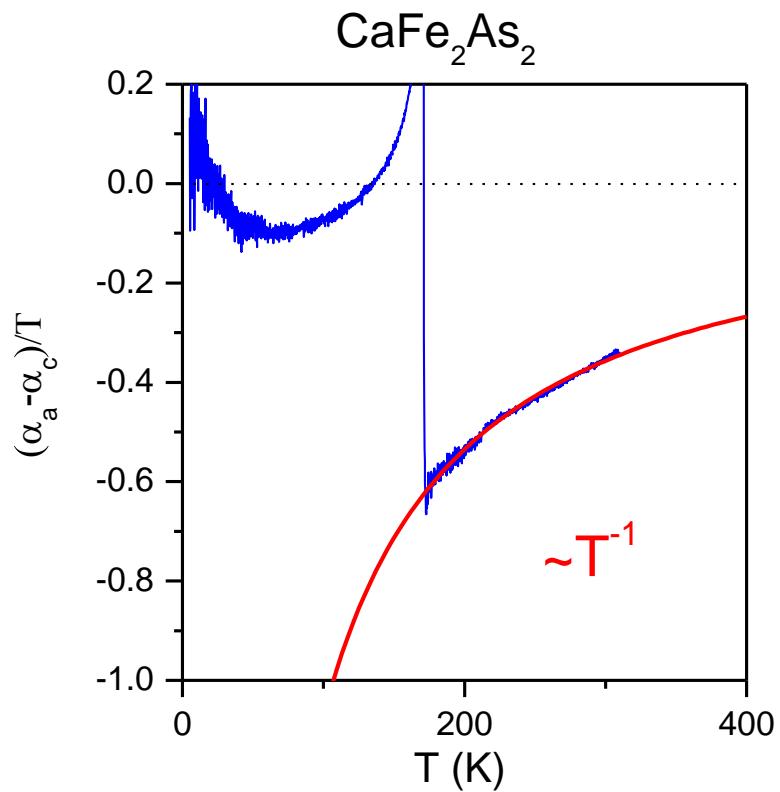


- sign changes of  $\alpha(T)$  - expected behavior at a QCP
- superconductivity is an emergent phase and covers QCP

**Diverging Thermal Expansion of the Spin-Ladder System  $(C_5H_{12}N)_2CuBr_4$** T. Lorenz,<sup>1,\*</sup> O. Heyer,<sup>1</sup> M. Garst,<sup>2</sup> F. Anfuso,<sup>2</sup> A. Rosch,<sup>2</sup> Ch. Rüegg,<sup>3</sup> and K. Krämer<sup>4</sup>

- weakly coupled 1d chains (magnetic field tuning)
- QCP 'hidden' - Bose Einstein condensation of magnons
  - additional sign changes of alpha
  - 2 QCPs (at 7 T and 14 T)

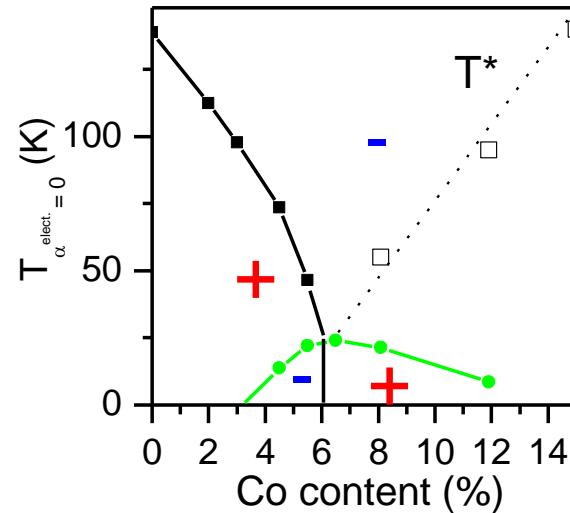
Paul Canfield



# Summary - Co-Ba122

## Evidence for quantum critical scenario?

- small enhancement of effective mass at critical doping
- NFL behavior of thermal expansion above  $T_{SDW}$  (Ca122)
- sign changes of Grüneisen parameters



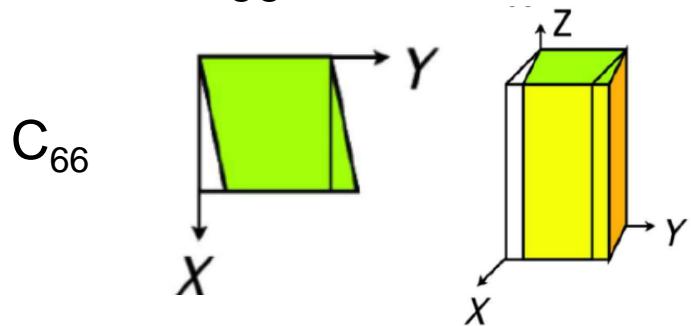
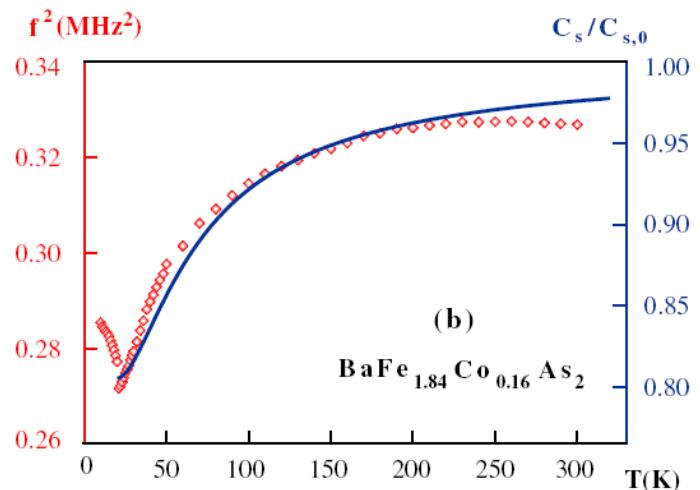
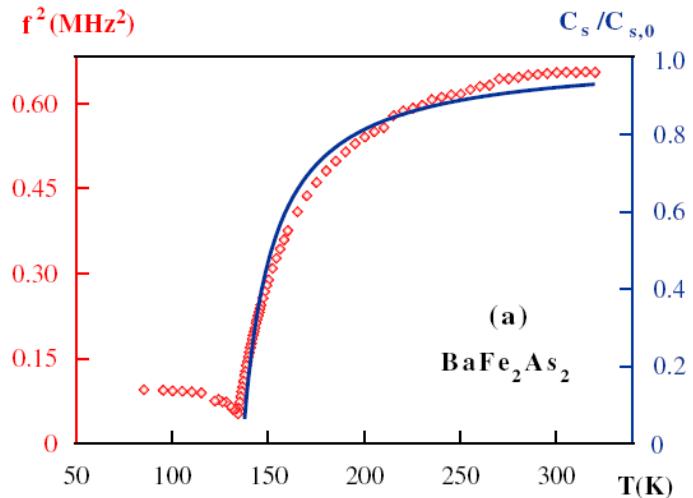
# shear modulus - nematicity

Co- and K-doped Ba122

- A. E. Böhmer, et al. arXiv:1305.3515
- Rafael M. Fernandes, et al. Phys. Rev. Lett. 111, 137001 (2013)

# softening of shear modulus - $C_{66}$

Fernandes et al. PRL 2010



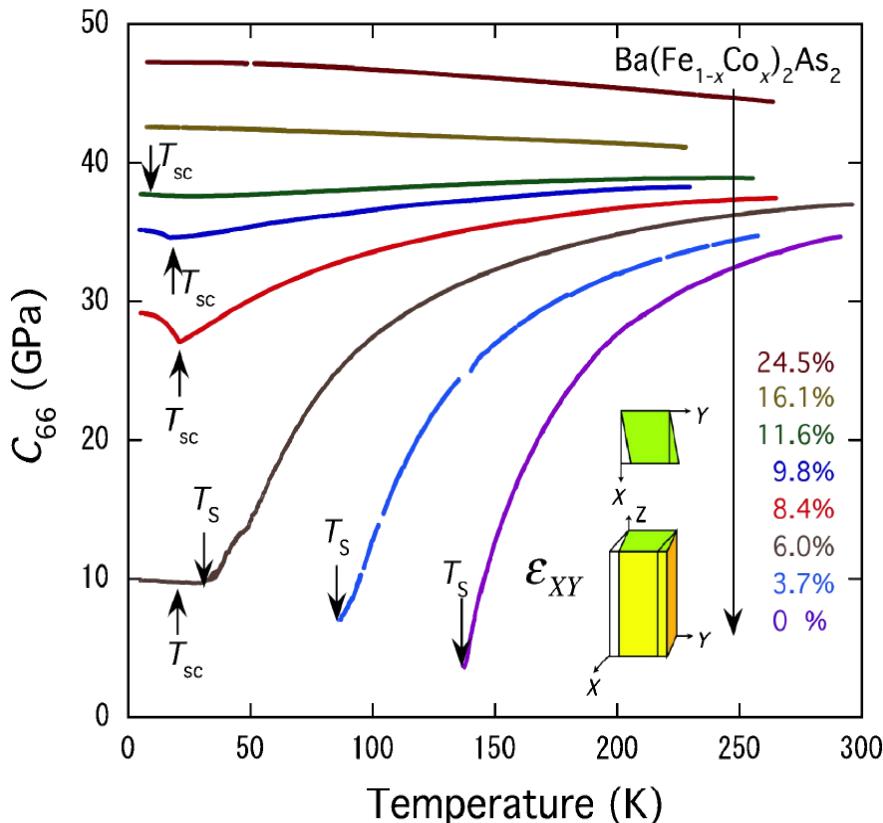
- soft mode of structural/magnetic transition

- **softening:**  
*emergent magnetic/nematic fluctuations*

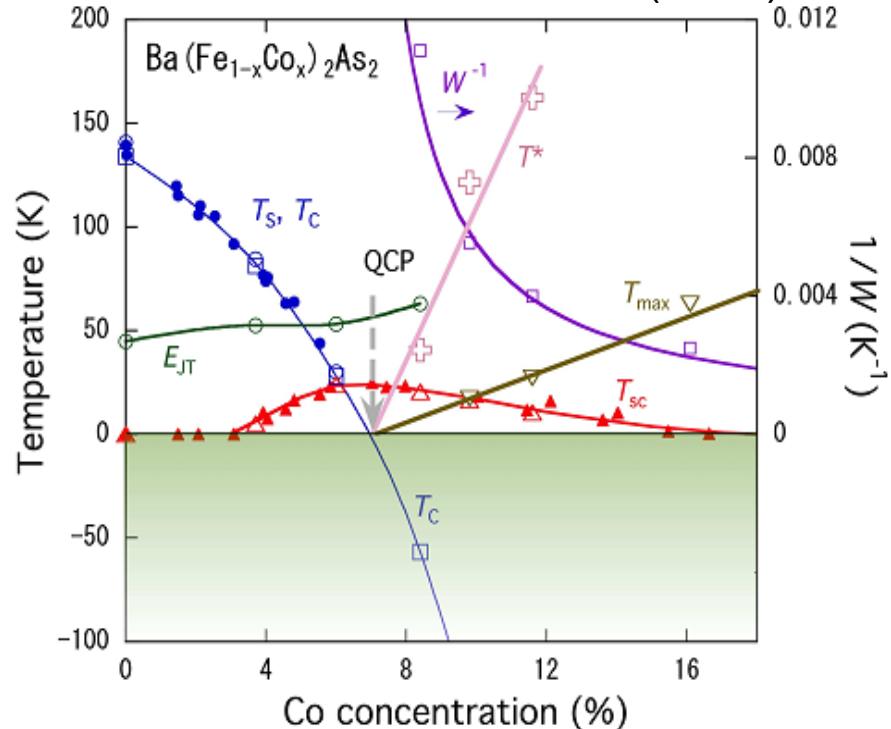
- **hardening below  $T_c$ :**  
*consistent with magnetically driven nematic fluctuations and competing AFM and SC order*

# Structural quantum critical point in Co-Ba122

Yoshizawa et al. JPSJ (2012)



Yoshizawa et al. JPSJ (2012)

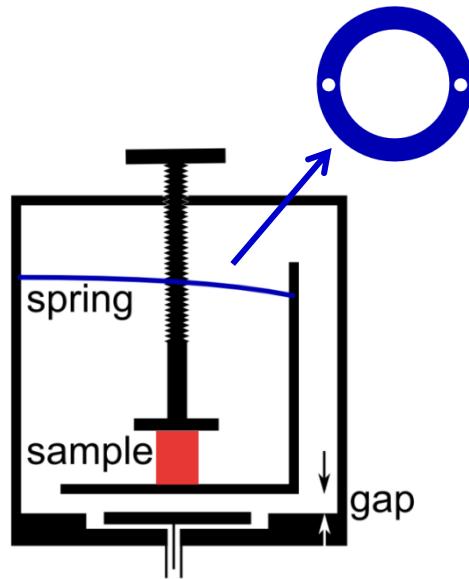


- softening observed also in overdoped tetragonal state
- evidence for 'structural' quantum critical point
- authors stressed importance of **orbital degrees of freedom**

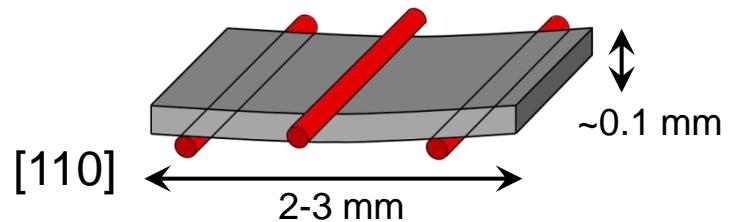
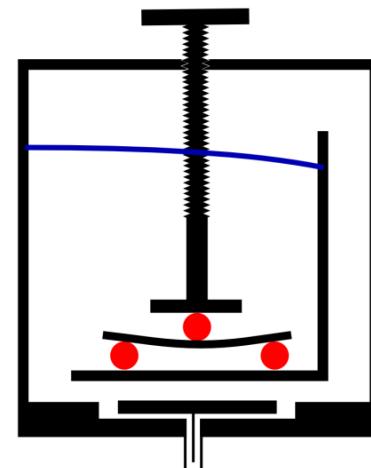
**Question:** Is this behavior universal in pnictides - e.g. K-Ba122?

## ■ Young's modulus in a capacitance dilatometer

A. E. Böhmer, et al. arXiv:1305.3515



resolution:  $10^{-11}$ - $10^{-12}$  m



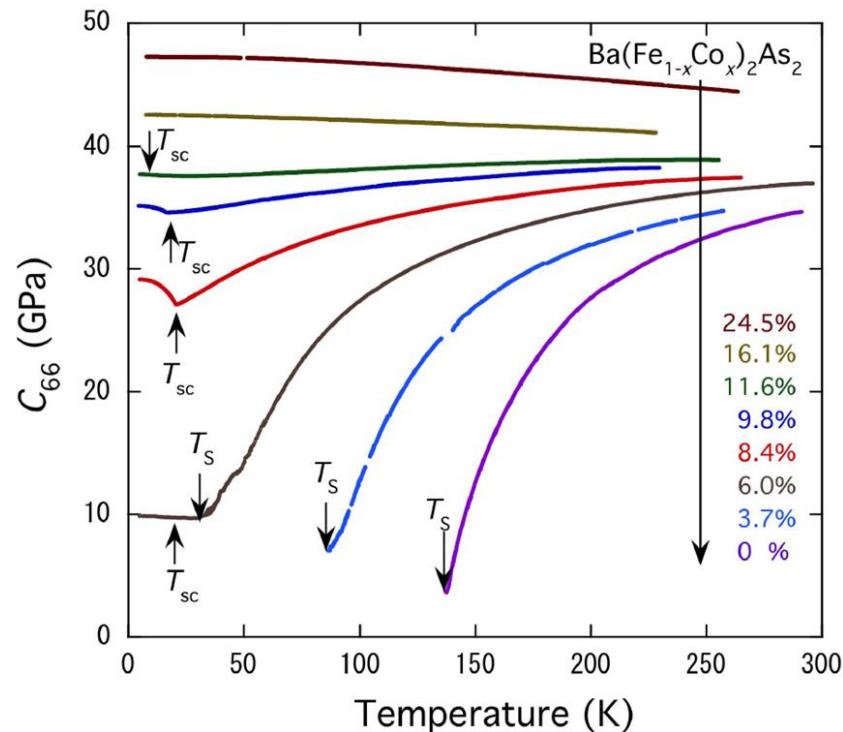
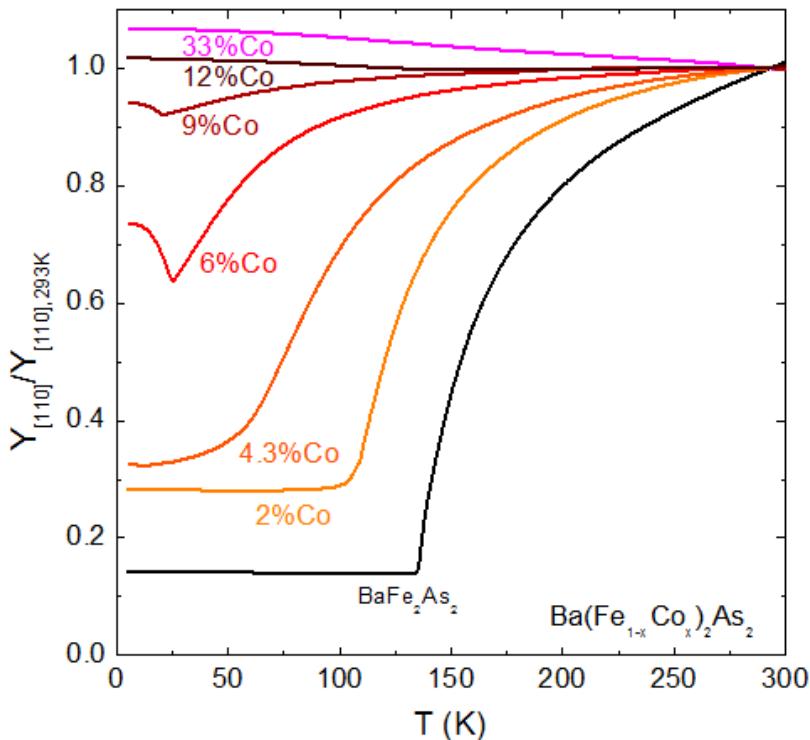
- Measure bending changes under constant force (~20 g) with high resolution vs T
- Young's modulus is directly related to  $C_{66}$  if  $C_{66}$  is small

$$Y_{[110]} = 4 \left( \frac{1}{C_{66}} + \frac{1}{\gamma} \right)^{-1} \text{ with } \gamma = \frac{C_{11}}{2} + \frac{C_{12}}{2} + \frac{C_{13}^2}{C_{33}}$$

e. g. Kityk et al., PRB, 2000

# Young's modulus vs $C_{66}$ from ultrasound: Co-Ba122

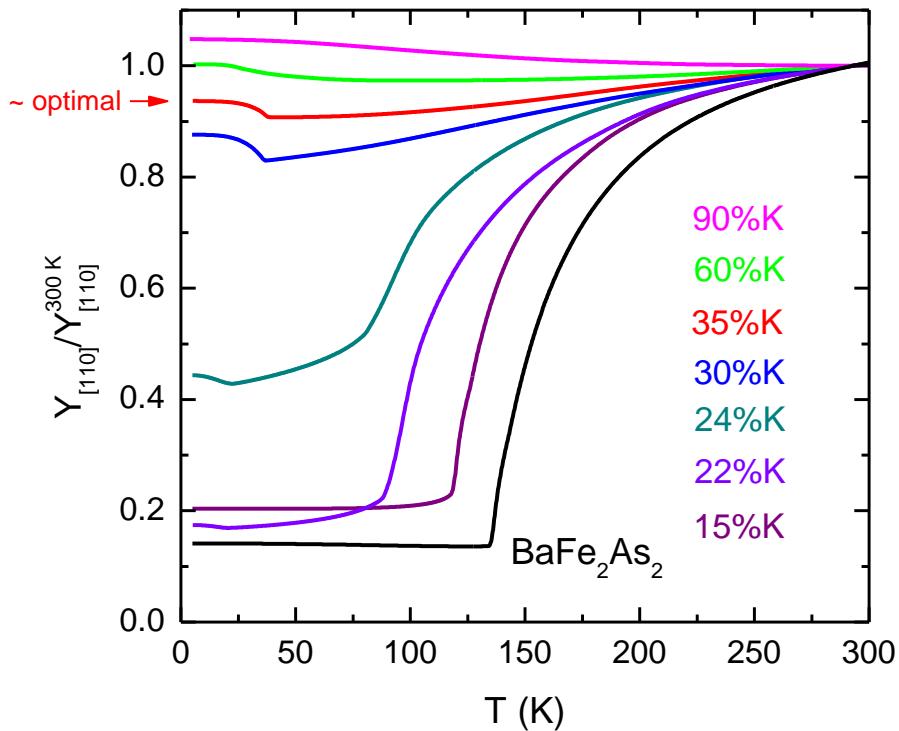
A. E. Böhmer, et al. arXiv:1305.3515



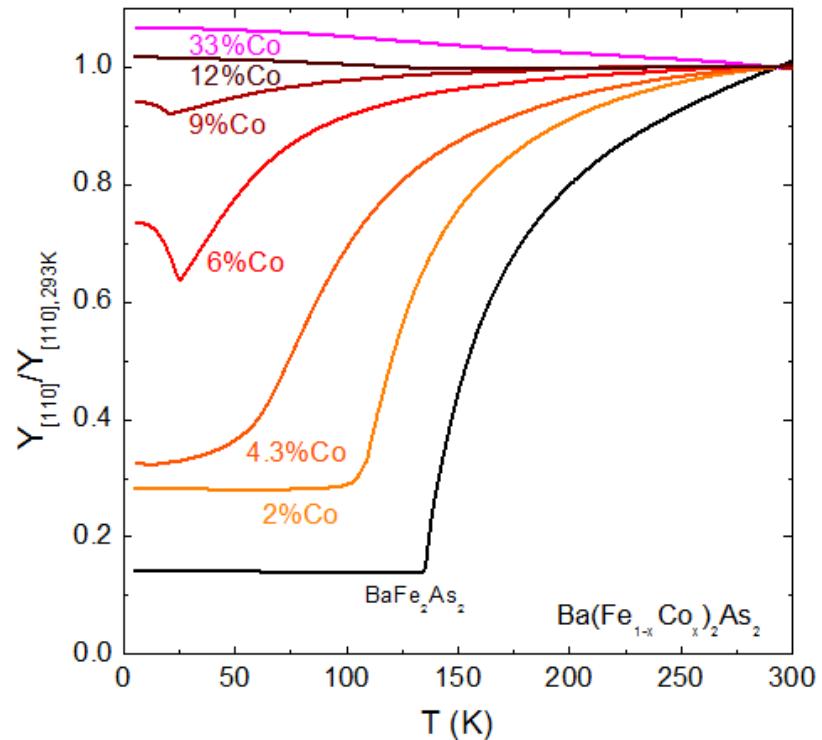
- Good qualitative agreement with  $C_{66}$  from ultrasound measurements by Yoshizawa et al.
- Young's moduli are normalized at room temperature

# Young's modulus: K- and Co-doped Ba122

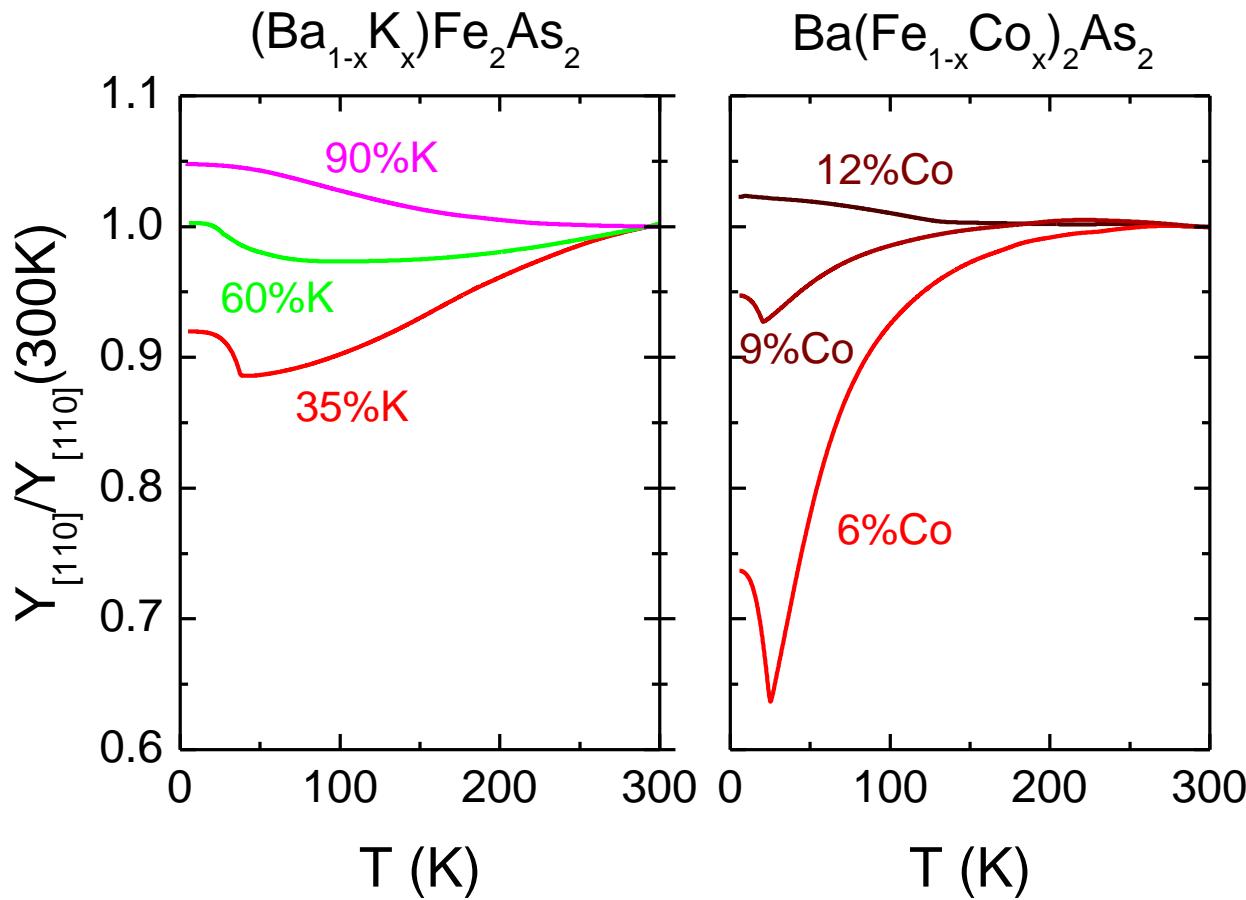
K-Ba122



Co-Ba122

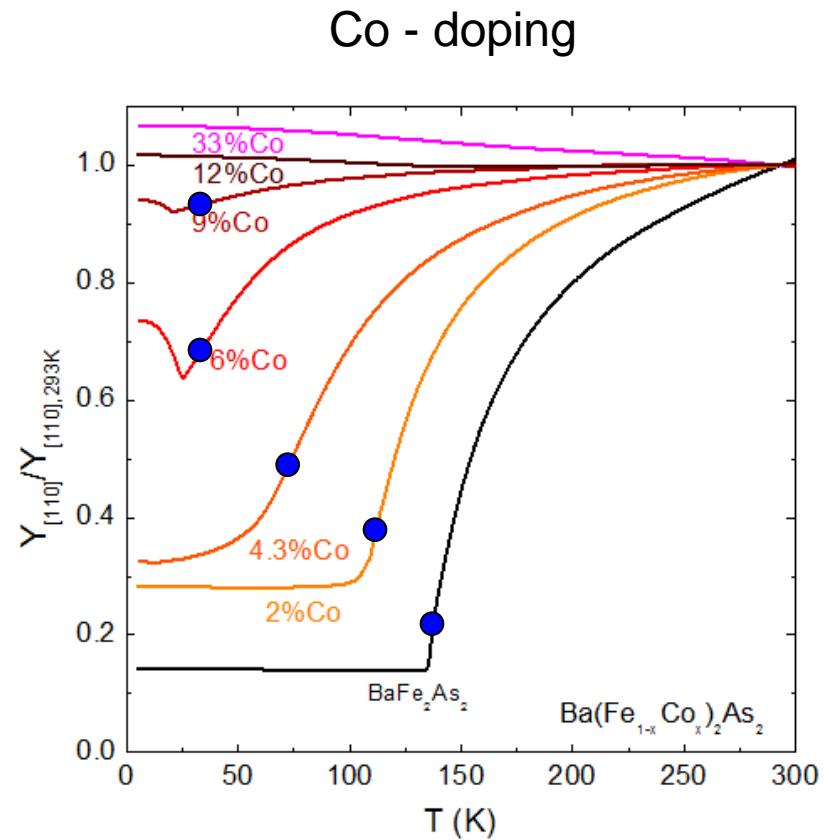
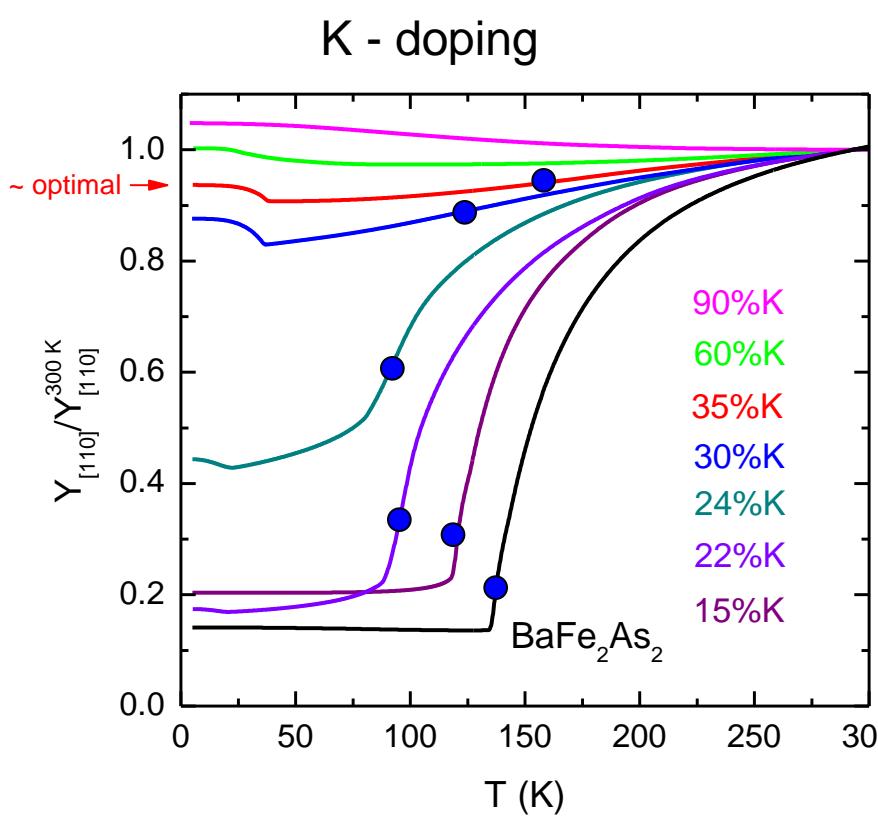


- K-Ba122 Young's moduli: qualitatively similar to Co-Ba122 data
- differences:
  - behavior at optimal doping less 'critical'
  - almost no hardening seen below  $T_c$  for 60 % K ( $T_c = 28$  K) vs 9 % Co



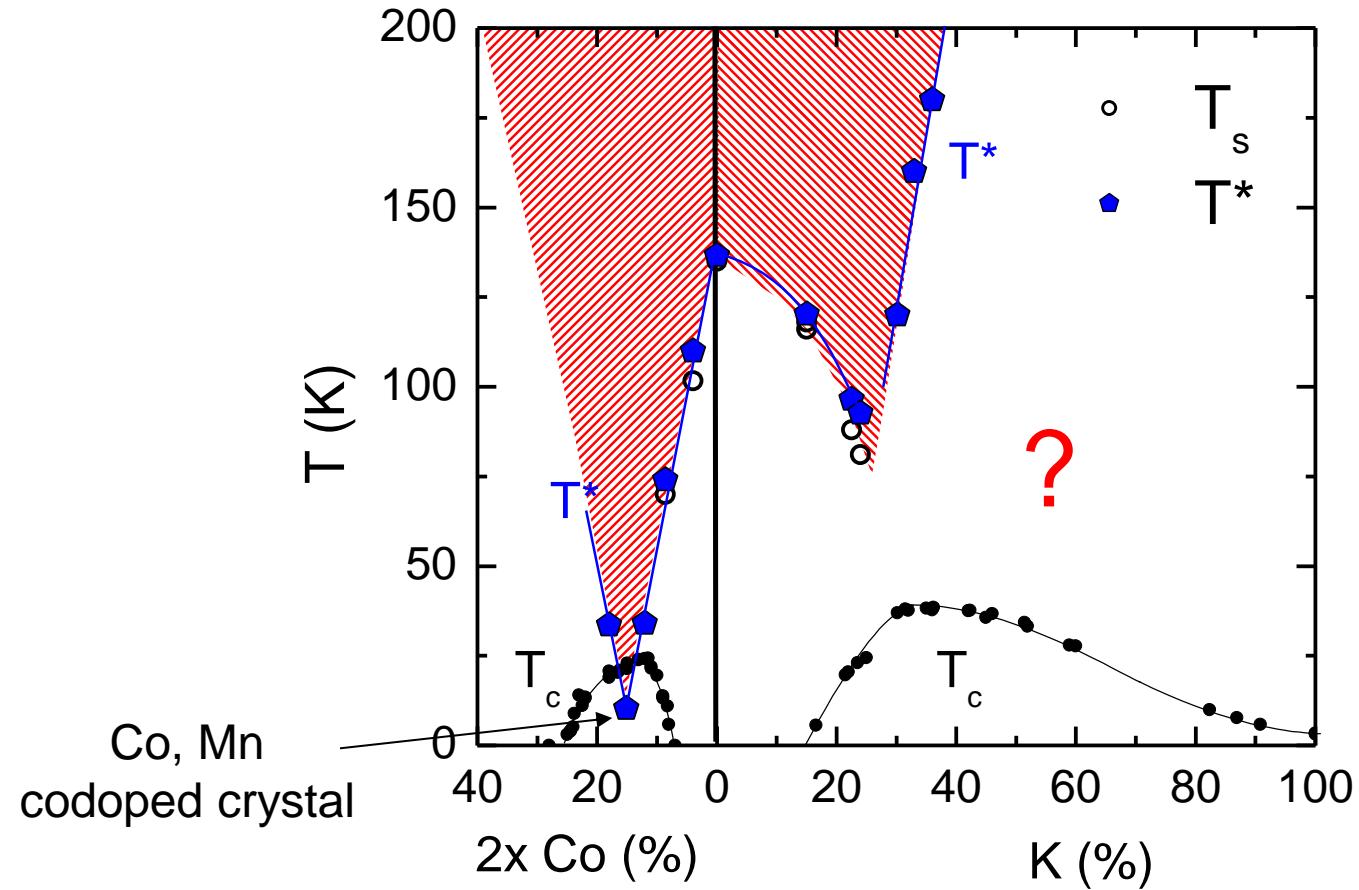
- clear difference at optimal doping - lack of critical behavior in shear modulus for K-doping
- broad hardening for 60 % K below 100 K (not related to  $T_c$ !)
- versus softening and hardening for 9 % Co (similar reduced  $T_c$ )

# Quantum critical points: K- vs Co-doping?



- Inflection points - maximum in 'nematic susceptibility'
- plot points vs doping.

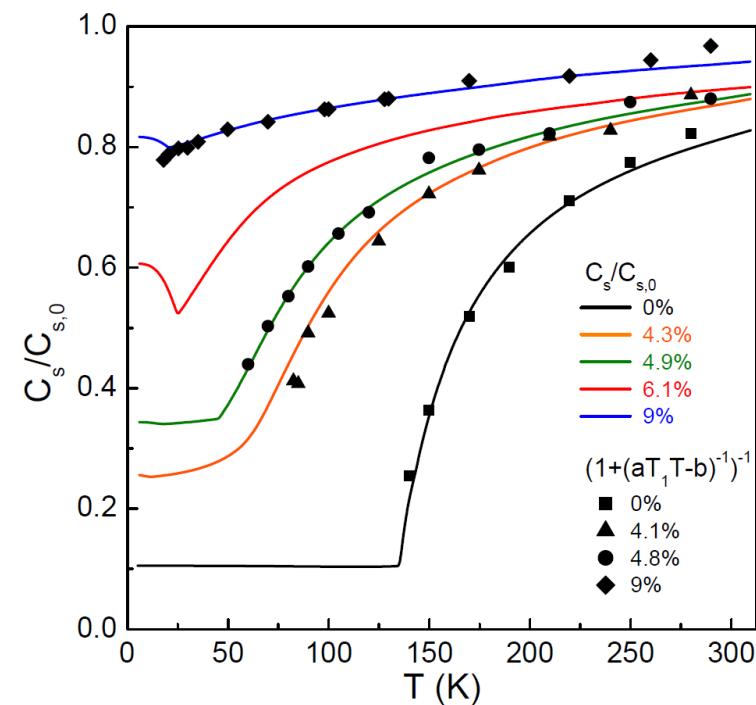
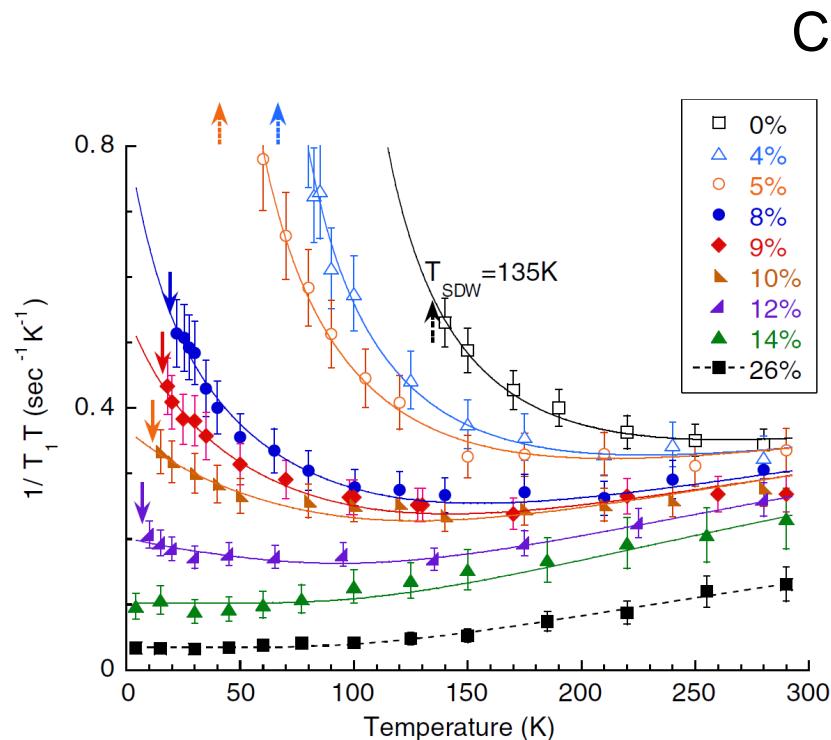
# Phase diagram of 'divergent' lattice softening



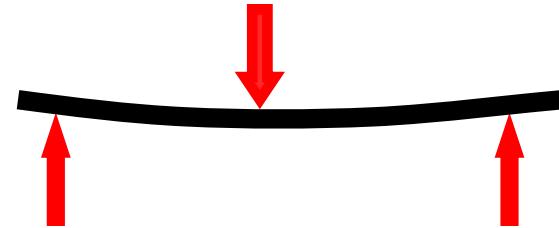
- Co - doping: resembles expected behavior at a quantum critical point
- K - doping: softening cut off already at high temperatures - lack of real QCP!
- Large region at higher K doping without large softening (and hardening)
- Question: Can one explain relatively large  $T_c$  (28 K at 60 % K) within spin mediated pairing scenario? Lack of critical softening and hardening!

# Scaling between magnetic and lattice fluctuations in a family of iron-pnictide superconductors

Rafael M. Fernandes,<sup>1</sup> Anna E. Böhmer,<sup>2</sup> Christoph Meingast,<sup>2</sup> and Jörg Schmalian<sup>3</sup>



$$\frac{C_s}{C_{s,0}} = \frac{1}{1 + [a(T_1 T) - b]^{-1}}$$



## Conclusions - shear modulus

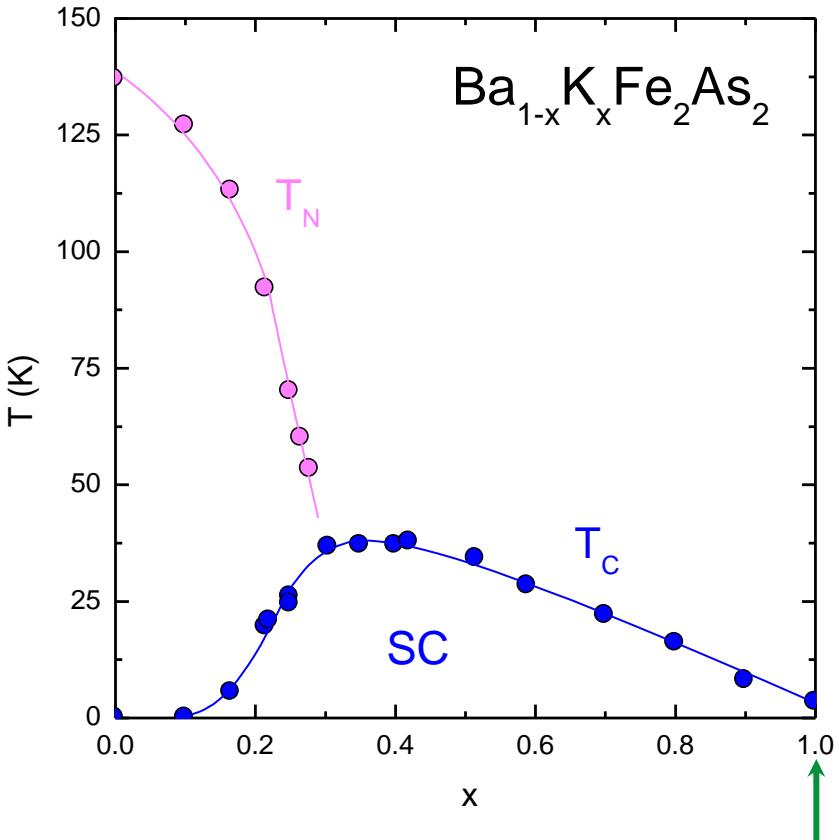
- New technique: three-point-bending in capacitance dilatometer
  - High resolution – crystals don't need to be perfect!!
- Confirmation of 'quantum criticality' in  $\text{Ba}(\text{Fe},\text{Co})_2\text{As}_2$
- New results for  $(\text{Ba},\text{K})\text{Fe}_2\text{As}_2$ :
  - Absence of quantum criticality !
  - Maximum  $T_c$  not at the point of vanishing orthorhombic order
  - Little coupling of  $C_{66}$  shear mode with superconductivity for overdoped samples
  - Reconcile  $T_c=28\text{K}$  at 60%  $(\text{Ba},\text{K})\text{Fe}_2\text{As}_2$  within spin-fluctuation scenario?



specific heat, magnetization,  
thermal expansion,..

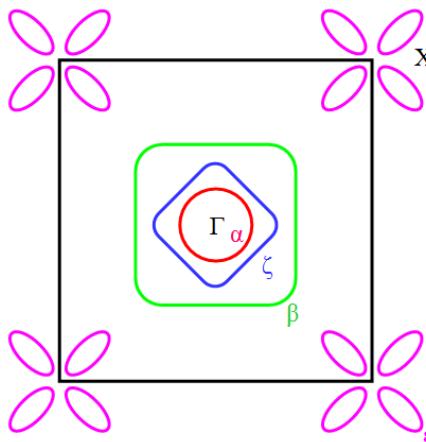
- F. Hardy, et al. Phys. Rev. Lett. 111, 27002 (2013)
- P. Burger, et al. Phys. Rev. B 88, 014517 ( 2013)
- Frederic Hardy, et al., arXiv:1309.5654

# KFe<sub>2</sub>As<sub>2</sub>



KFe<sub>2</sub>As<sub>2</sub>

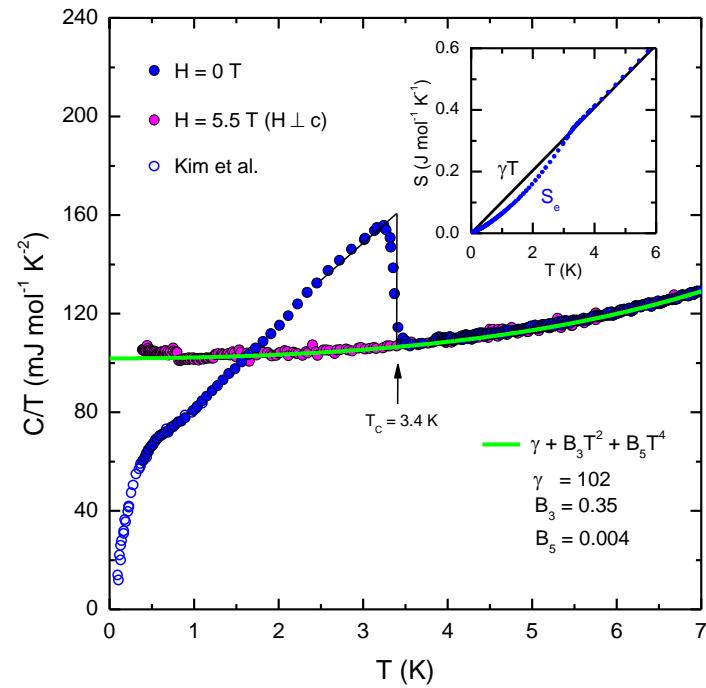
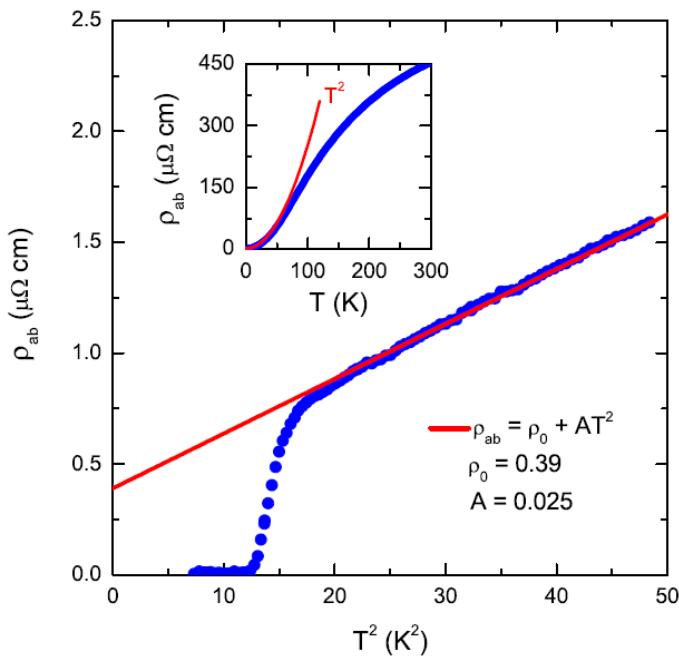
$T_C = 3.4$  K



- stoichiometric - clean system!!
- non magnetic
- strongly correlated - Hund's metal
- '3d heavy fermion metal'
- low  $T_c$  - 3.4 K (advantage!)
- nodes? (nodal-s or d-wave?)

# resistivity and heat capacity

F. Hardy, et al. PRL 111, 27002  
(2013)



- Fermi liquid!
- clean: RRR ~ 1000 - 2000

Sommerfeld coefficient

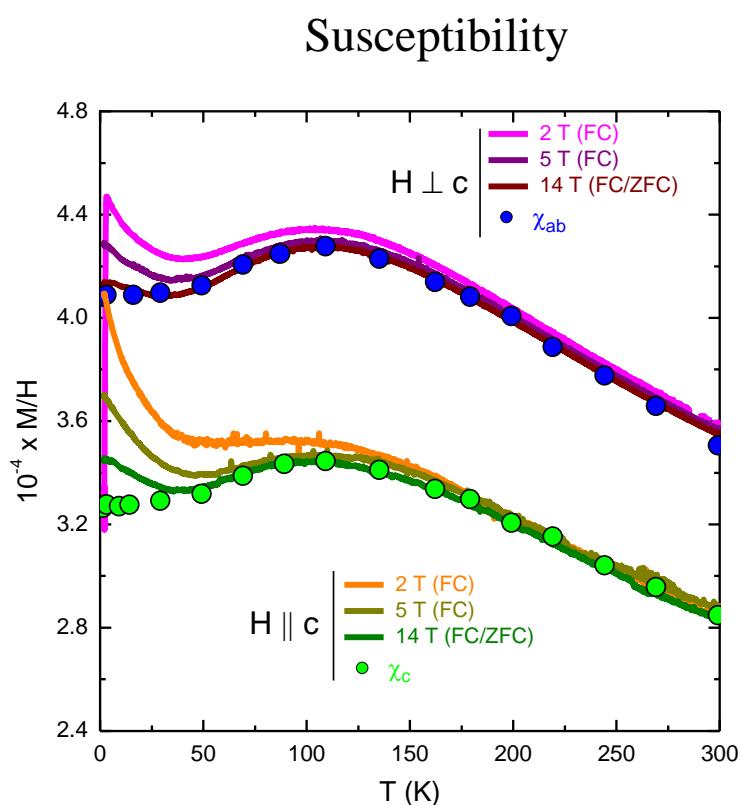
$$\gamma_n = 102 \text{ mJ mol}^{-1} \text{K}^{-2}$$

$$(\gamma_{LDA} = 10 \text{ mJ mol}^{-1} \text{K}^{-2})$$

- strongly correlated!!
- small gap

# Coherence – incoherence crossover

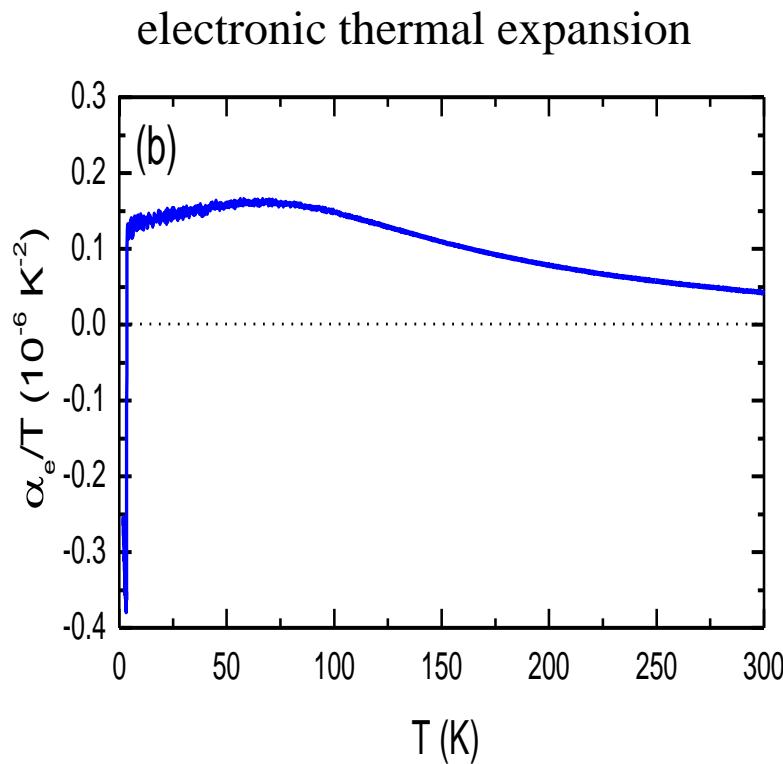
F. Hardy, et al. PRL 111, 27002  
(2013)



Pauli susceptibility

$$\chi_c = 3.3 \times 10^{-4}$$

$$\chi_{ab} = 4.1 \times 10^{-4}$$



Similar to heavy-fermion compounds

$T \ll T^*$  : heavy Landau quasiparticles (FL)

$T \gg T^*$  : strongly incoherent regime  
local moment behavior

# correlations: orbitally-selective Mott transition?

F. Hardy, et al. PRL 111, 27002 (2013)

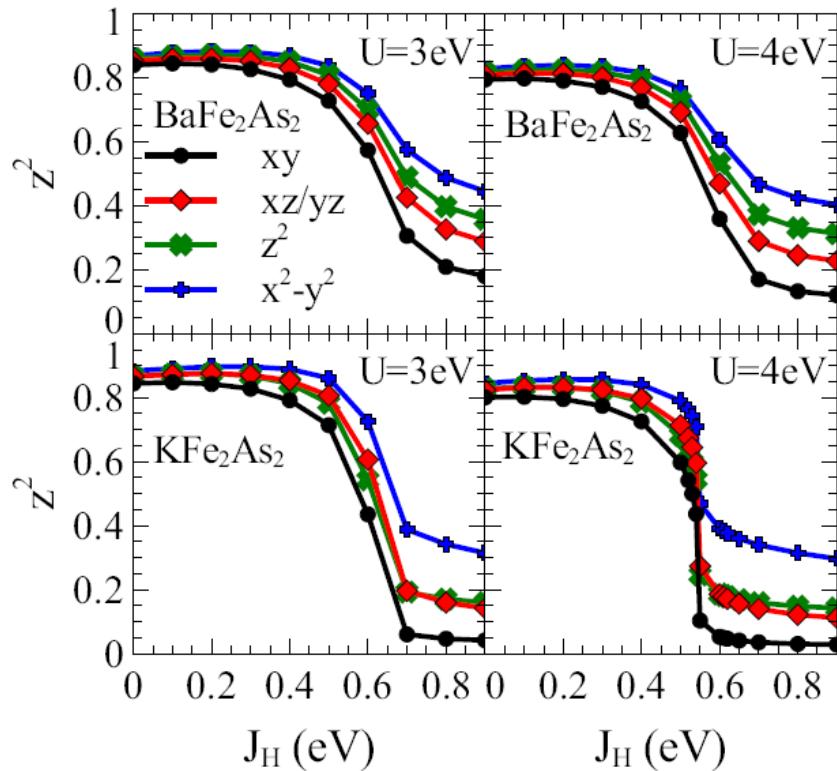


FIG. 5: (Color online) Gutzwiller slave-boson mean-field calculations of the orbitally-resolved mass-enhancement factor  $z_\alpha$  for  $\text{BaFe}_2\text{As}_2$  and  $\text{KFe}_2\text{As}_2$ , for two different values of the intraorbital Coulomb repulsion  $U$ .

LDA+DMFT: Strong Hund's coupling

Haule, et al., New J. Phys. 11, (2009) 025021

Yin, Nature Materials 10, (2011) 932

de' Medici, et al., arxiv:1212.3966 (2012)

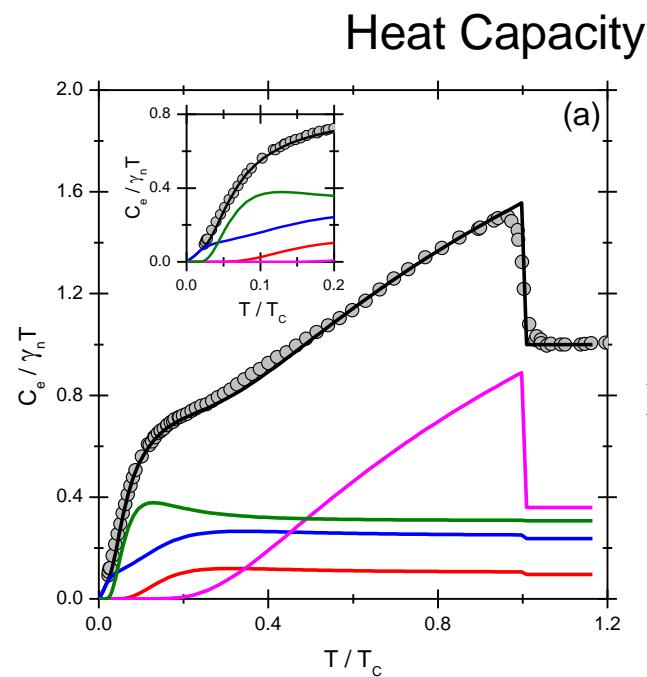
Kondo interactions between  
localized spins and itinerant  $e$

L.P. Gor'kov et al., PRB 87 (2012) 024504

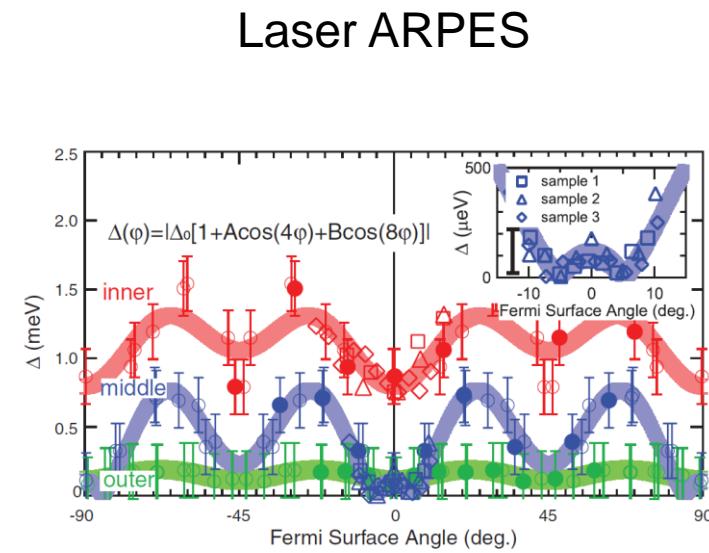
J. Schmalian, G. Kotliar

# specific heat - 4-band BCS model

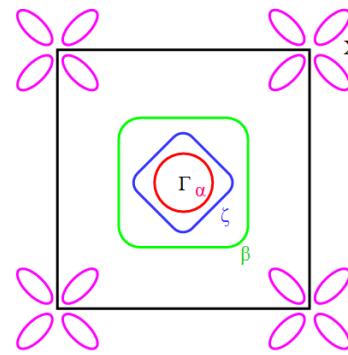
Frederic Hardy, et al., arXiv:1309.5654



- four-band BCS 'fit'
- density of states from de Haas-van Alphen
- consistent with ARPES (not values of  $\Delta$ !)
- small gaps and nodes

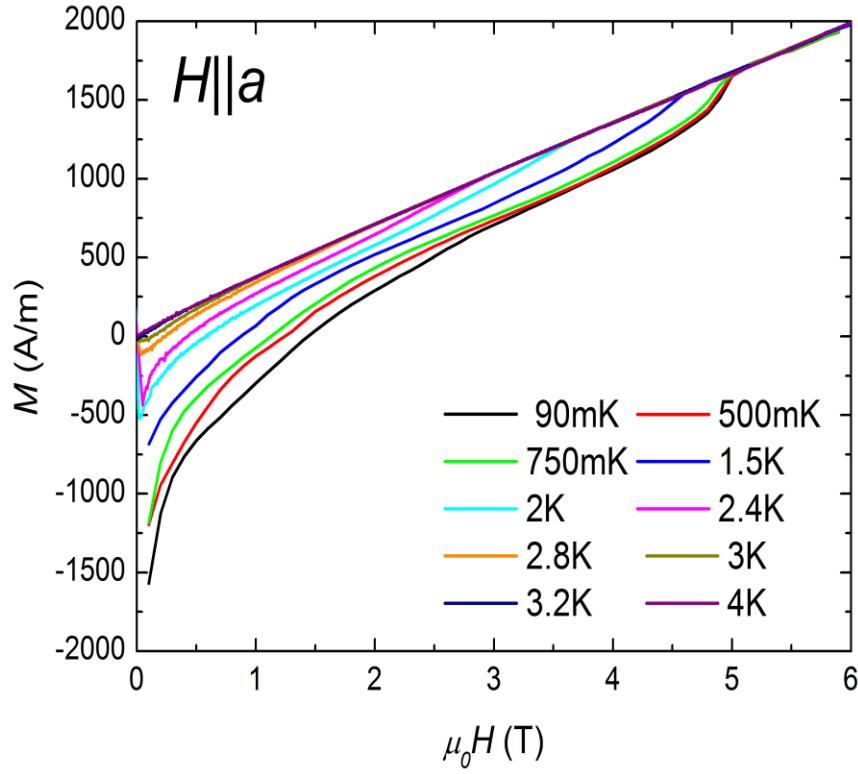


Okazaki et al., Science 337 (2012) 1314

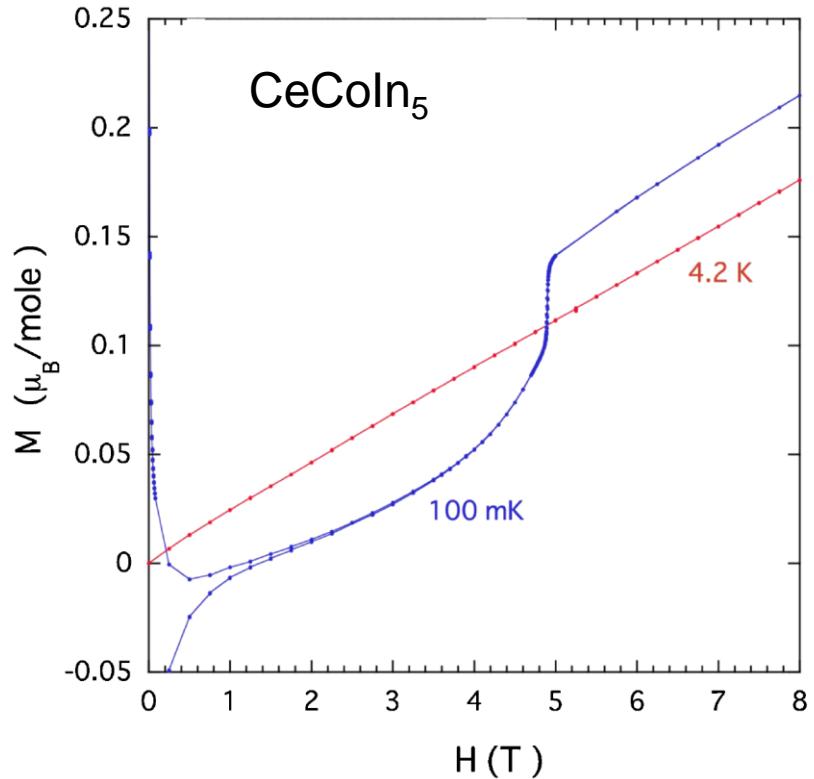


# Strong Pauli-limiting behavior - KFe<sub>2</sub>As<sub>2</sub> H||a

P. Burger, et al. Phys. Rev. B 88, 014517 ( 2013)



Paulsen et al., JPSJ 80 (2011) 053701



- strong Pauli limitation seen at low temperatures  
weakly first-order transition at  $H_{c2}$   
FFLO?
- similar to CeCoIn<sub>5</sub>

# H-T phase diagram

Simple approximation of Pauli field

- single band
- ignore vortices....

$$H_p = \sqrt{\frac{1}{\chi_n}} H_c$$

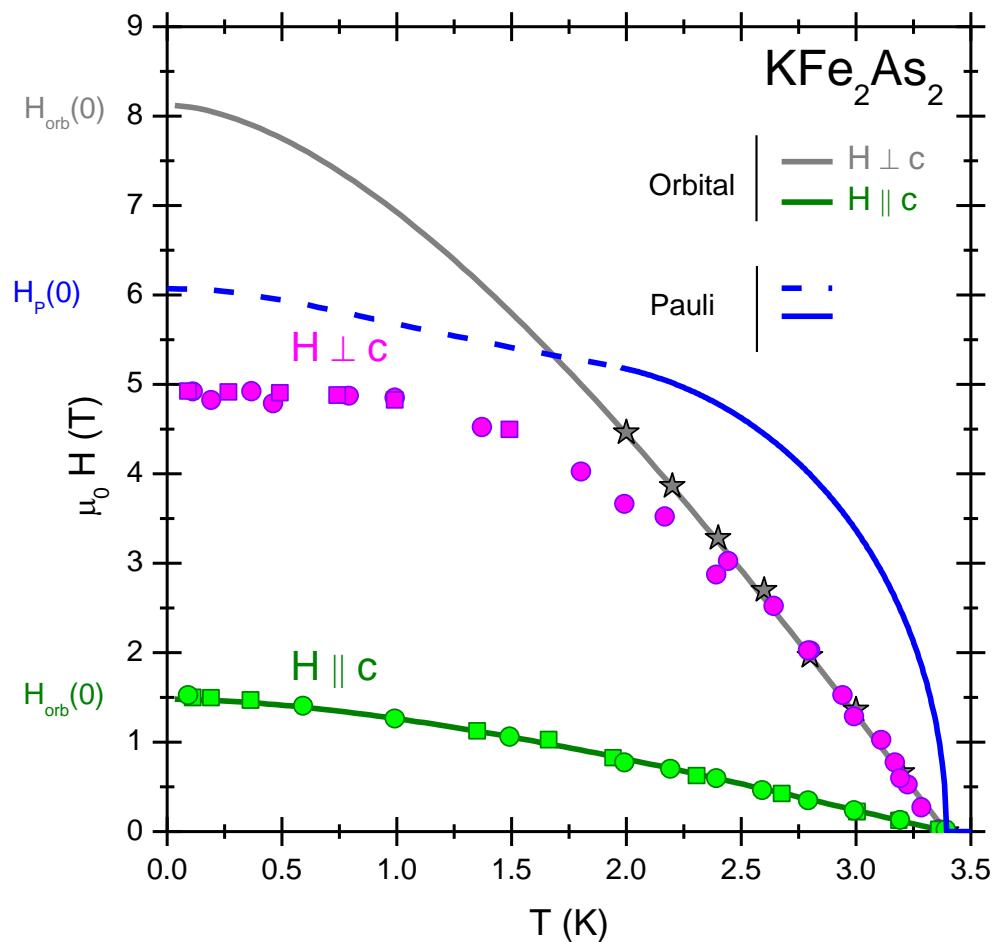
$$H_c = 0.072 \text{ T}$$

$$\chi_n^a = 4.1 \cdot 10^{-4}$$

$$\chi_n^c = 3.2 \cdot 10^{-4}$$

(Hardy et al PRL 2013)

$$H_p = 3.5 - 3.9 \text{ T}$$



Maki parameter:  $\alpha_M \approx 1.9$

# Conclusions - K122

- Strong ‘Hund’ correlations
- Coherence-incoherence crossover
- **Large s-wave gap** - several tiny energy gaps
- Strong paramagnetic effects - Pauli limited  $H_{c2}$  (FFLO?)

Thanks

# Superconducting state

## 4-band BCS analysis (*s*-wave)

Hardy, et al., unpublished

### Angle-indep. intraband

$$V_{\alpha\alpha}^0 = V_{\beta\beta}^0 = V_{\zeta\zeta}^0 = V_1$$

$$V_{\varepsilon\varepsilon}^0 = 2.5 \cdot V_1$$

### Angle-indep. interband

$$V_{\alpha\beta}^0 = V_{\alpha\zeta}^0 = V_{\beta\zeta}^0 = 0.7 \cdot V_1$$

$$V_{\alpha\varepsilon}^0 = -0.5 \cdot V_1$$

$$V_{\zeta\varepsilon}^0 = -0.15 \cdot V_1$$

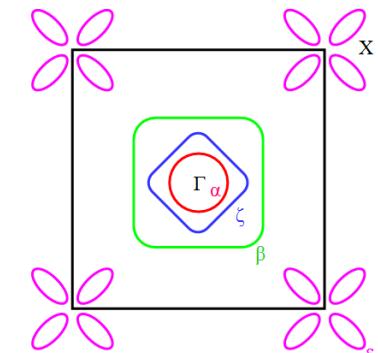
### Angle-dependent interband

$$V_{\zeta\varepsilon}^1 = -0.6 \cdot V_1$$

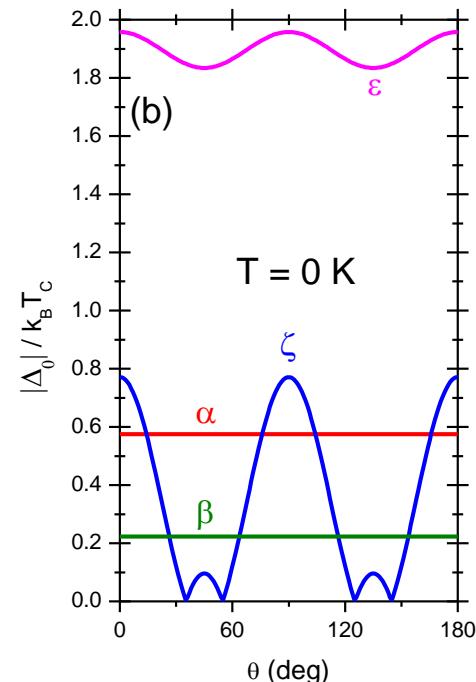
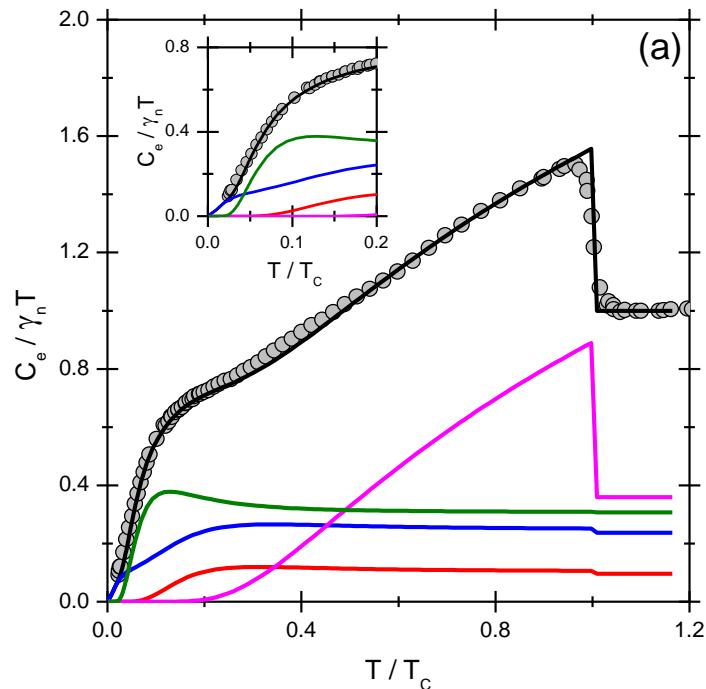
Maiti et al., PRB 85 (2012) 014511

$$V_{ij}(\phi, \phi') = V_{ij}^0 + V_{ij}^1 (\cos 4\phi + \cos 4\phi')$$

$$\Delta_i(\phi, T) = \Delta_i^0(T) + \Delta_i^1(T) \cdot \cos 4\phi$$

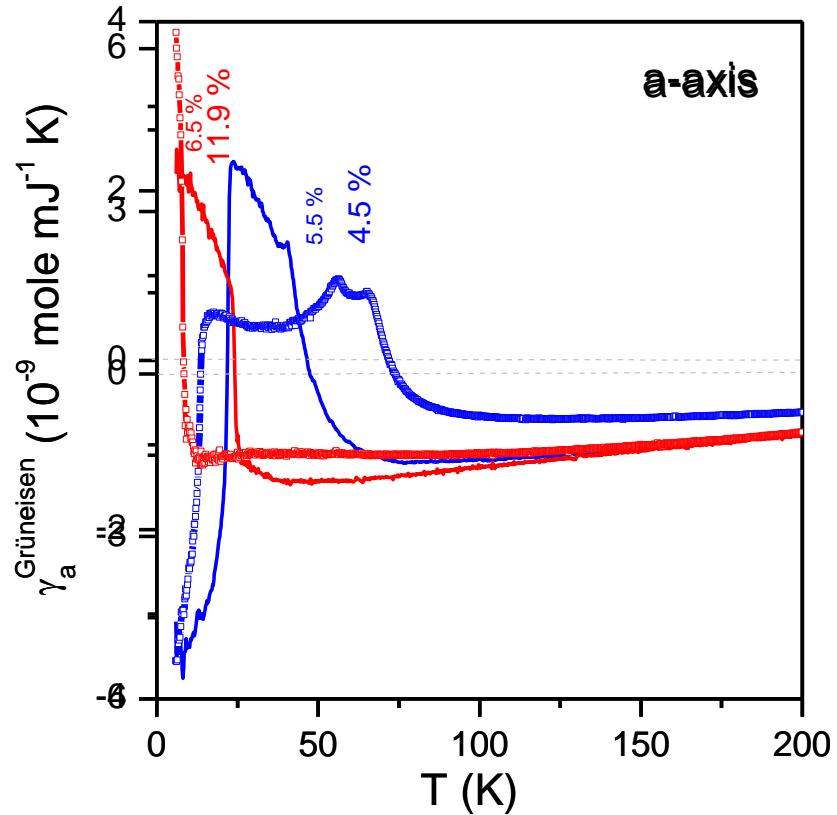
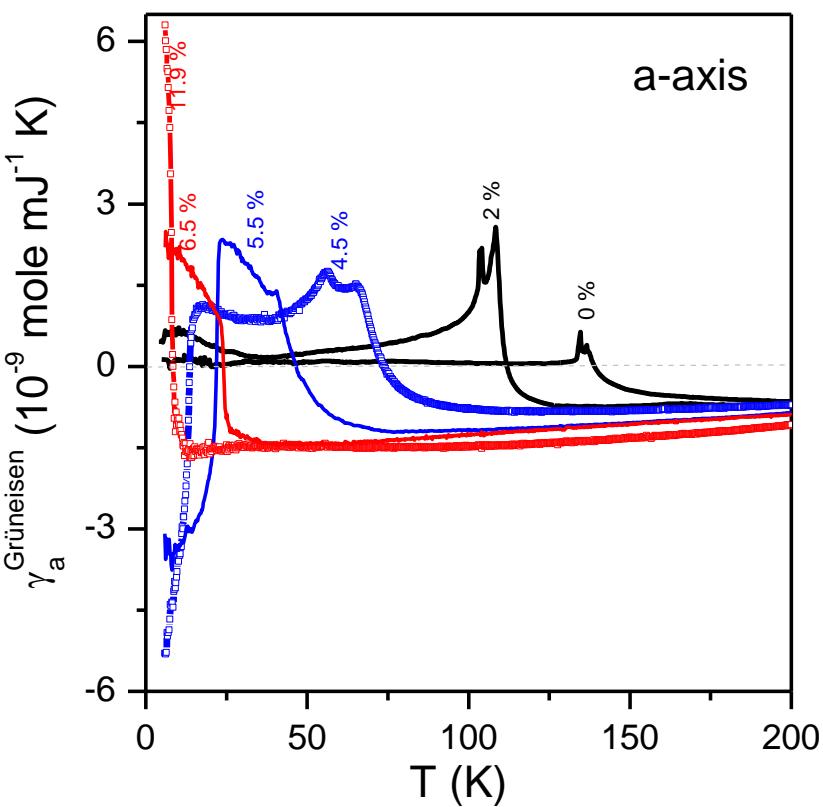


### Enforcing DOS from dHvA/ARPES exp.



# electronic Grüneisen parameter

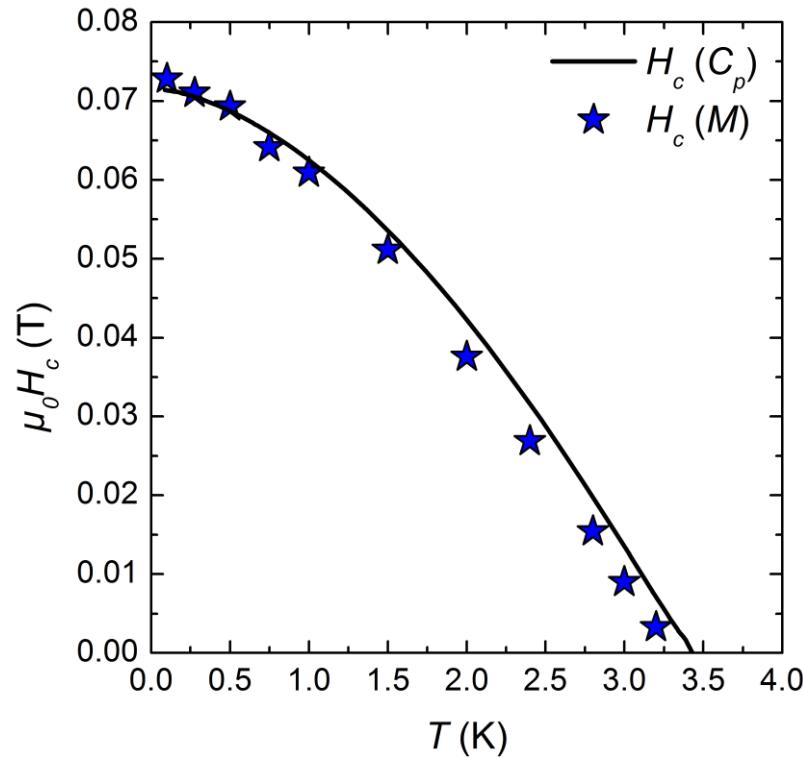
$\alpha_{\text{electronic}}/\text{C}_{\text{electronic}}$



- sign change of Grüneisen parameter at  $T_{\text{SDW}}$  and  $T_c$
- 'diverging' Grüneisen parameter near onset and end of sc dome - new QCPs!
- similar Grüneisen parameters for 5.5% and 6.5 % Co point to an intimate connection between SDW and SC states!

# Thermodynamical critical field from reversible magnetization

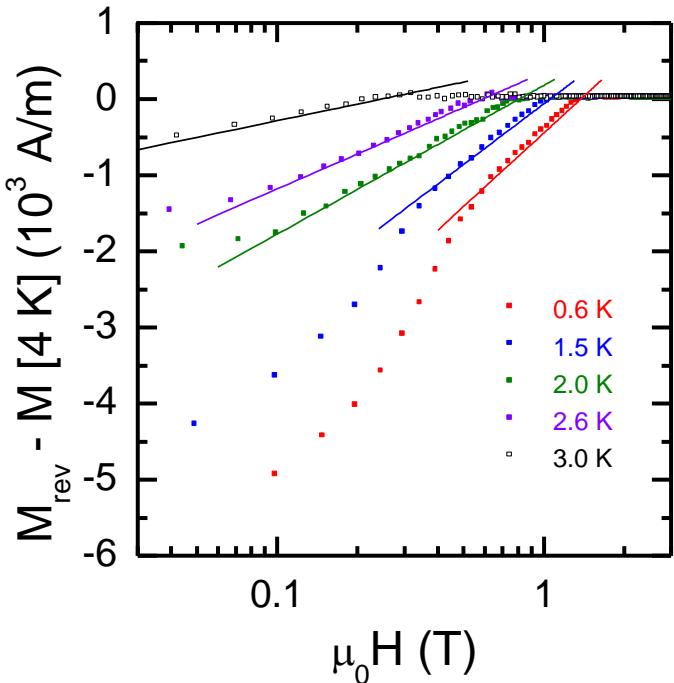
$$\int_0^{H_{c2}} (M_s - M_n) dH = -\frac{H_c^2}{2}$$



- good agreement with  $H_c$  from heat capacity data
- no spurious magnetic contributions in  $C_p$

# Magnetization in the mixed state, $H \parallel c$

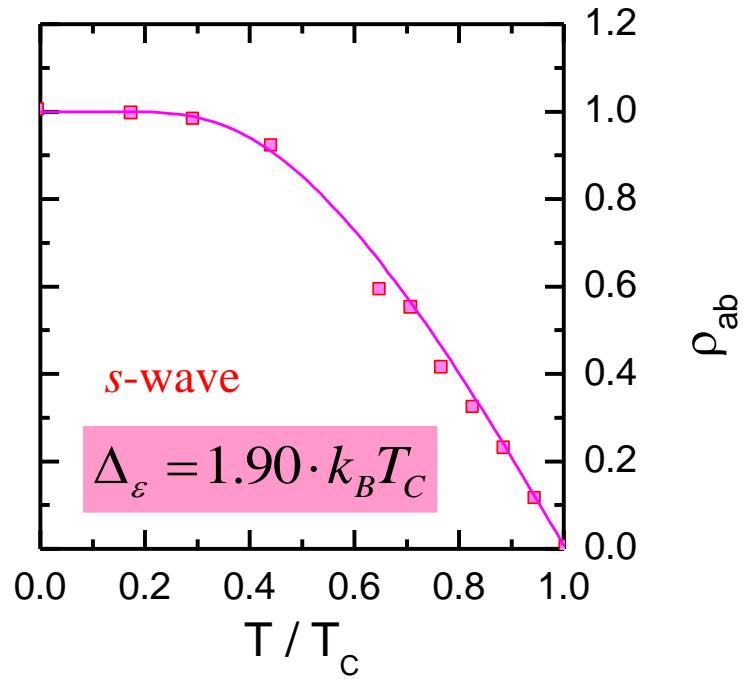
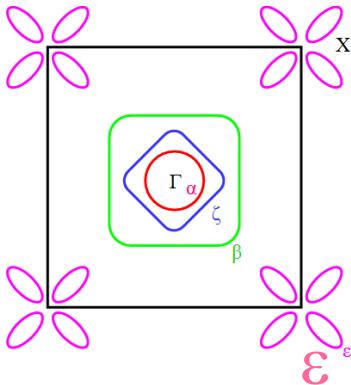
Reversible magnetization



$$H_{C2} > H > H_{C1}$$

$$\mu_0 M = -\frac{\phi_0}{8\pi\lambda_{ab}^2} \ln\left(\beta \frac{H_{C2}}{H}\right)$$

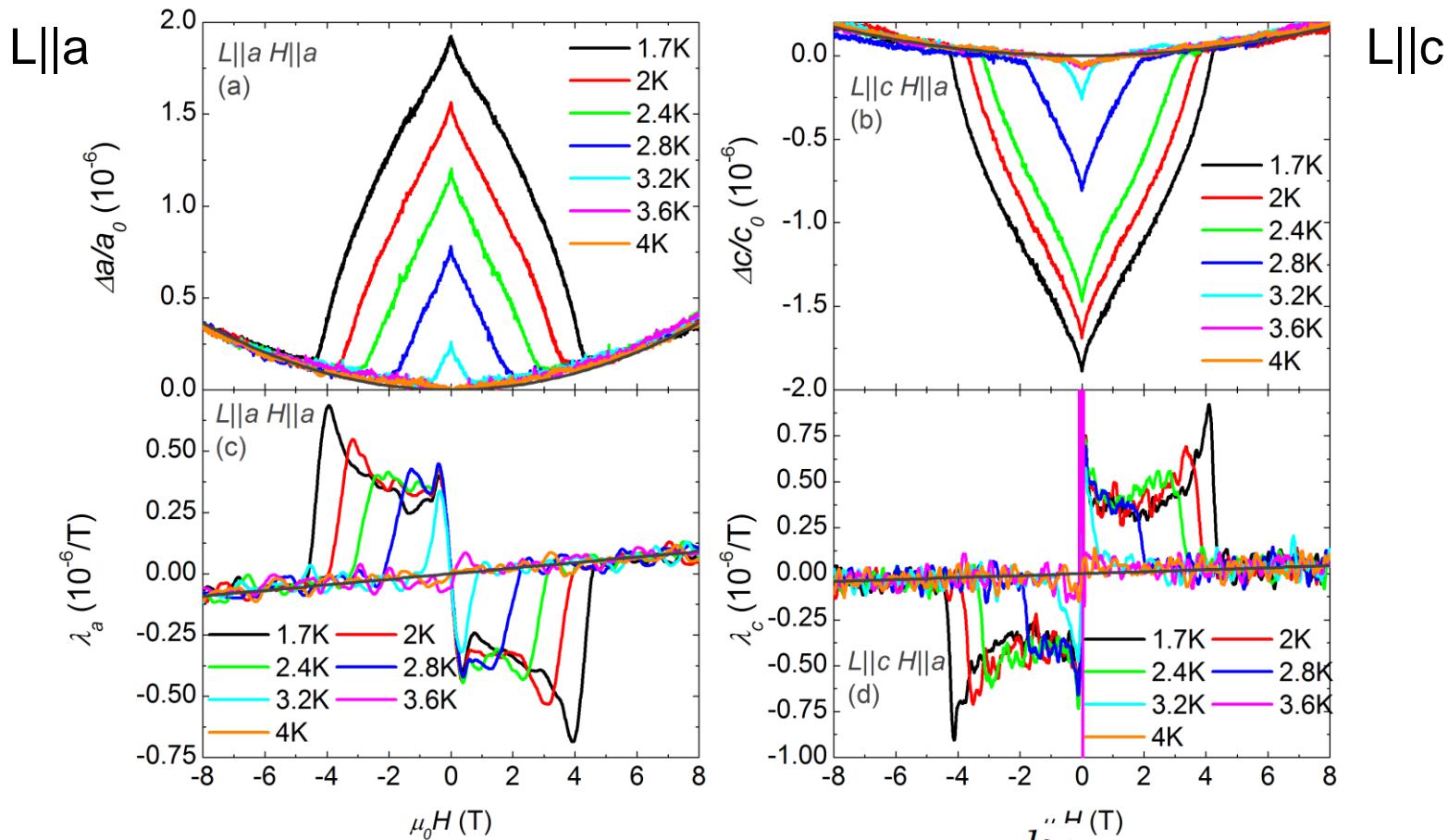
de Gennes, Superconductivity of Metals and Alloys (1966)  
Kogan et al., PRB 38R (1988), 11958



$$\rho_{ab}(T) = \frac{\lambda_{ab}^2(0)}{\lambda_{ab}^2(T)}$$

Near  $H_{C2}$ : only sensitive to the large gap because vortices related with small gaps have already overlapped

# Magnetostriction measurements: $H \parallel a$



- paramagnetic signal:

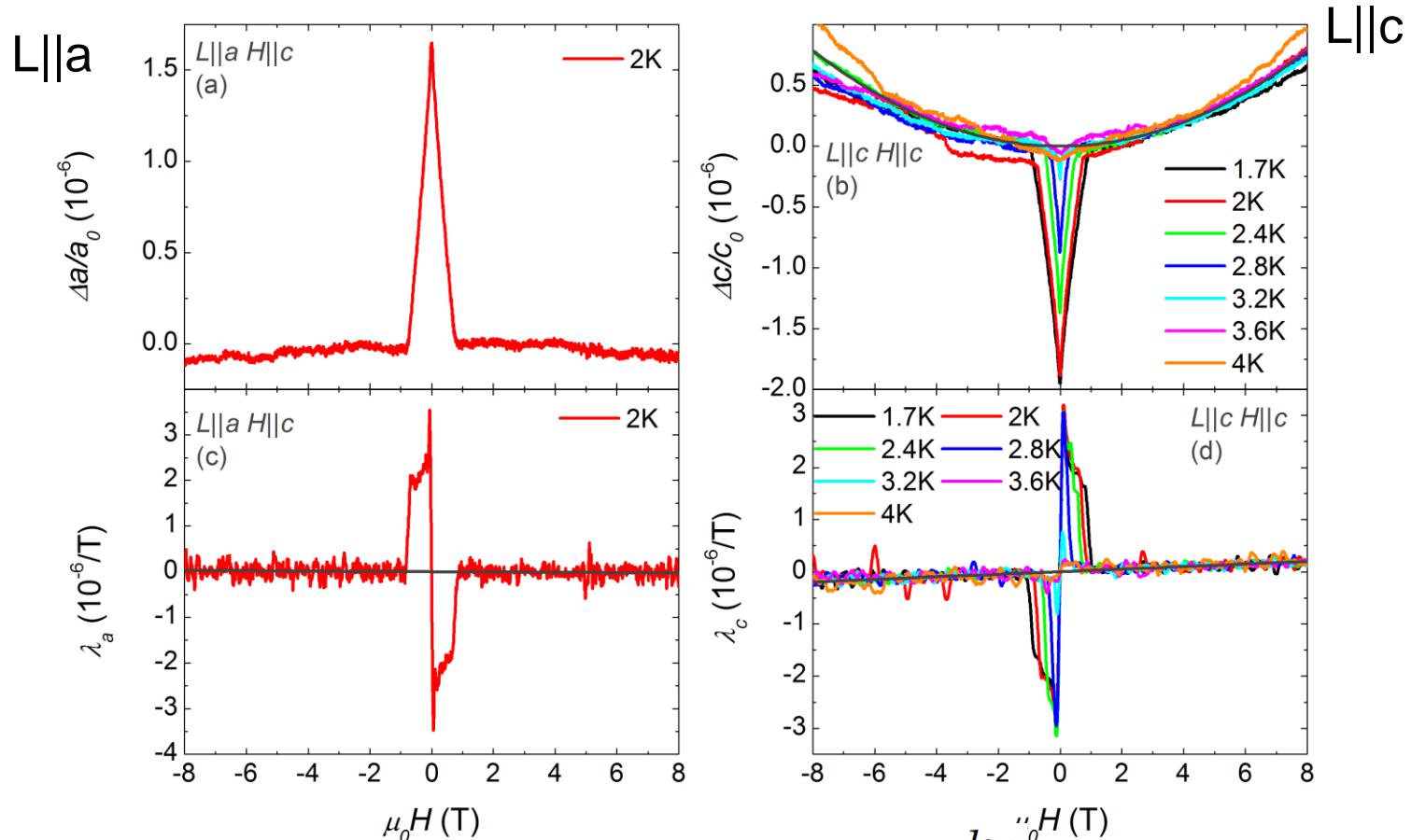
$$\frac{d\chi}{dp_i}$$

- strong Pauli limiting for  $H \parallel a$

-  $d\kappa/dp_i \ll dH_c/dp_i$

$$\frac{dH_c}{dp_i}$$

# Magnetostriction measurements: $H \parallel c$



- paramagnetic signal:

$$\frac{d\chi}{dp_i}$$

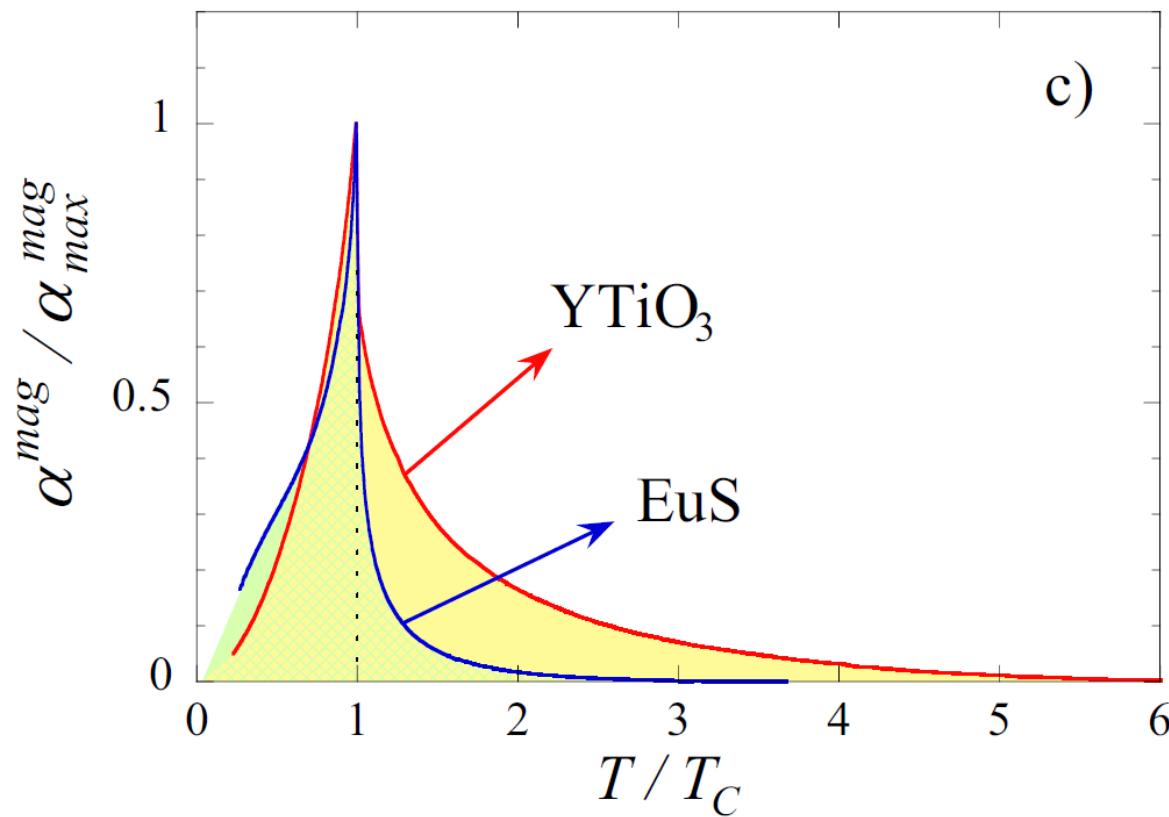
- weak Pauli limiting for  $H \parallel c$

-  $d\kappa/dp_i \ll dH_c/dp_i$

$$\frac{dH_c}{dp_i}$$

**Ferromagnetism and lattice distortions in the perovskite  $\text{YTiO}_3$** 

W. Knafo,<sup>1,2,3</sup> C. Meingast,<sup>1</sup> A. V. Boris,<sup>4,5</sup> P. Popovich,<sup>4</sup> N. N. Kovaleva,<sup>4,5</sup> P. Yordanov,<sup>4</sup> A. Maljuk,<sup>4,6</sup> R. K. Kremer,<sup>4</sup> H. v. Löhneysen,<sup>1,2</sup> and B. Keimer<sup>4</sup>



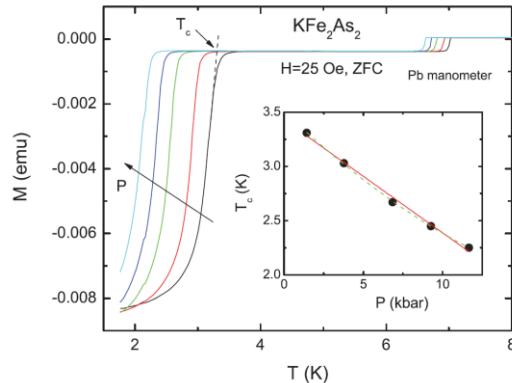
# Pressure dependencies

Pressure along	$d\gamma_n/dp_i$ [mJ/mol K <sup>2</sup> GPa]	$dT_c/dp_i$ [K/GPa]	$dH_c/dp_i$ [T/GPa]	$d\chi^a/dp_i$ [1/GPa]	$d\chi^c/dp_i$ [1/GPa]
a-axis	-7.7	-1.9	-0.049	$-1.4 \times 10^{-5}$	$4.1 \times 10^{-6}$
c-axis	-4.81	2.10	0.046	$-6.7 \times 10^{-6}$	$-3.0 \times 10^{-5}$

$$dT_c/dP \approx -1 \text{ K/GPa}$$

$$dT_c/dp_c \approx +1.1 \text{ K/GPa}$$

- superconductivity couples strongly to c/a ratio  
(opposite sign for Co-Ba122)  
normal state less anisotropic
- fair agreement with Bud'ko et al.



Bud'ko et al. PRB **86**, 224514 (2012)

# Normalized pressure dependencies

[1/GPa]	$1/\gamma_n \frac{d\gamma_n}{dp_i}$	$1/T_c \frac{dT_c}{dp_i}$	$1/H_c H_c \frac{dH_c}{dp_i}$	$1/X^a \frac{dX^a}{dp_i}$	$1/X^c \frac{dX^c}{dp_i}$
a-axis	-0.076	-0.56	-0.71	-0.035	0.013
c-axis	-0.047	0.61	0.66	-0.016	-0.096
volume	-0.20	-0.51	-0.75	-0.086	-0.070

- largest relative pressure effects:  $T_c$  and  $H_c$
- $T_c$  and  $H_c$  closely related
- $\gamma$  and  $\chi$  much smaller
- detailed analysis complicated due to multiband nature  
(too many parameters)

# Volume Grüneisen parameters

B = 50 GPa (DFT, Rolf Heid)

	- $d\ln\gamma_n/d\ln V$	- $d\ln T_c/d\ln V$	- $d\ln H_c/d\ln V$	- $d\ln\chi^a/d\ln V$	- $d\ln\chi^c/d\ln V$
volume	- 8.9	- 23	- 34	- 3.9	- 3.1

## classical superconductors

	- $d\ln T_c/d\ln V$	- $d\ln\gamma/d\ln V$
Al	-17	-1.8
Pb	-3	-1.7
Nb	0	-1.5

Boughton, Olsen, Palmy 1970

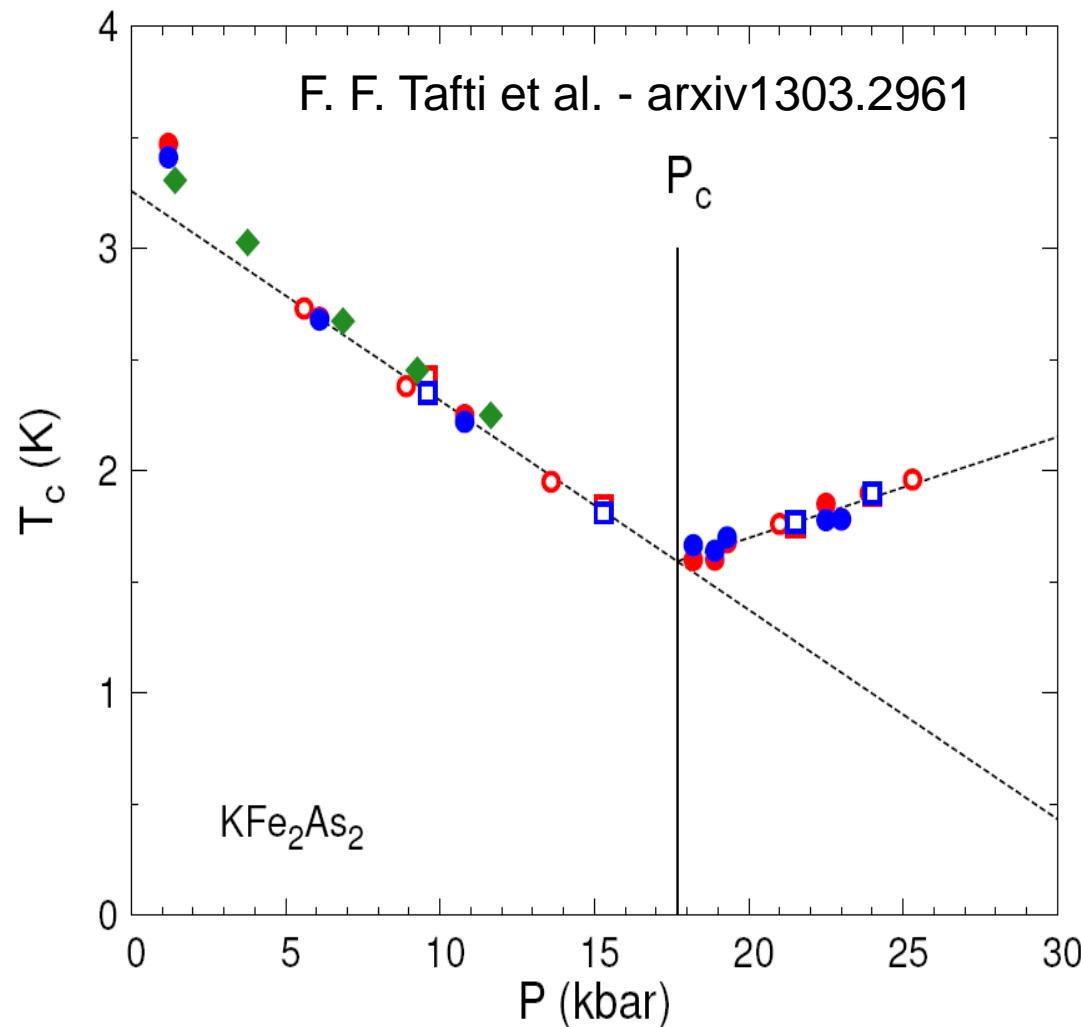
## U-based superconductors

	- $d\ln T_c/d\ln V$	- $d\ln\gamma/d\ln V$
UPt <sub>3</sub>	- 65	- 50
URu <sub>2</sub> Si <sub>2</sub>	- 59	- 40
UBe <sub>13</sub>	- 21	- 52

J. Flouquet et al. Physica C, 1991

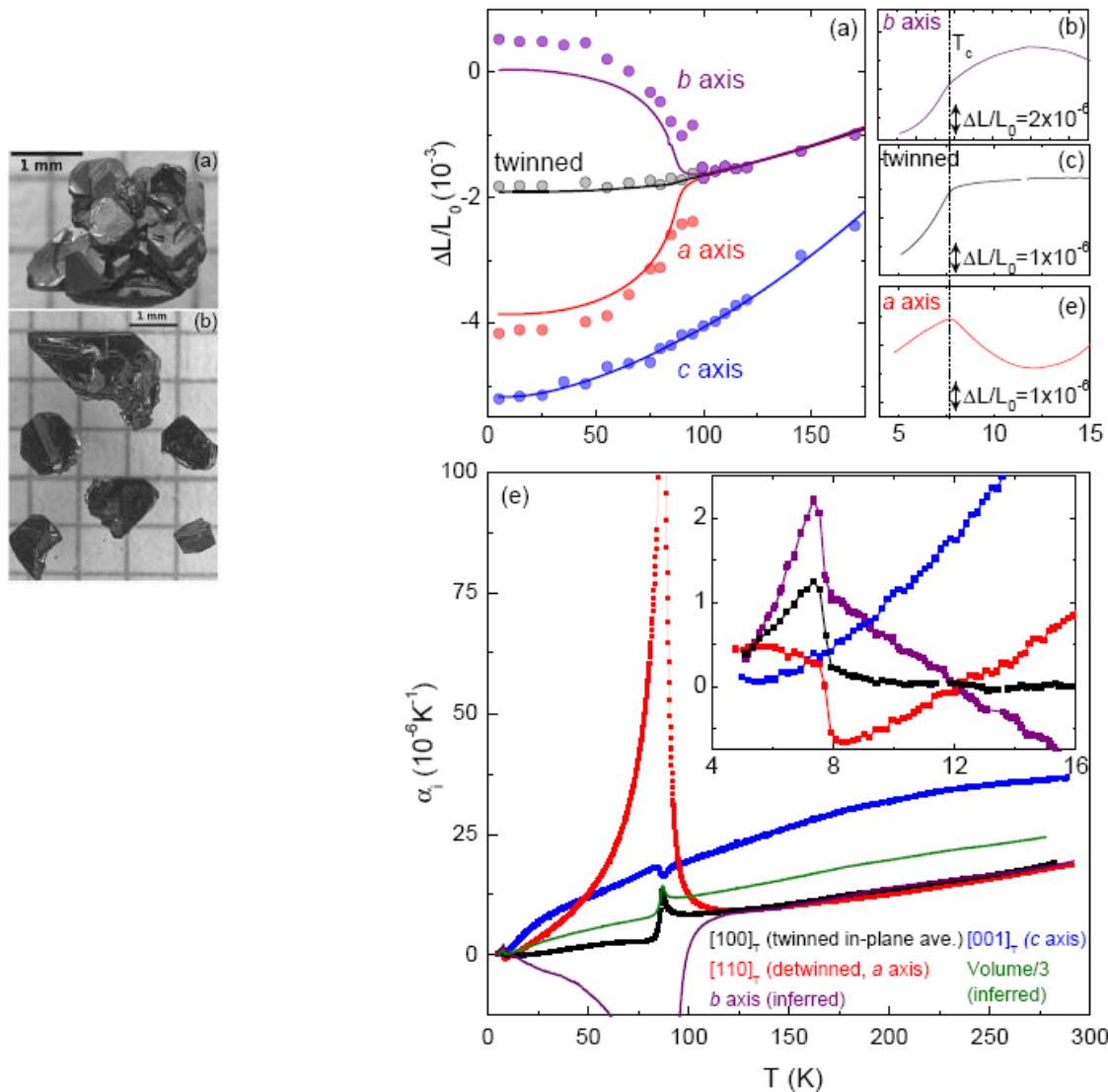
- same signs of  $T_c$  and  $\gamma$  Grüneisen parameters as other SC's
- intermediate absolute values of Grüneisen parameters
- does not match trend with Ba doping ( $T_c$  increases,  $\gamma$  decreases)

# change of pairing symmetry under pressure?

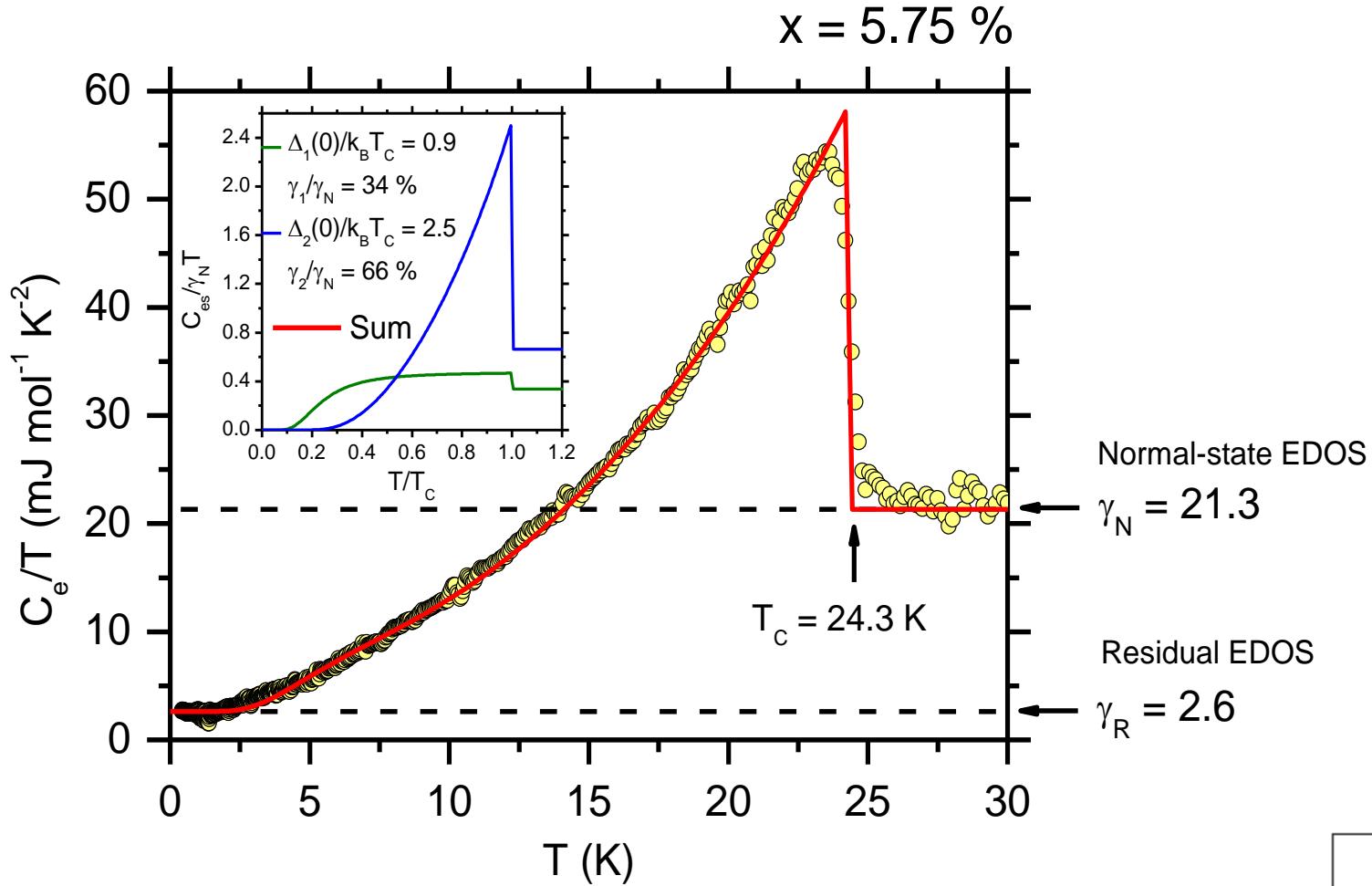


# Uniaxial pressure effects in FeSe

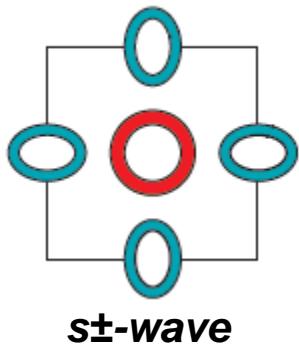
Anna Böhmer et al. arxiv 1303.2026v1

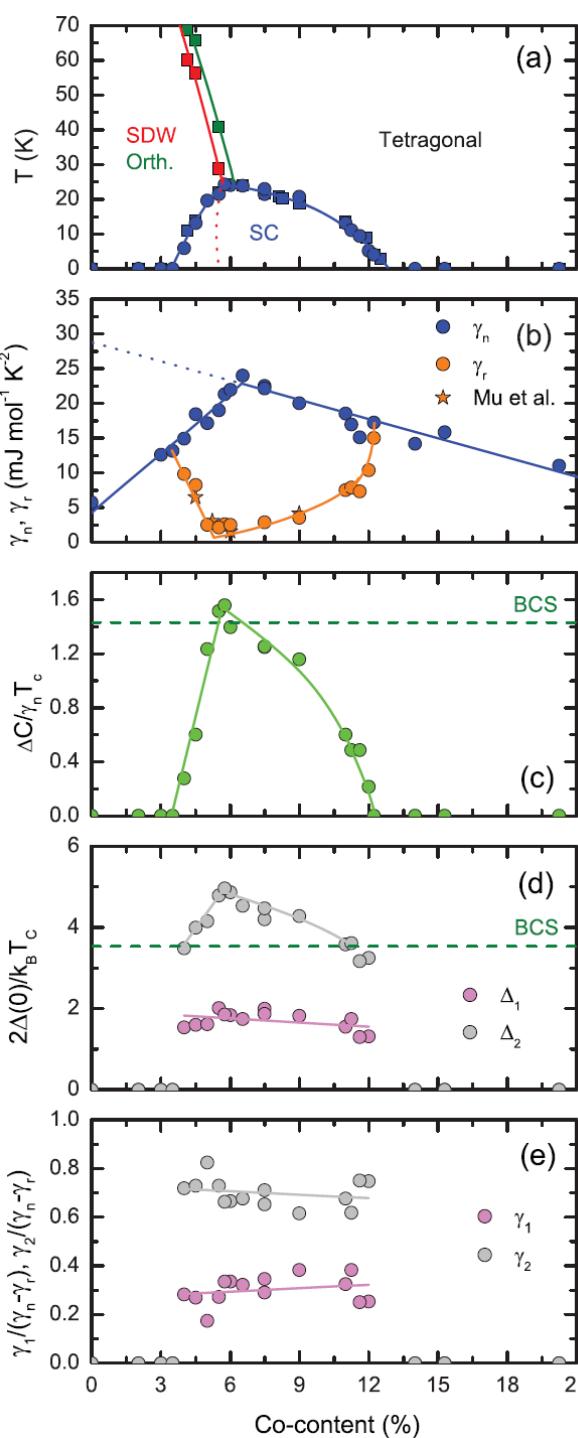


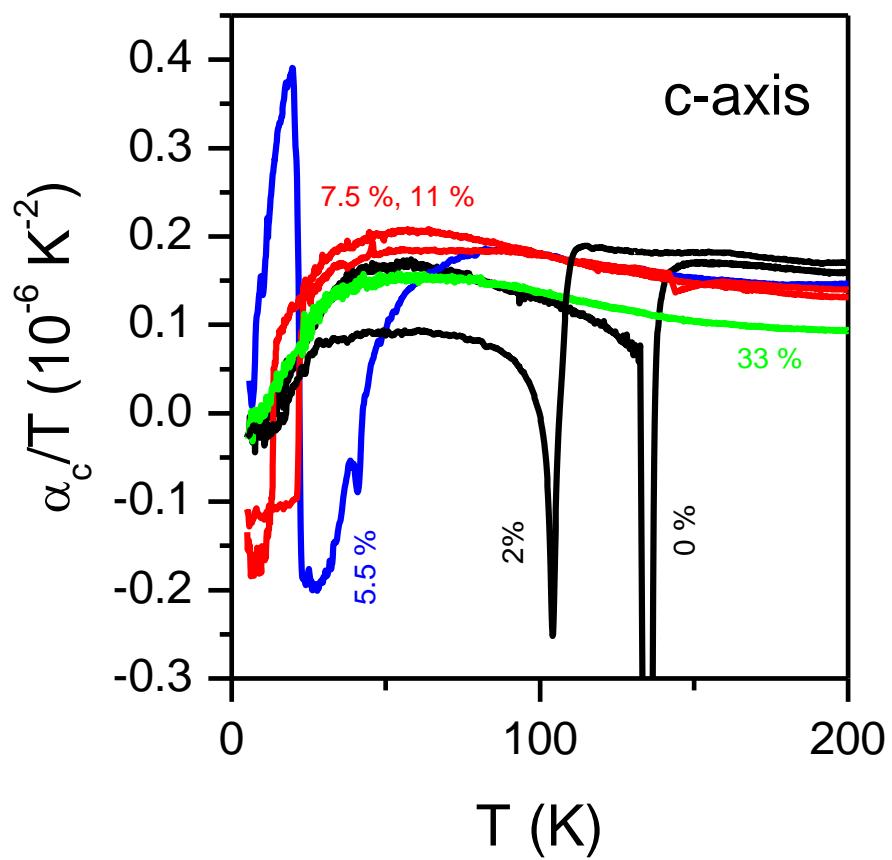
# Two gap (s-wave) Analysis



- two s-wave gaps provide very good fit of data
- consistent with proposed s+- state

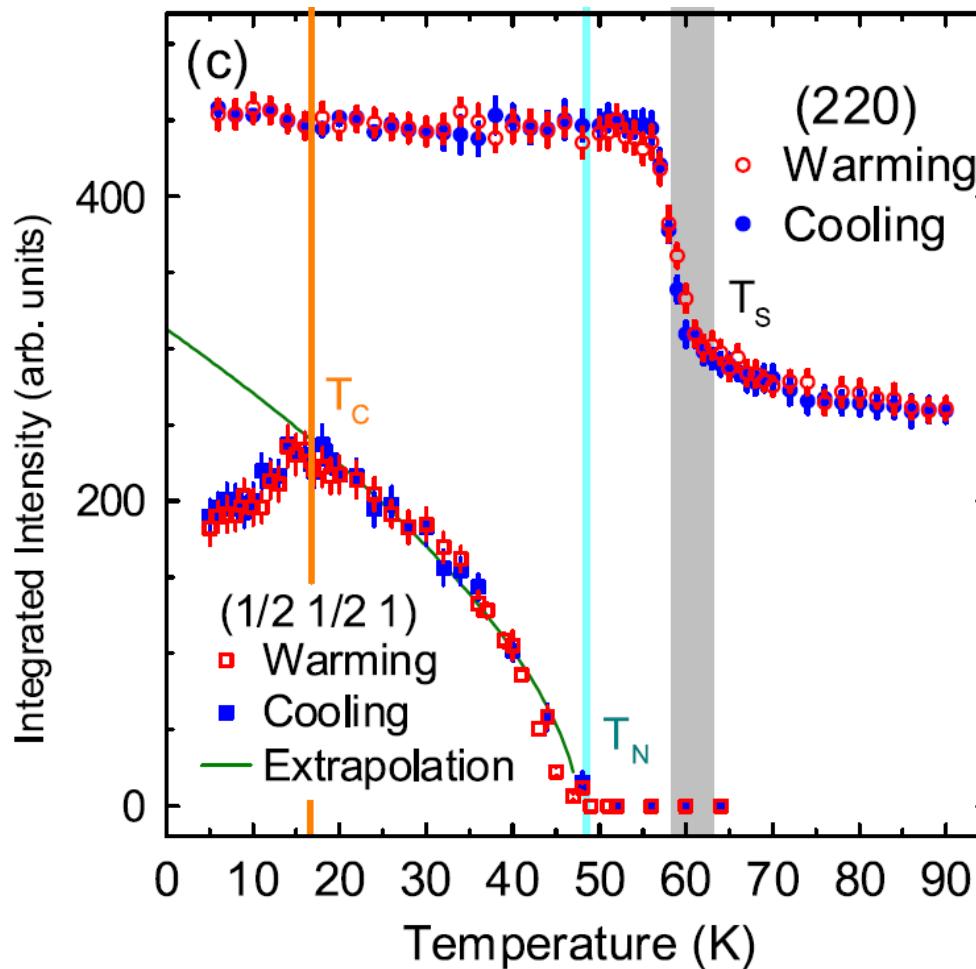






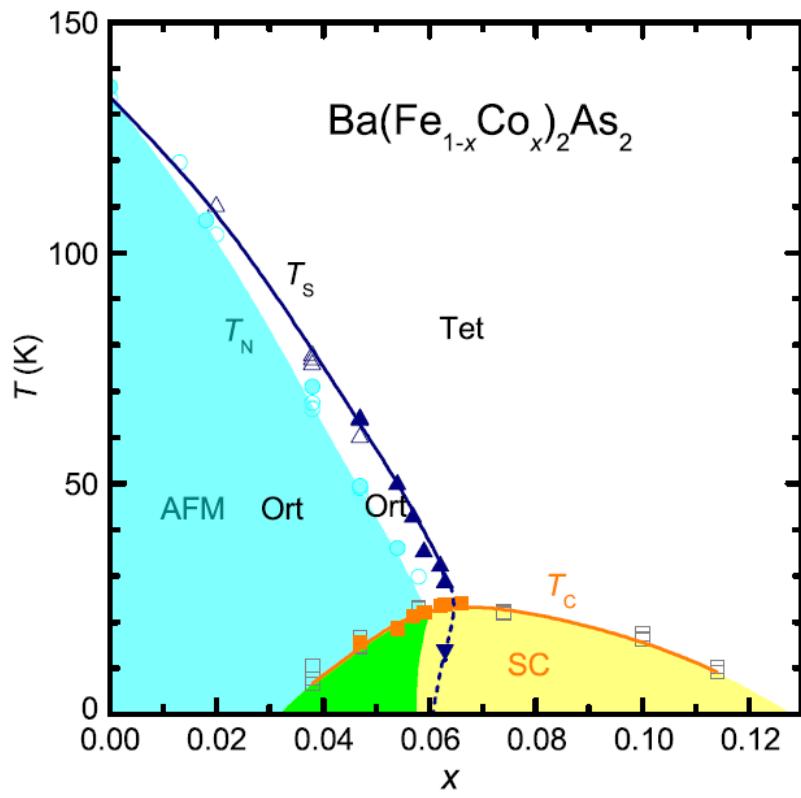
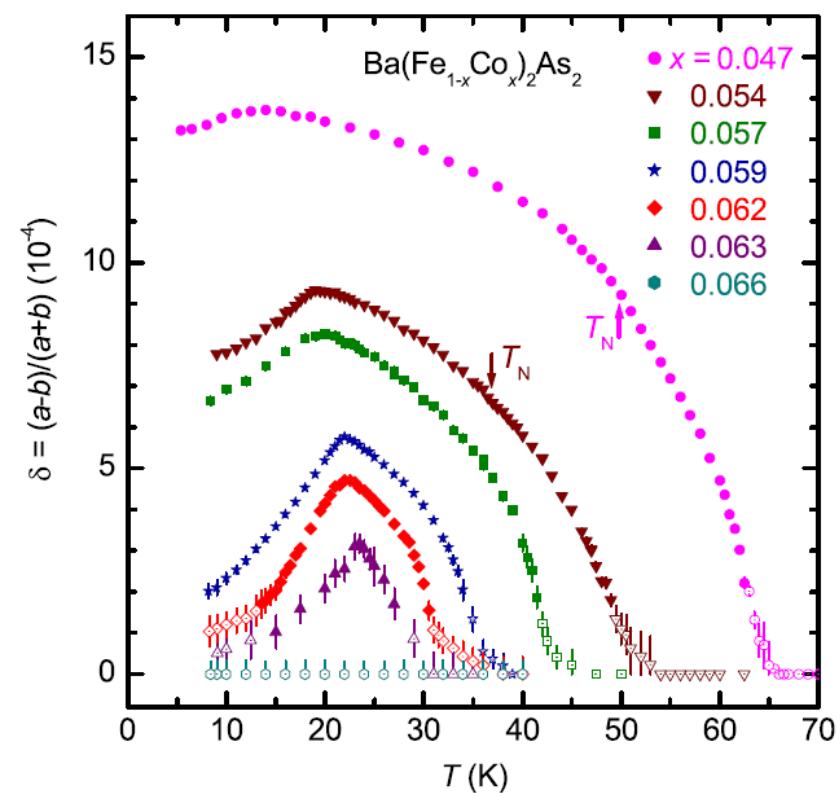
# Coexistence of Competing Antiferromagnetic and Superconducting Phases in the Underdoped Ba(Fe<sub>0.953</sub>Co<sub>0.047</sub>)<sub>2</sub>As<sub>2</sub> Compound Using X-ray and Neutron Scattering Techniques

D. K. Pratt, W. Tian, A. Kreyssig, J. L. Zarestky, S. Nandi, N. Ni, S. L. Bud'ko, P. C. Canfield,  
A. I. Goldman, and R. J. McQueeney



# Anomalous Suppression of the Orthorhombic Lattice Distortion in Superconducting $\text{Ba}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$ Single Crystals

S. Nandi, M. G. Kim, A. Kreyssig, R. M. Fernandes, D. K. Pratt, A. Thaler, N. Ni, S. L. Bud'ko, P. C. Canfield, J. Schmalian, R. J. McQueeney, and A. I. Goldman\*



# Specific heat and thermal expansion

Gibbs free energy:

$$G = U - TS + pV$$

specific heat:

$$C_p = \left. \frac{dQ}{dT} \right|_p = -T \left( \frac{\partial^2 G}{\partial T^2} \right) = T \left. \frac{dS}{dT} \right|_p$$

Volume thermal expansion:

$$\beta = \frac{1}{V} \left. \frac{dV}{dT} \right|_p = \frac{1}{V} \left. \frac{\partial^2 G}{\partial P \partial T} \right|_T = \kappa_T \left. \frac{dS}{dV} \right|_T$$

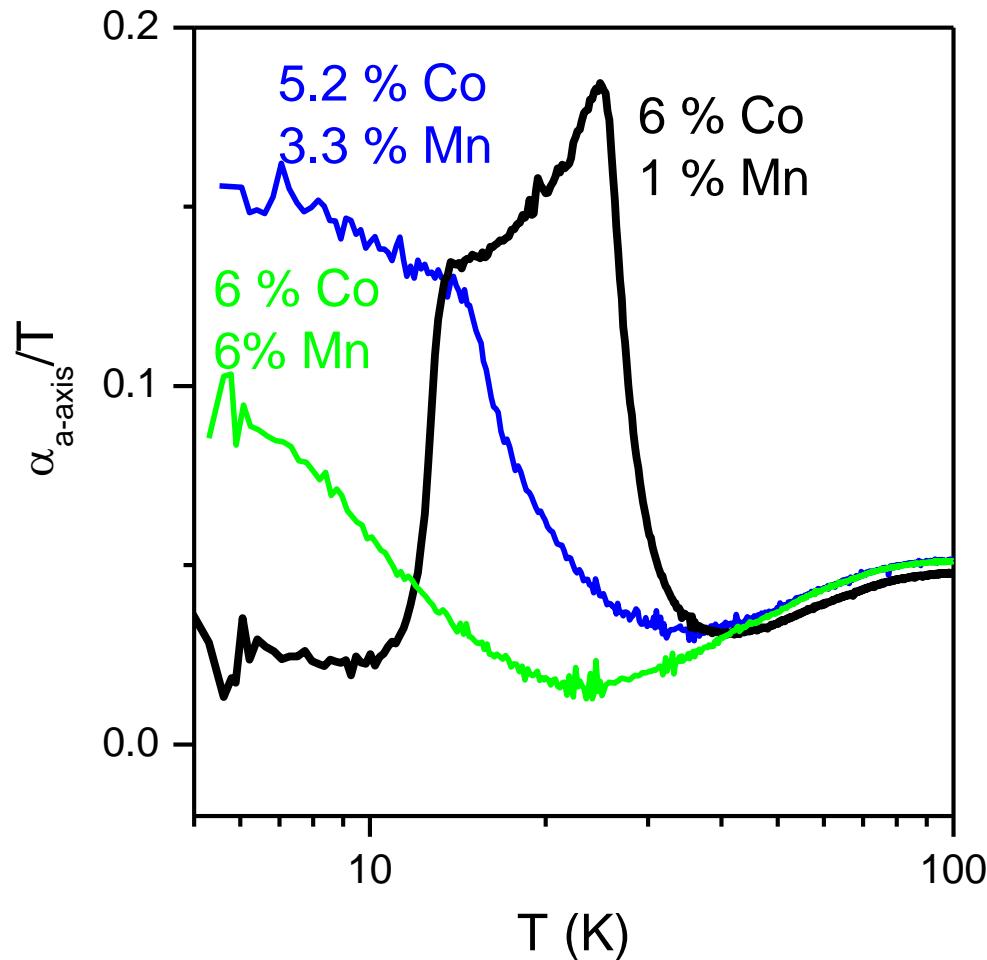
- for superconductors

- bulk superconductivity?
- Sommerfeld coefficient
- nature of energy gap  
(s, d, ...multigap)
- strong or weak coupling?

- pressure dependences (uniaxial!)
- Grüneisen parameter
- Ehrenfest Relation:

$$\frac{dT_c}{dp_i} = \frac{\Delta \alpha_i V_m}{\Delta C_p / T_c}$$

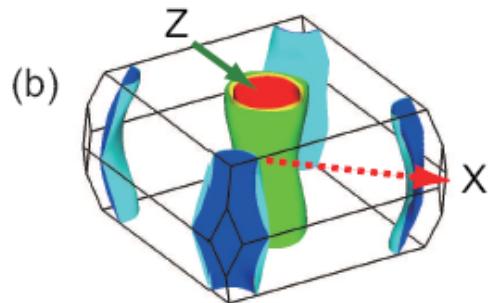
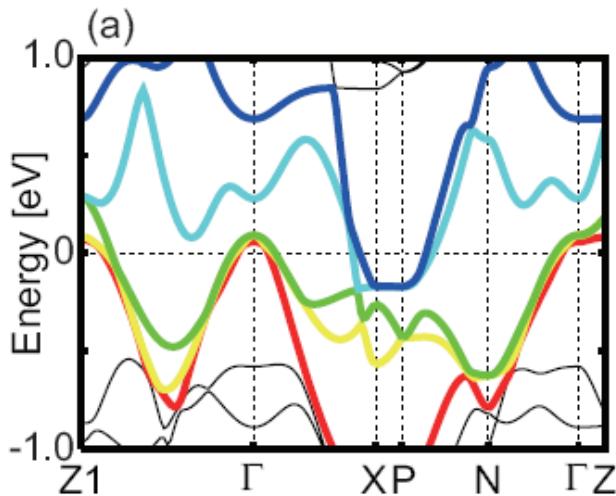
# Suppression of superconducting dome in $\text{Ba}(\text{Fe}_{0.94-x}\text{Co}_{0.06}\text{Mn}_x)_2\text{As}_2$



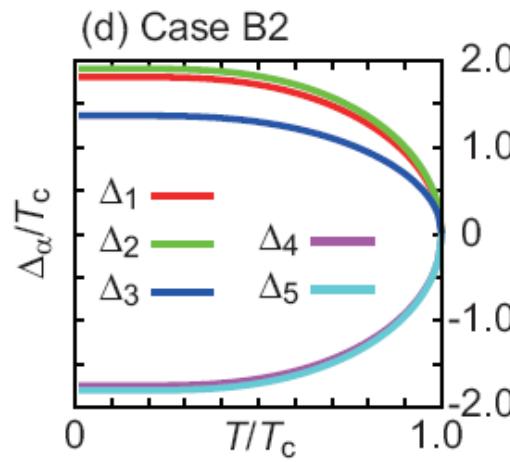
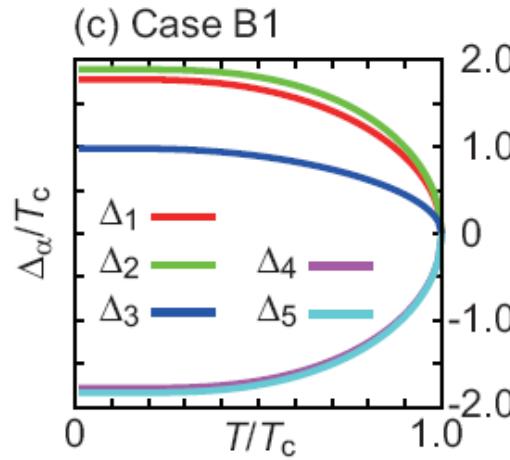
# First-Principles Calculations + Eliashberg

First-principles-based  $\pm s$ -wave modelling for iron-based superconductors: Studies for specific heat and nuclear magnetic relaxation rate

N. Nakai,<sup>1, 2,\*</sup> H. Nakamura,<sup>1, 2, 3</sup> Y. Ota,<sup>1, 2</sup> Y. Nagai,<sup>3, 4</sup> N. Hayashi,<sup>1, 5</sup> and M. Machida<sup>1, 2, 3</sup>



$$N_1 : N_2 : N_3 : N_4 : N_5 = 0.393 : 0.642 : 0.490 : 0.420 : 0.384$$

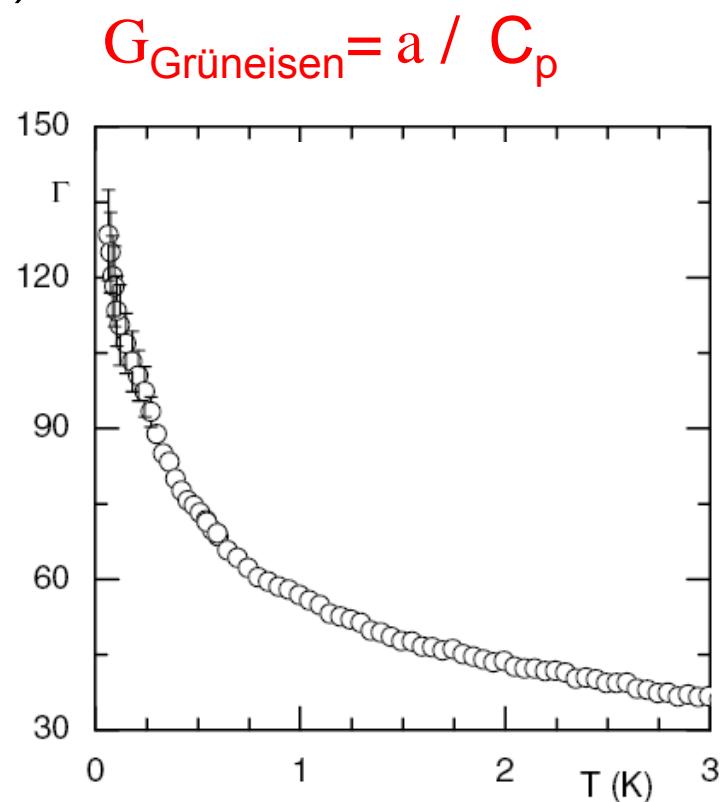
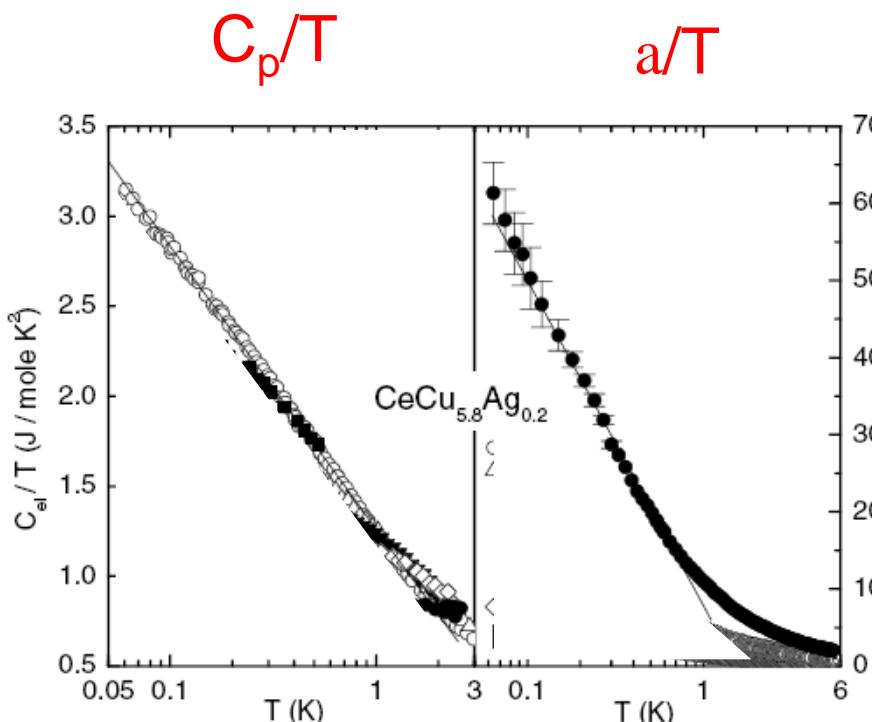


# Grüneisen parameter at a QCP?

$$\Gamma = \frac{3\alpha V_{mol}}{C_p K_S}$$

phonons       $\Gamma = -\frac{V}{\omega_{Debye}} \frac{\partial \omega_{Debye}}{\partial V} \approx const.$

**CeCuAg:** Küchler *et al.* PRL 93 (2004)

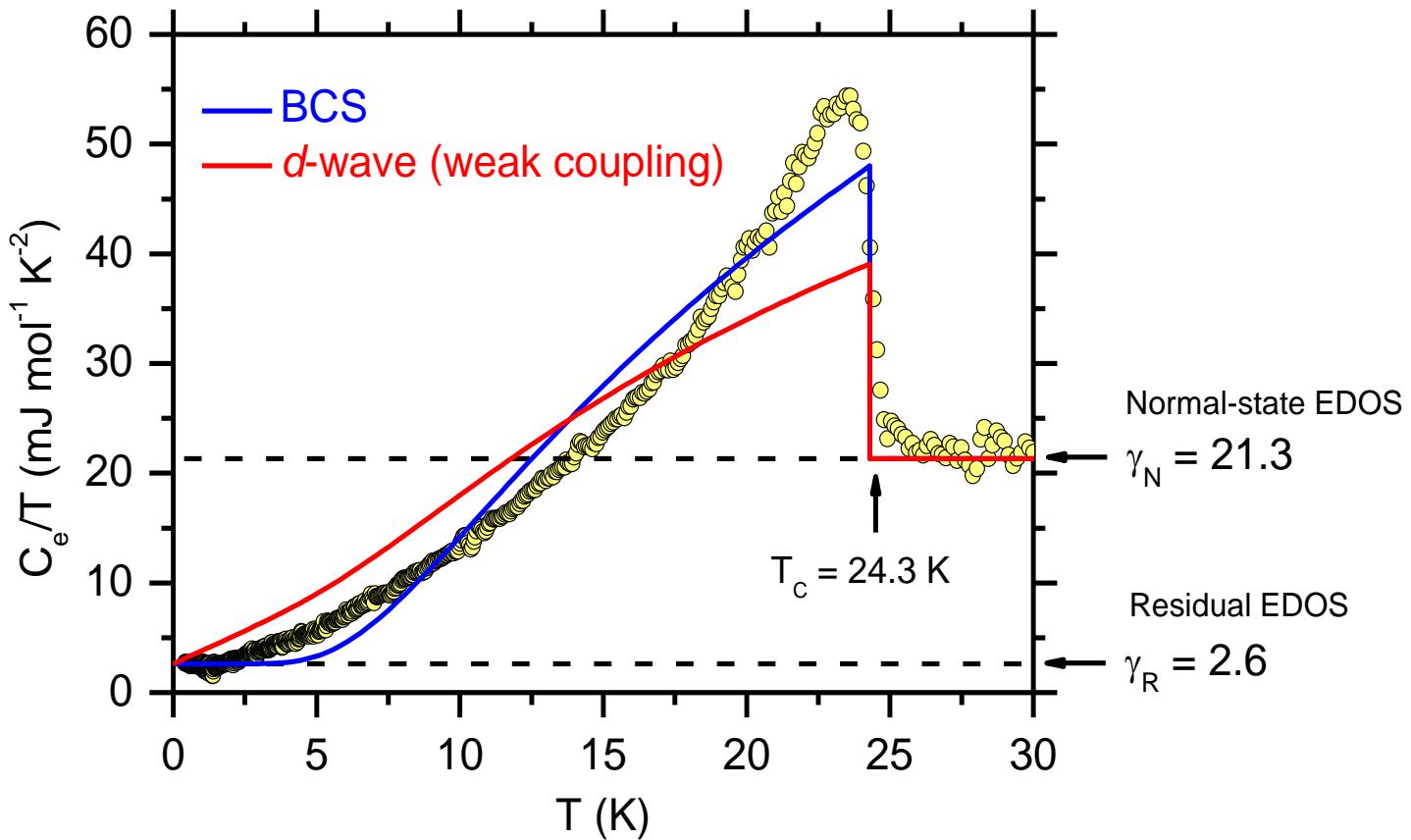


# electronic specific heat of $\text{Ba}(\text{Fe},\text{Co})_2\text{As}_2$

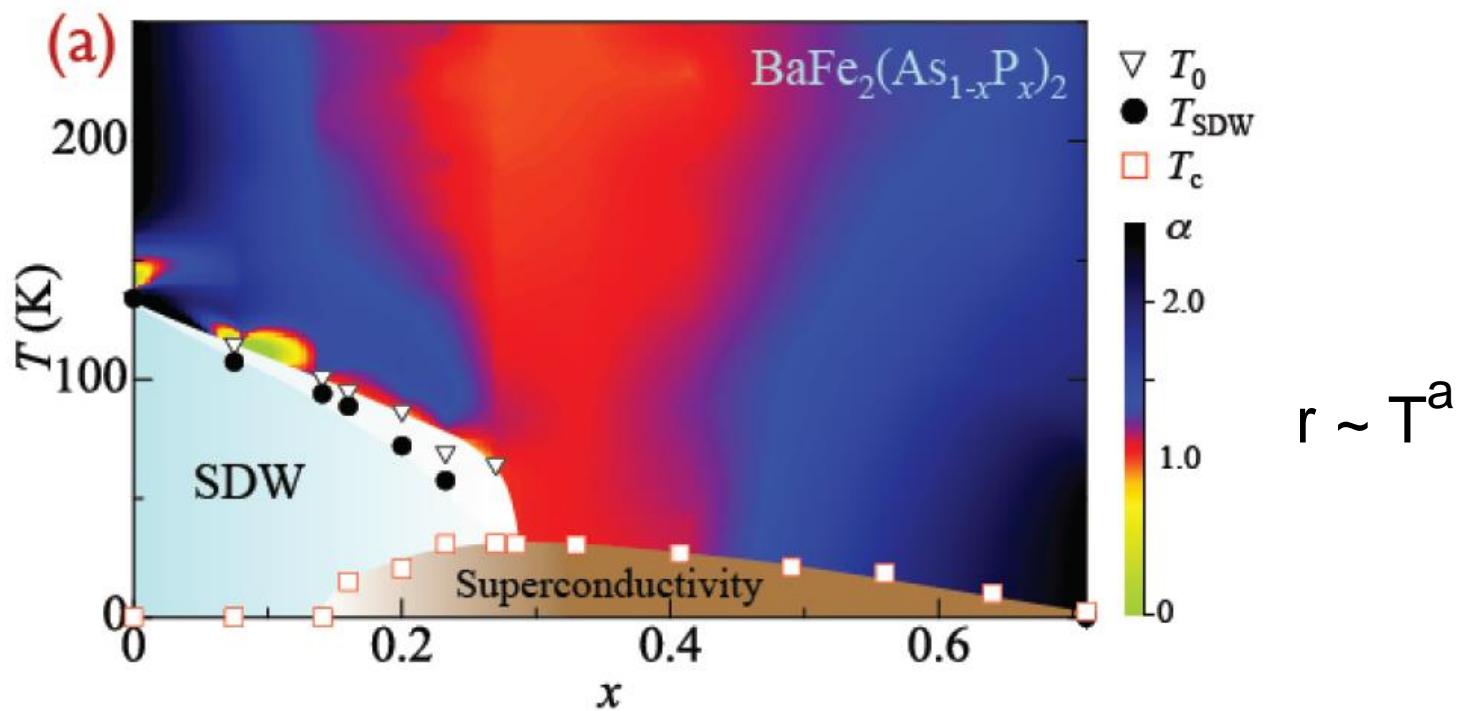
F. Hardy et al., PRB 81 (2010)

060501(R)

$x = 5.75 \%$



- some residual electronic term at low  $T$  (need to measure below 2 K!!)
- simple single-band  $d$ -wave or  $s$ -wave fits do not work

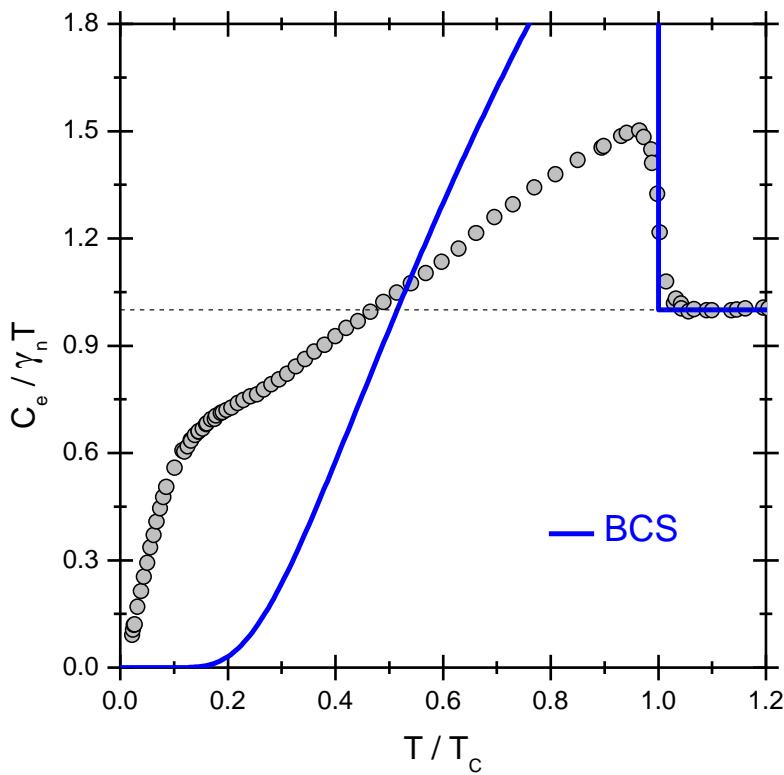


- nearly linear resistivity at optimal doping!
- similar behavior found in cuprates and heavy fermions
- need thermodynamic data showing non-Fermi liquid behavior**

# Superconducting state

$\text{KFe}_2\text{As}_2$

Hardy et al., unpublished

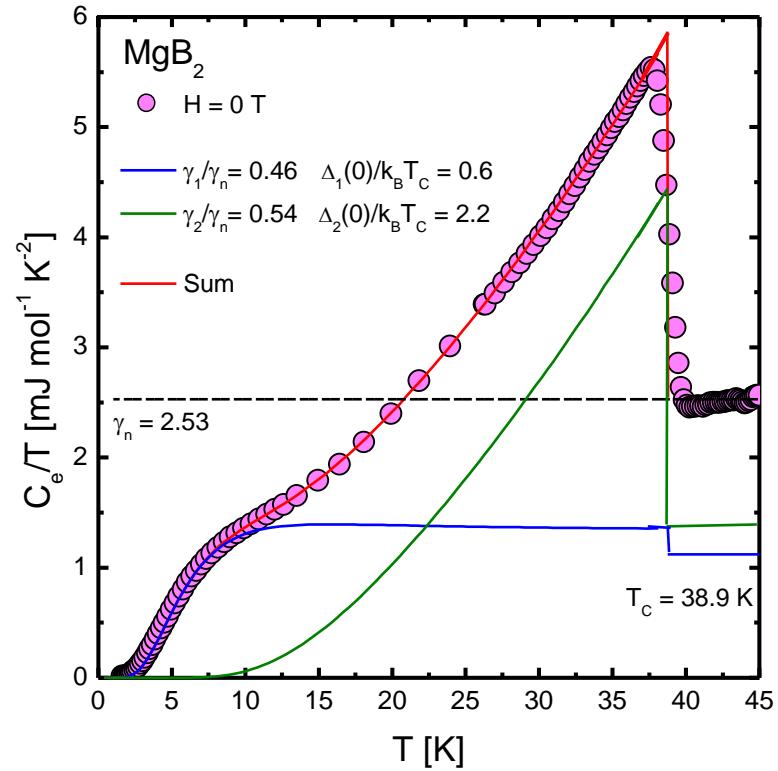


$$T_c = 3.4 \text{ K}$$

$$\gamma_n = 102 \text{ mJ mol}^{-1} \text{ K}^{-2}$$

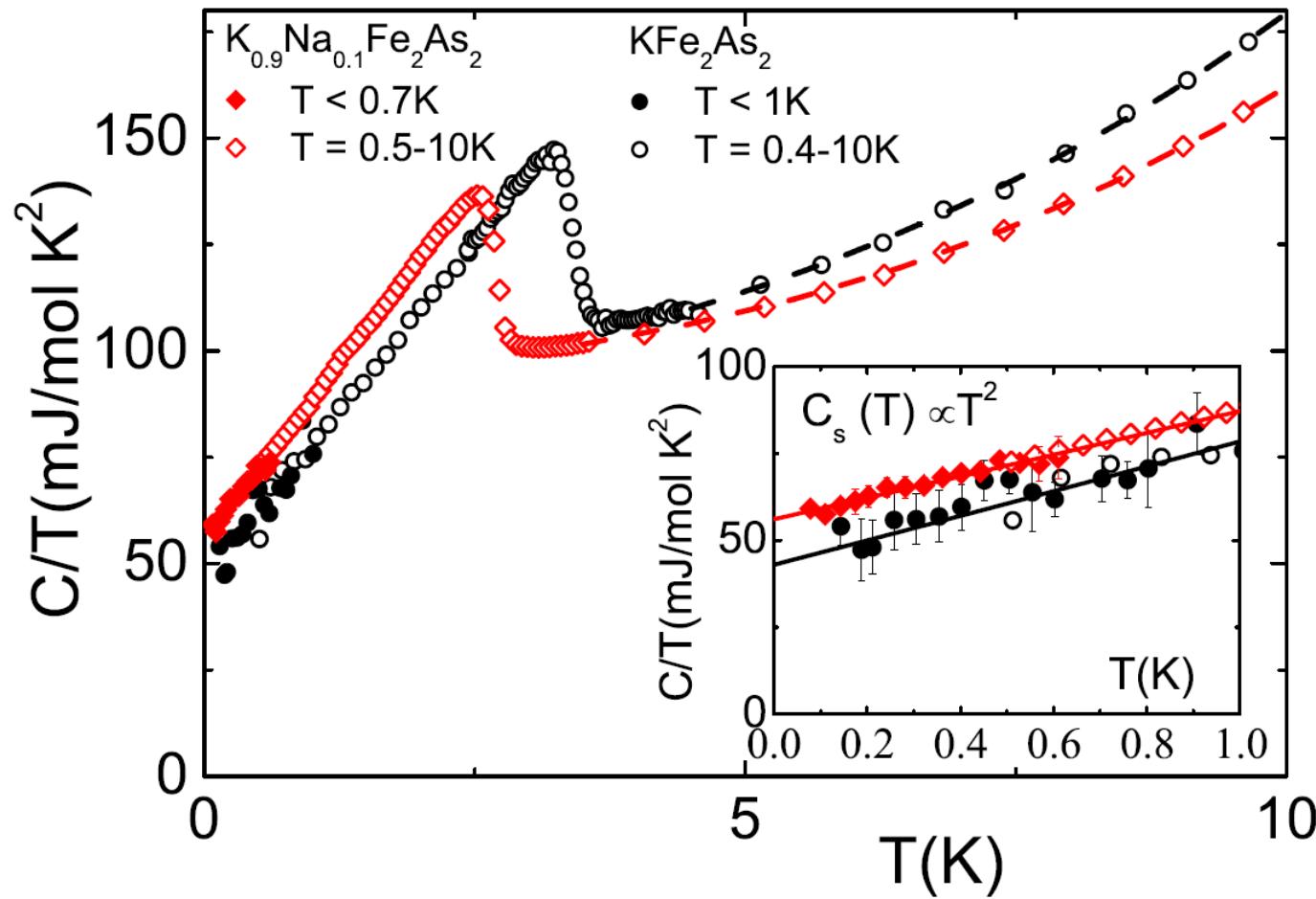
$\text{MgB}_2$

Bouquet et al., PRL 109 (2012) 087001

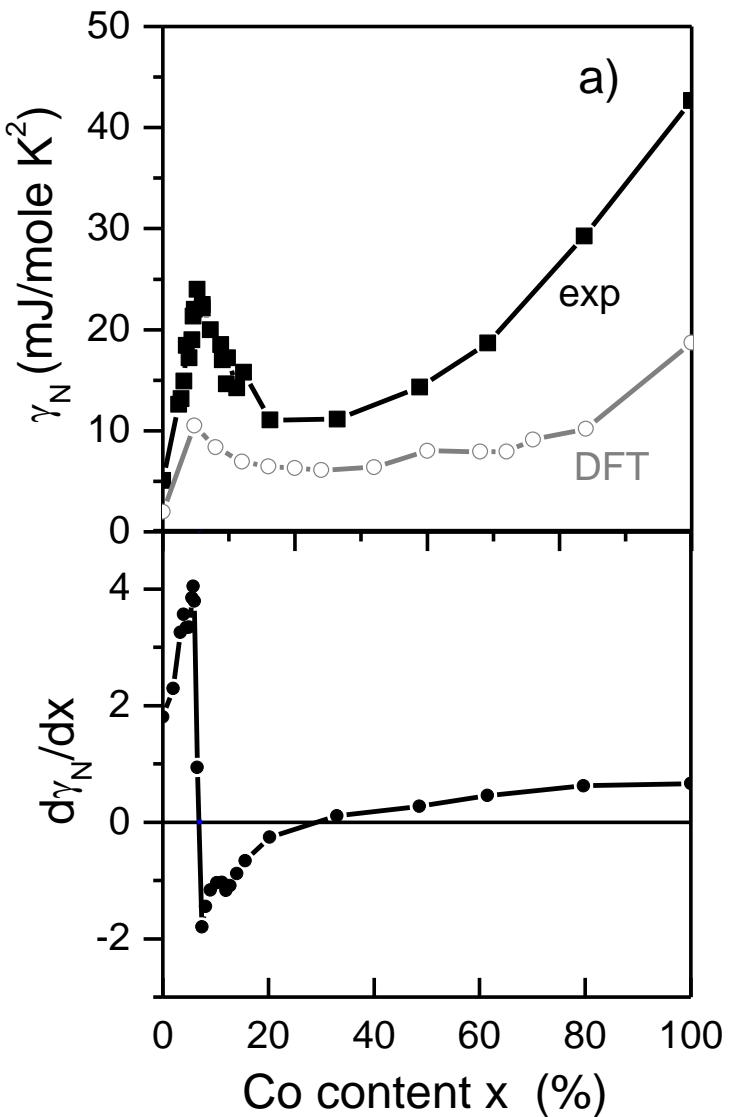
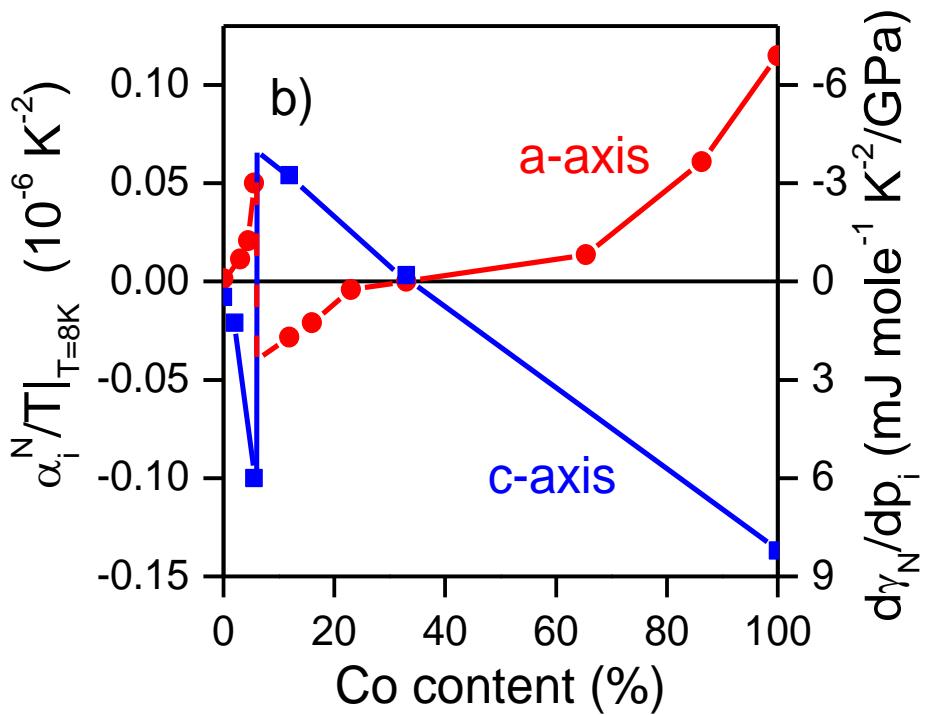


$$T_c = 39 \text{ K}$$

$$\gamma_n = 2.5 \text{ mJ mol}^{-1} \text{ K}^{-2}$$



$$\frac{\alpha_i}{T} = -\frac{d\gamma}{dP_i}$$

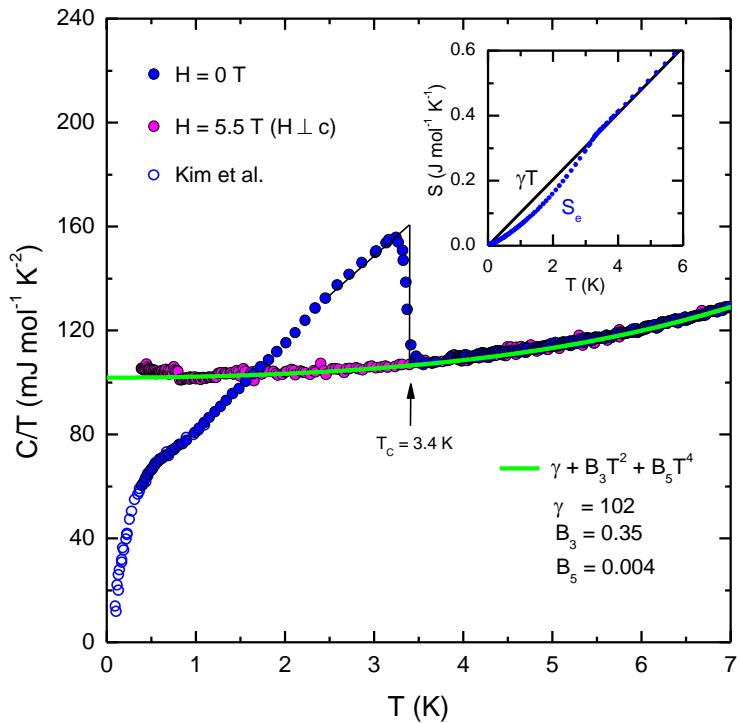


- doping and pressure are closely related:  $dg/dp \sim - dg/dx$
- uniaxial pressure is a good tuning parameter
- 33% Co good background -  $dg/dp = 0$

# Heat capacity and susceptibility

F. Hardy, et al. PRL 111, 27002  
(2013)

Heat Capacity



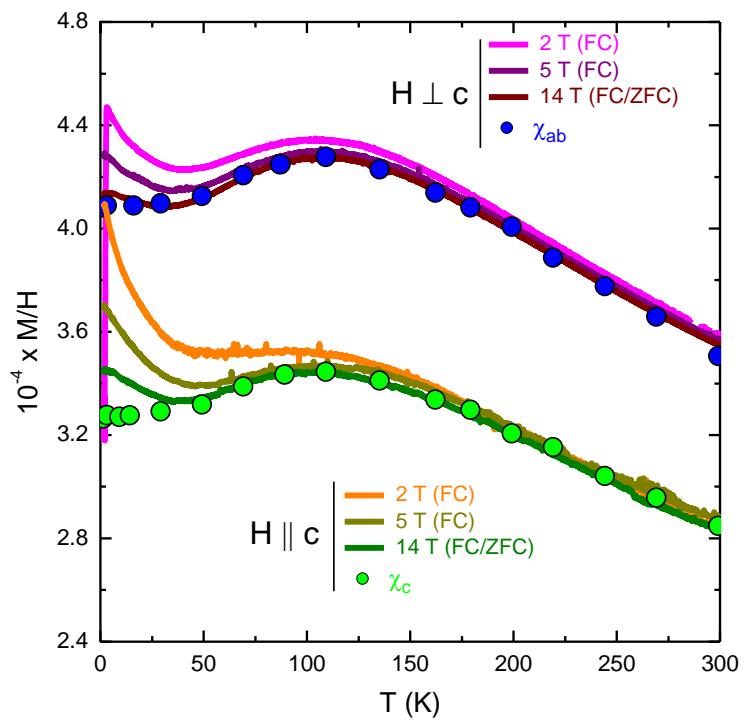
Sommerfeld coefficient

$$\gamma_n = 102 \text{ mJ mol}^{-1} \text{ K}^{-2}$$

$$(\gamma_{\text{LDA}} = 10 \text{ mJ mol}^{-1} \text{ K}^{-2})$$

Confirm heavy QP (dHvA, ARPES)

Susceptibility



Pauli susceptibility

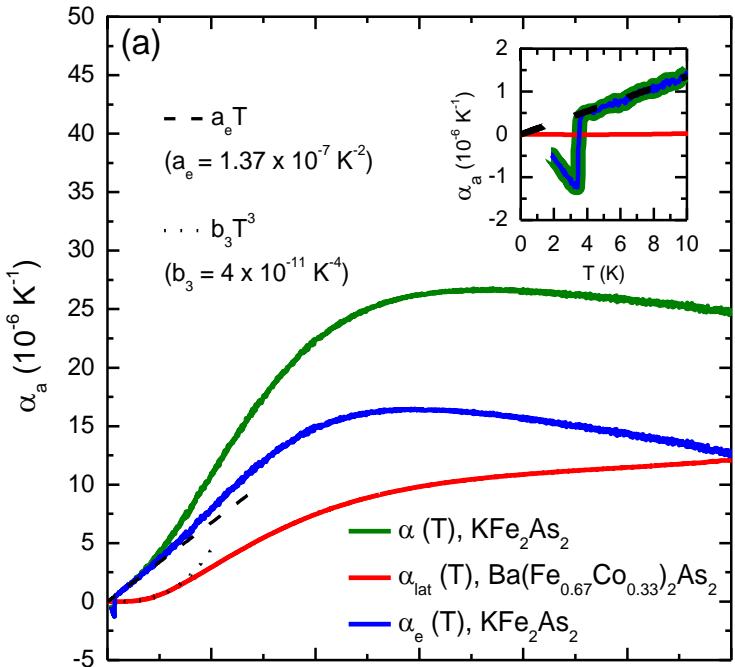
$$\chi_c = 3.3 \times 10^{-4}$$

$$\chi_{ab} = 4.1 \times 10^{-4}$$

Coherence – incoherence crossover

# Thermal expansion

F. Hardy, et al. PRL 111, 27002  
(2013)



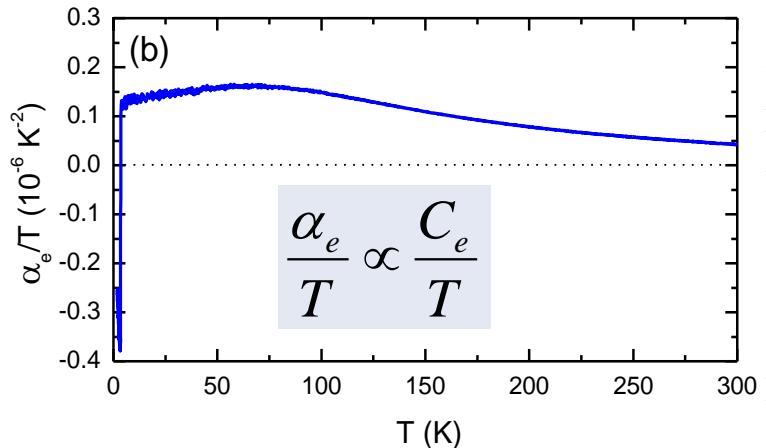
Existence of strong correlations

Similar to heavy-fermion compounds and ruthenates

Evidence for coherence-incoherence crossover

$T \ll T^*$  : heavy Landau quasiparticles  
(Fermi liquid)

$T \gg T^*$  : strongly incoherent regime  
local moment behavior  
non-linear heat capacity



LDA+DMFT: Strong Hund's coupling

Haule, et al., New J. Phys. 11, (2009) 025021

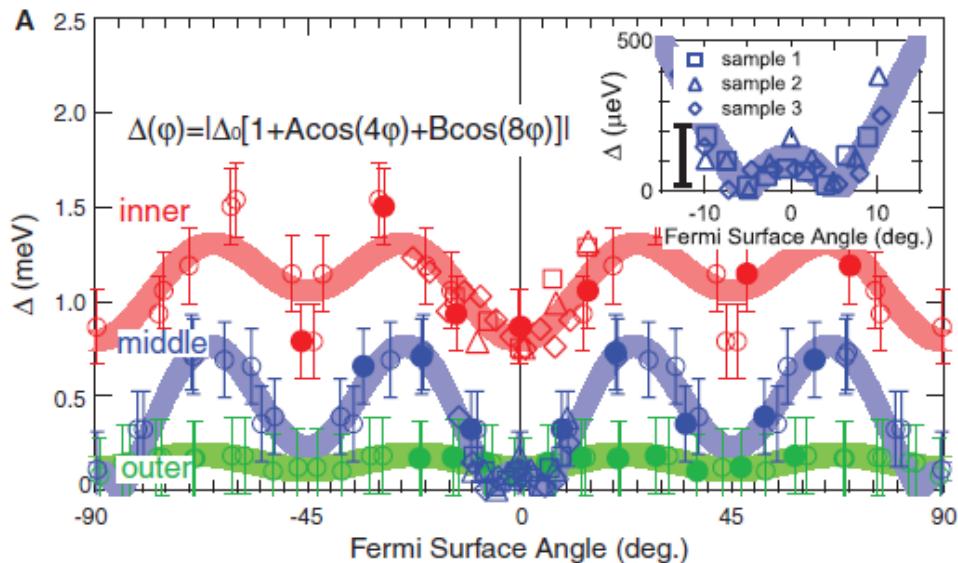
Yin, Nature Materials 10, (2011) 932

de' Medici, et al., arxiv:1212.3966 (2012)

Kondo interactions between localized spins and itinerant  $e$

L.P. Gor'kov et al., PRB 87 (2012) 024504

# Laser ARPES – KFe<sub>2</sub>As<sub>2</sub>



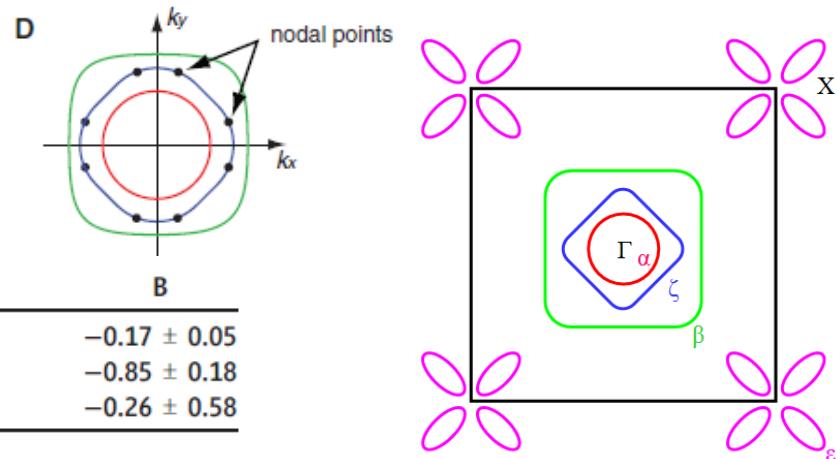
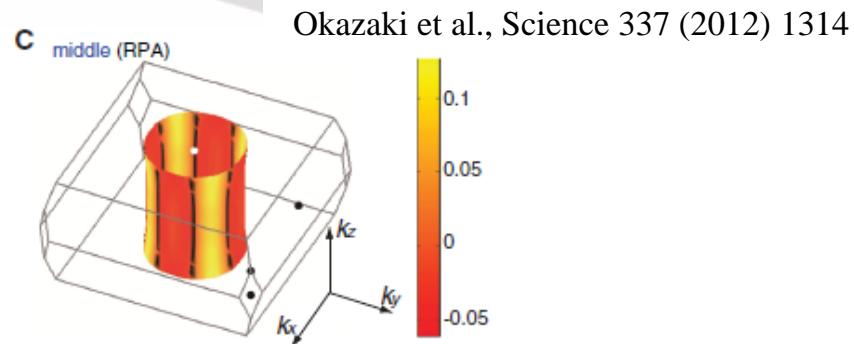
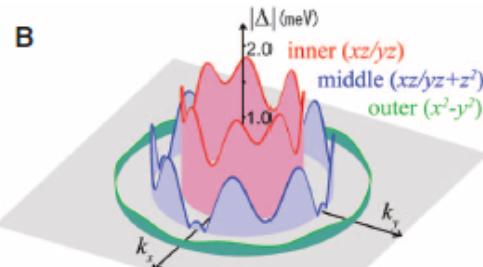
$T = 1.5$  K

Three gaps around  $\Gamma$ - point observed

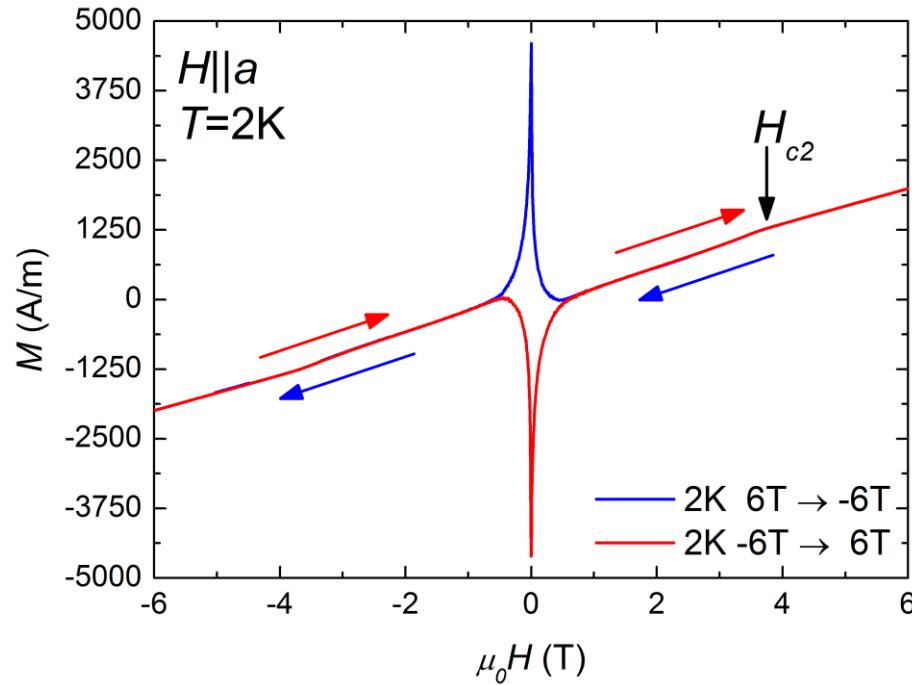
Gap around X- point not observed

Accidental Nodes (*s*-wave)

	$\Delta_0$ (meV)	$2\Delta_0/k_B T_c$	A	B
Inner FS	$1.11 \pm 0.05$	$7.58 \pm 0.34$	$-0.12 \pm 0.06$	$-0.17 \pm 0.05$
Middle FS	$0.41 \pm 0.05$	$2.80 \pm 0.34$	$-0.40 \pm 0.14$	$-0.85 \pm 0.18$
Outer FS	$0.15 \pm 0.06$	$1.02 \pm 0.41$	$-0.01 \pm 0.57$	$-0.26 \pm 0.58$



# Magnetization of KFe<sub>2</sub>As<sub>2</sub>: H||a



- reversible down to small fields  
reversible magnetization:  $M = (M^+ + M^-)/2$
- large paramagnetic signal